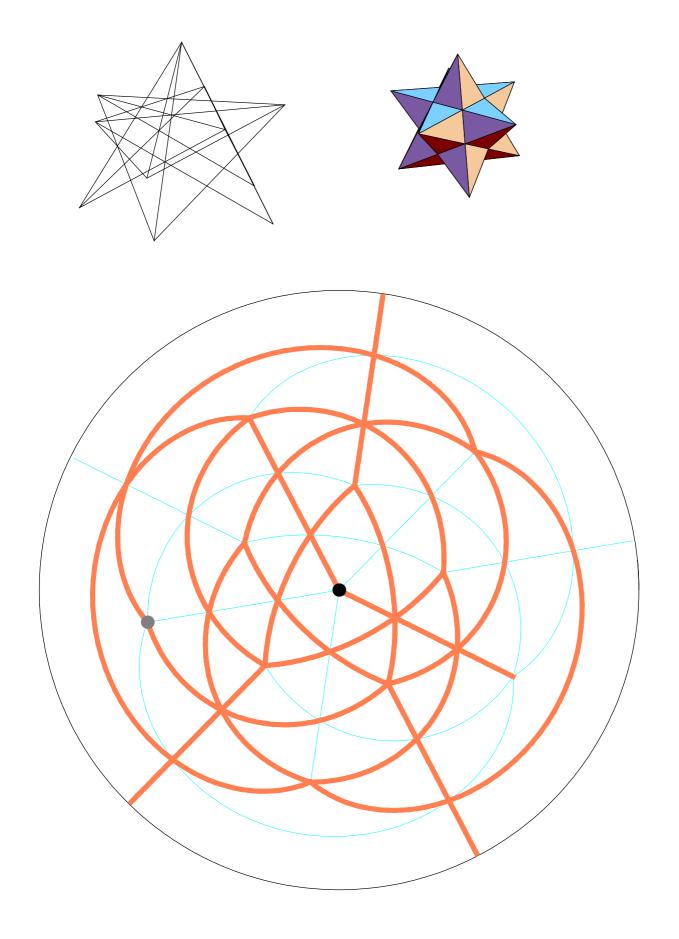
Izidor Hafner

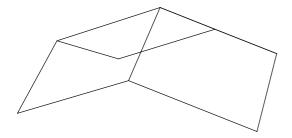
Mazes on Uniform Polyhedra

Azimuthal projection



Introduction

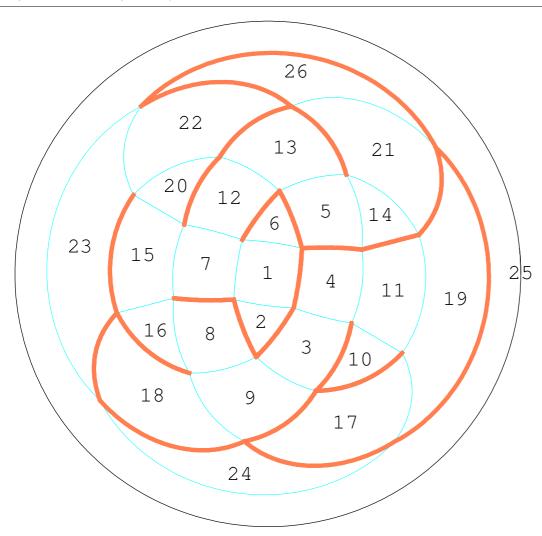
Let as take an example. We are given a uniform polyhedron.

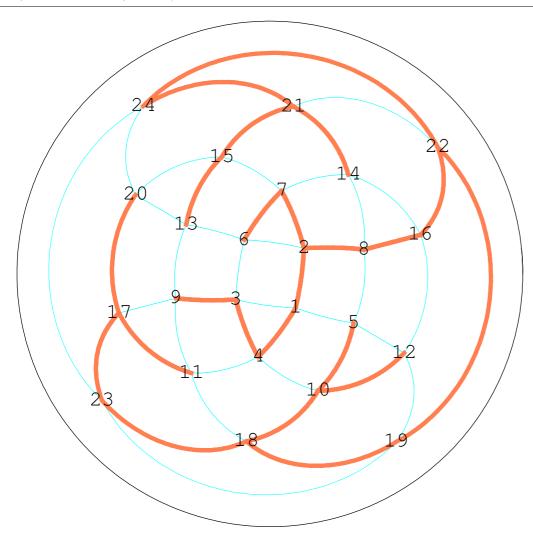




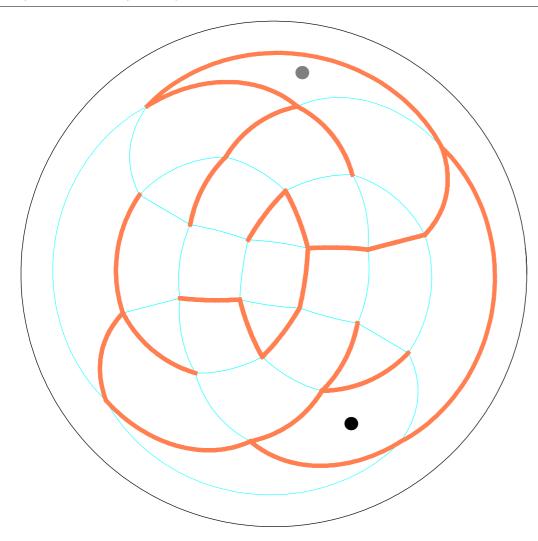
In Mathematica the polyhedron is given by a list of faces and with a list of koordinates of vertices [Roman E. Maeder, The Mathematica Programmer II, Academic Press1996]. The list of faces consists of a list of lists, where a face is represented by a list of vertices, which is given by a matrix. Let us show the first five faces:

The nest two figures represent faces and vertices. The polyhedron is projected onto supescribed sphere and the sphere is projected by a cartographic projection.

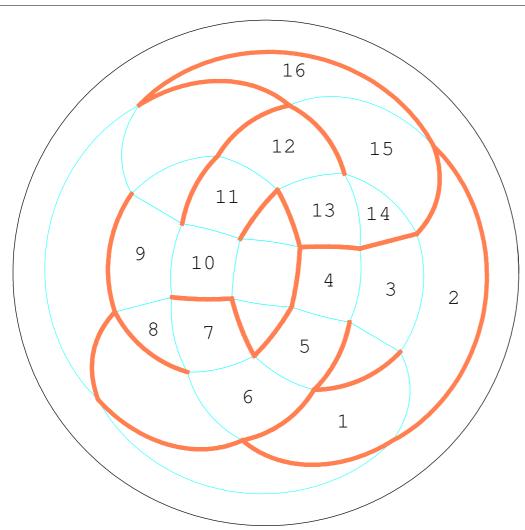




The problem is to find the path from the black dot to gray dot, where thick lines represent walls of a maze.

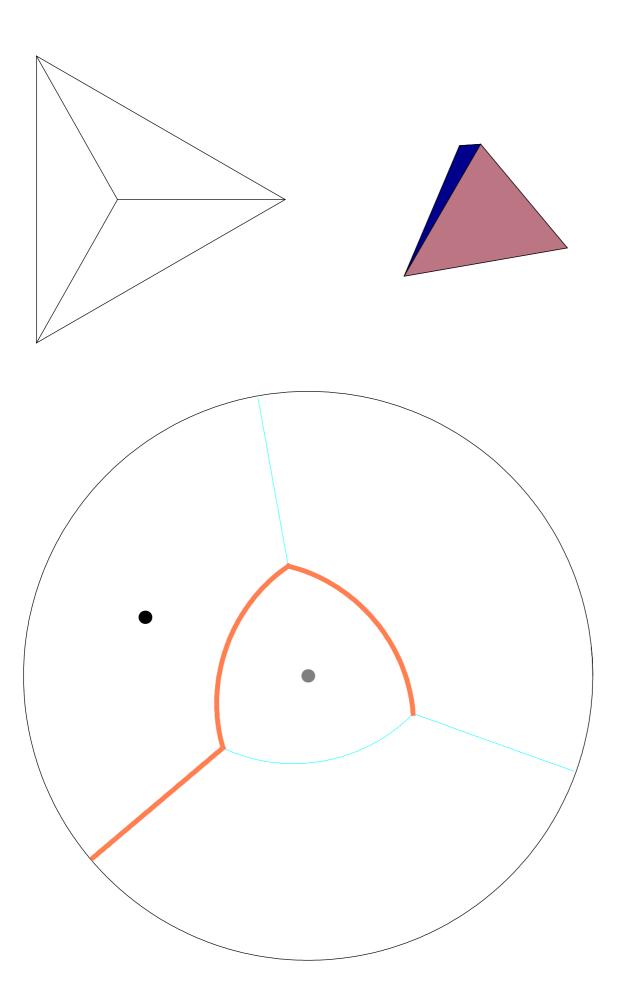


The solution is given by a list of faces passed from the black to gray dot.

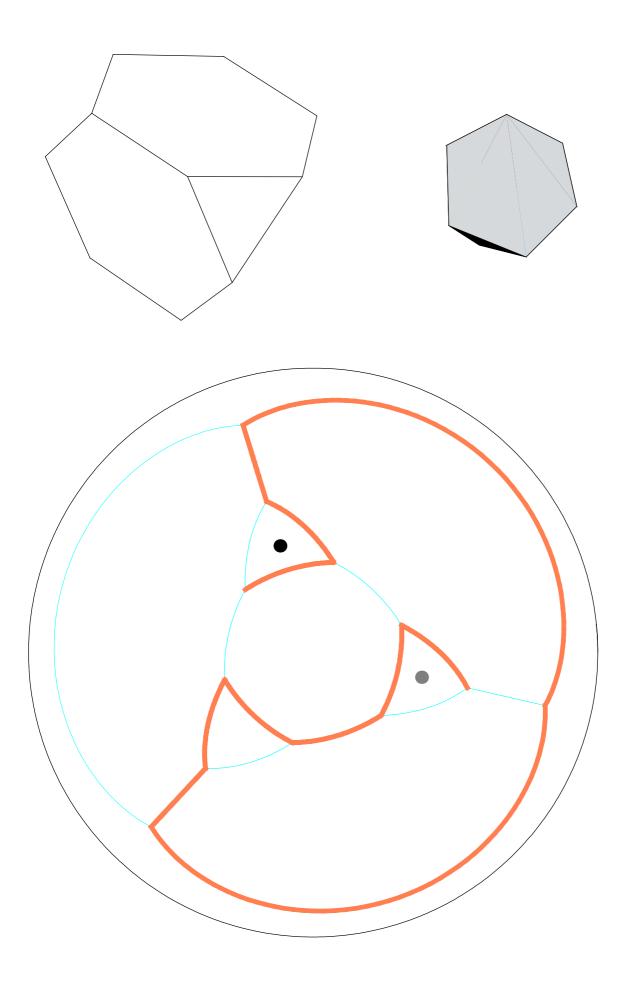


Problems

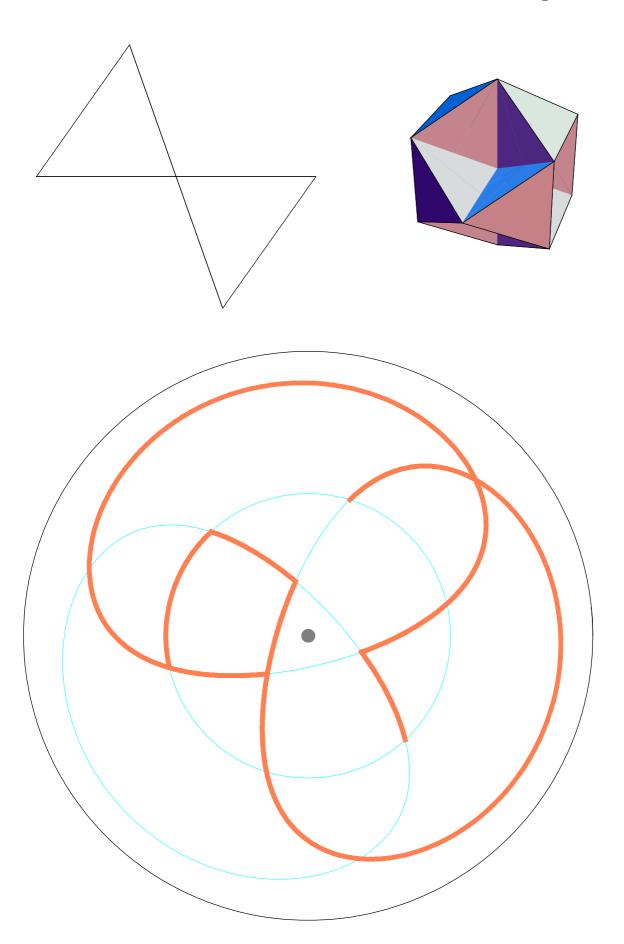
tetrahedron ${3,3,3}$



truncated tetrahedron $\{6, 6, 3\}$

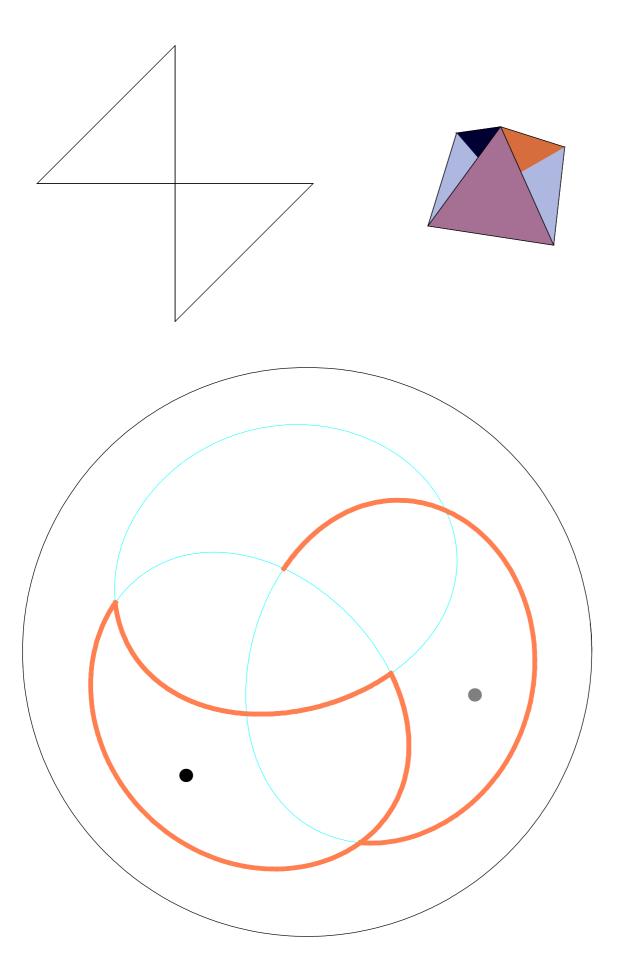


octahemioctahedron $\left\{6,\,\frac{3}{2},\,6,\,3\right\}$

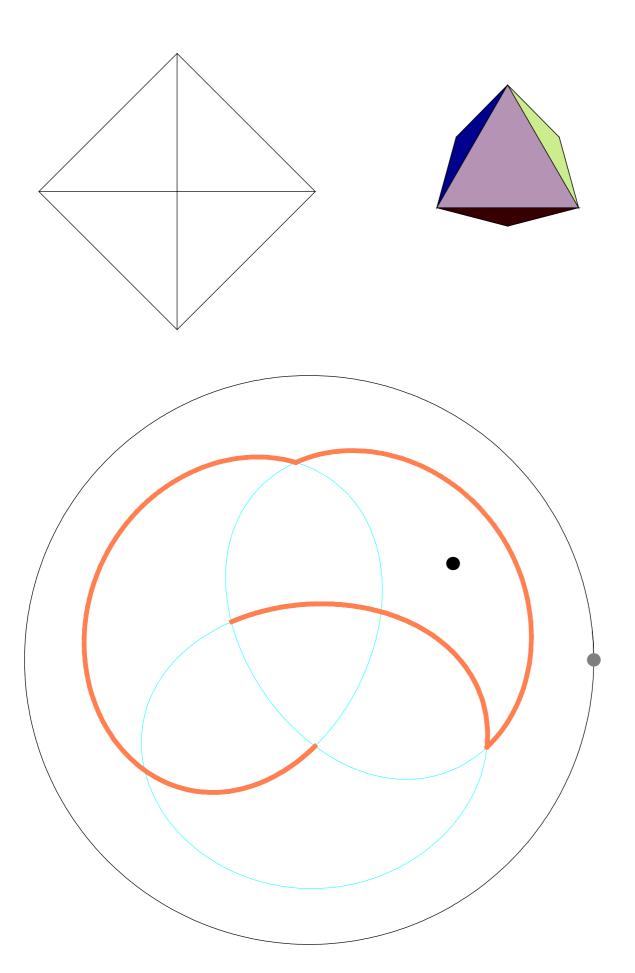


tetrahemihexahedron

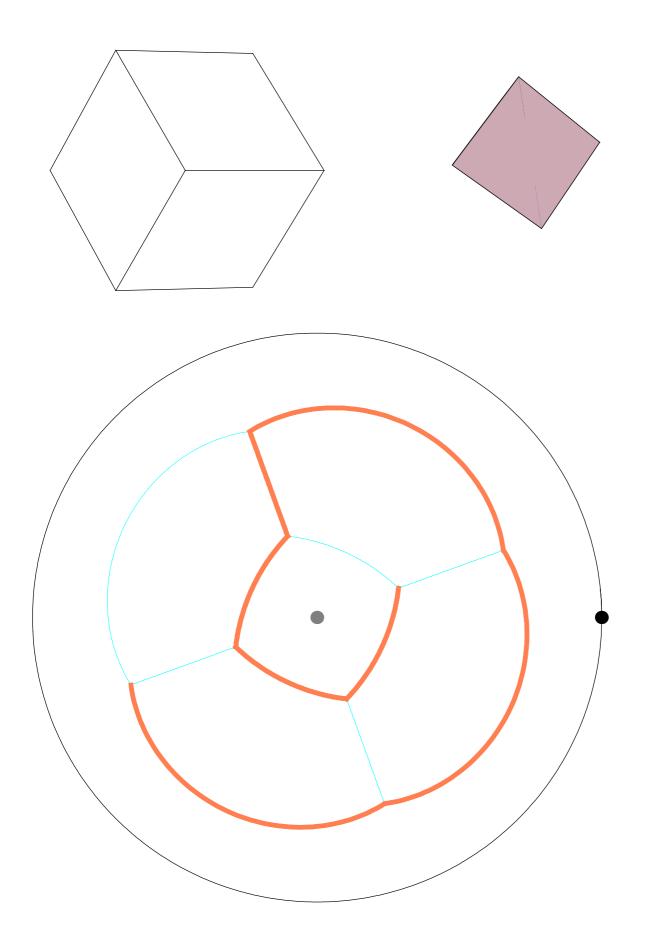
$$\left\{4, \frac{3}{2}, 4, 3\right\}$$



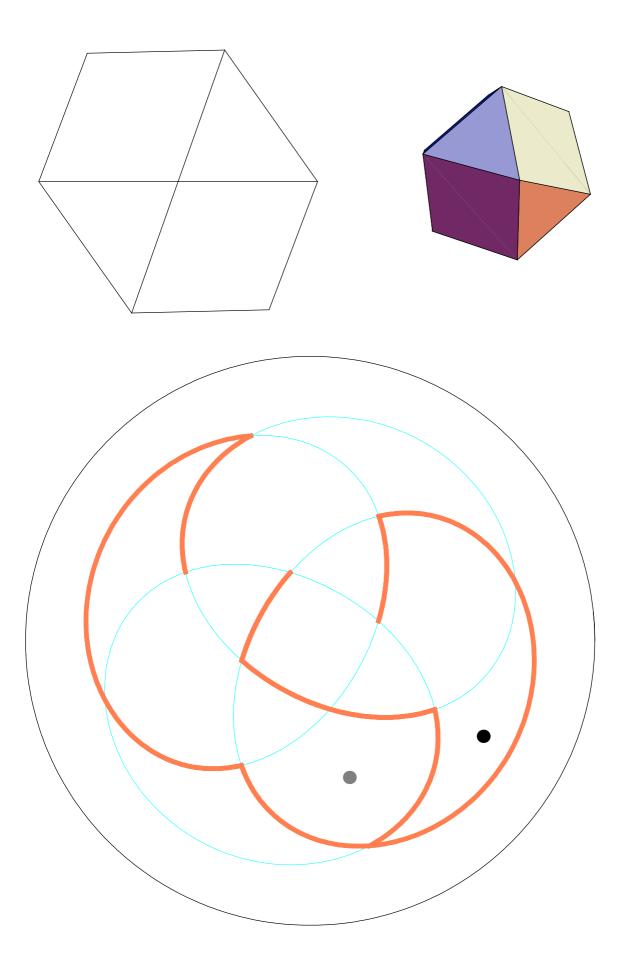
octahedron $\{3, 3, 3, 3\}$



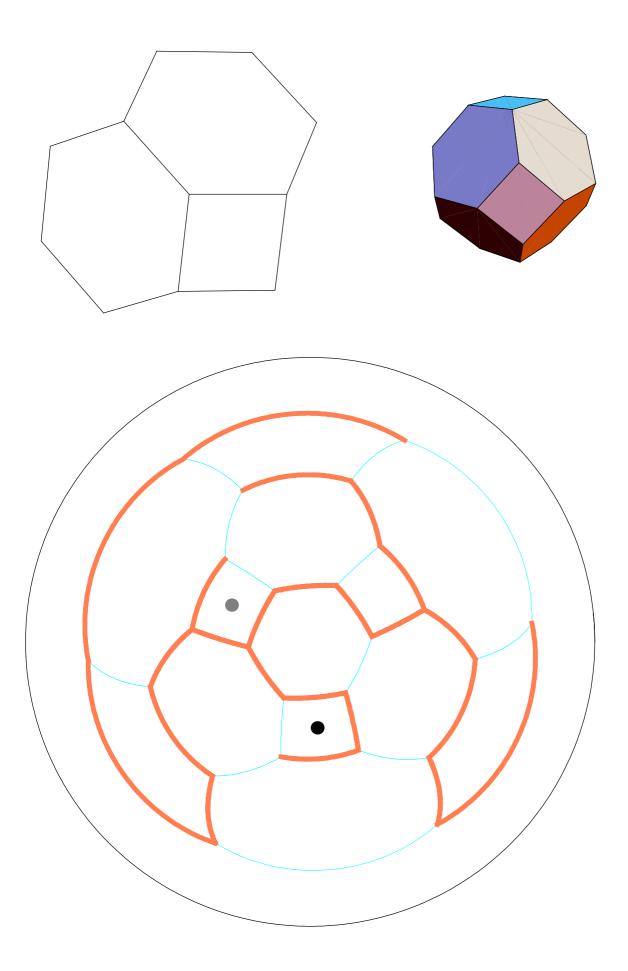
cube {4, 4, 4}



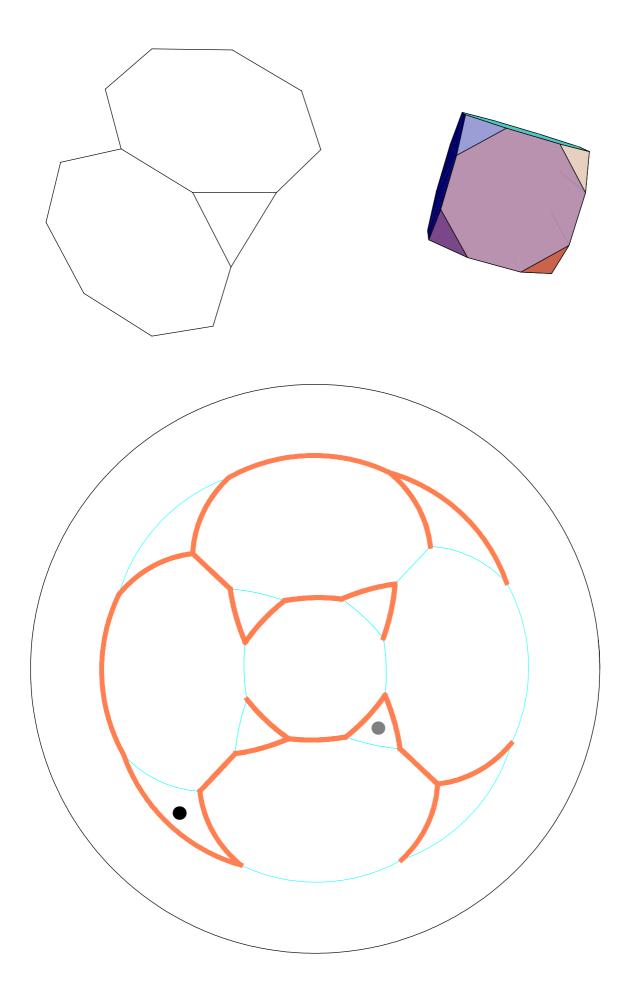
 $cuboctahedron \\ \{3,4,3,4\}$

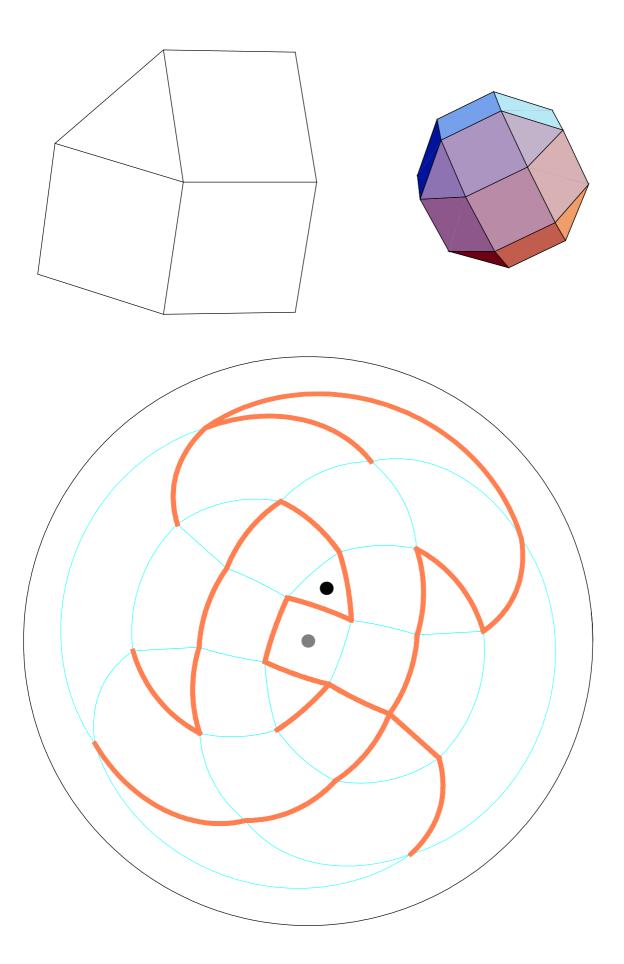


truncated octahedron $\{6, 6, 4\}$



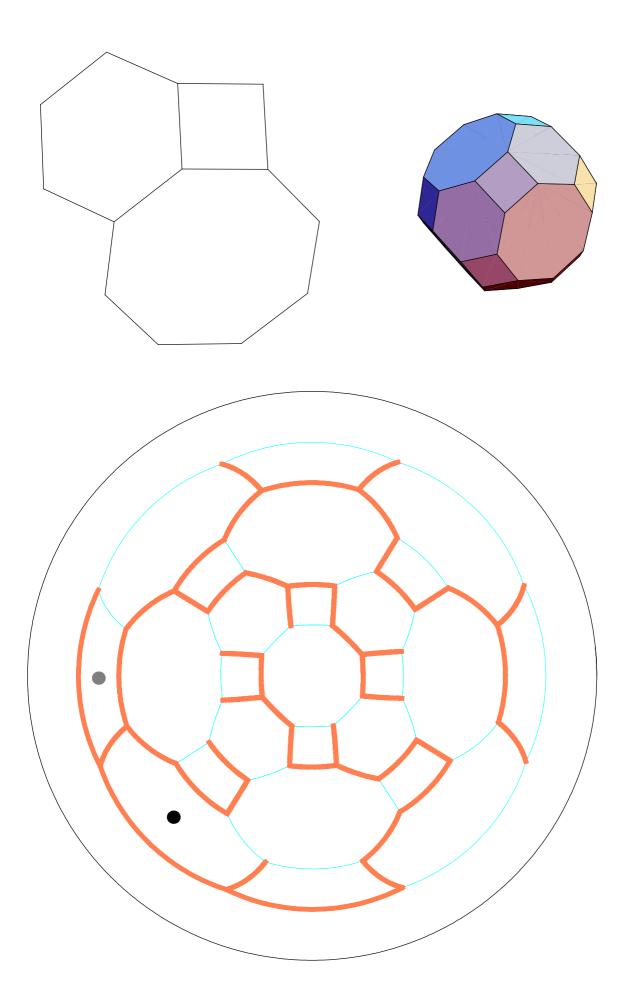
truncated cube $\{8, 8, 3\}$



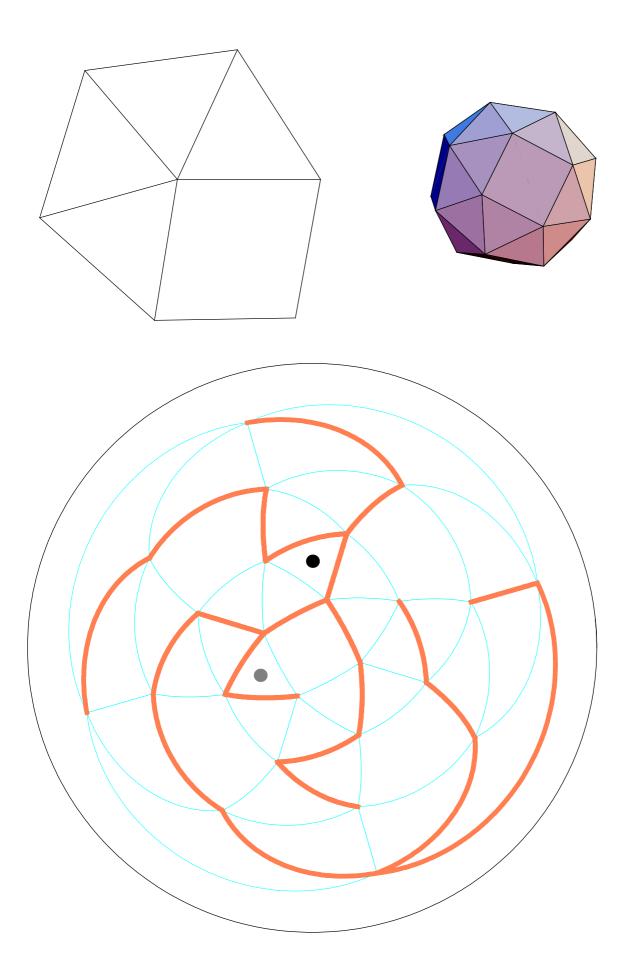


truncated cuboctahedron

{4, 6, 8}

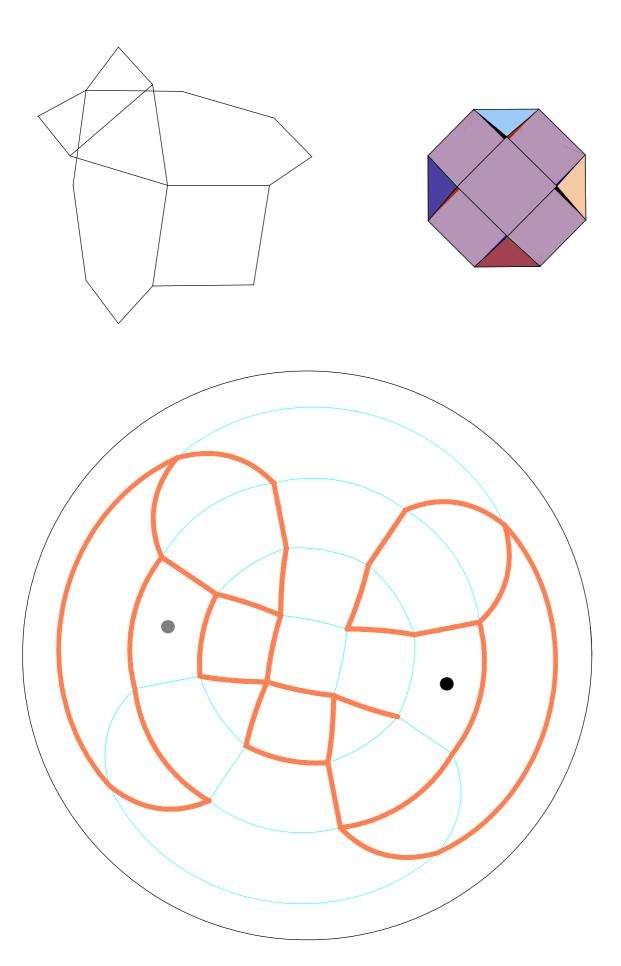


snub cube ${3, 3, 3, 3, 4}$



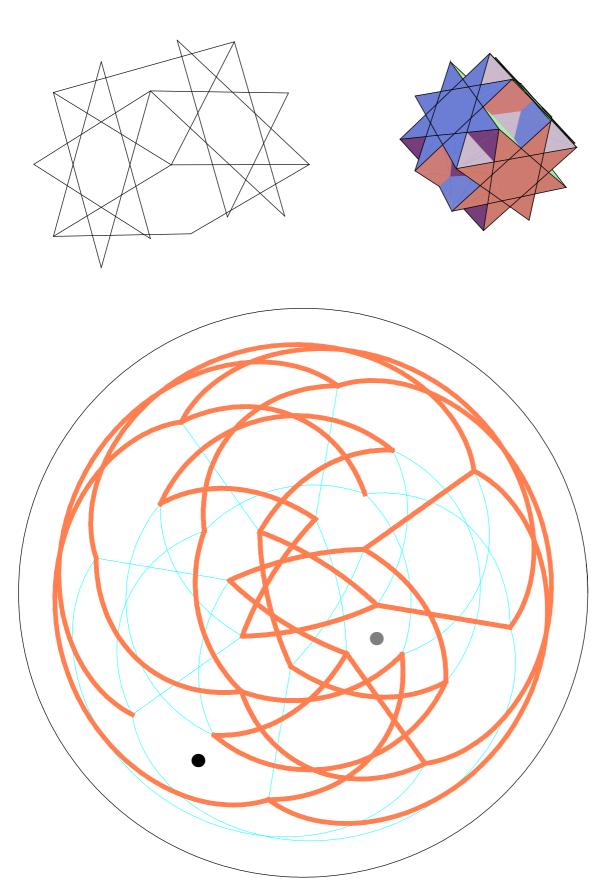
small cubicuboctahedron

$$\left\{8, \frac{3}{2}, 8, 4\right\}$$



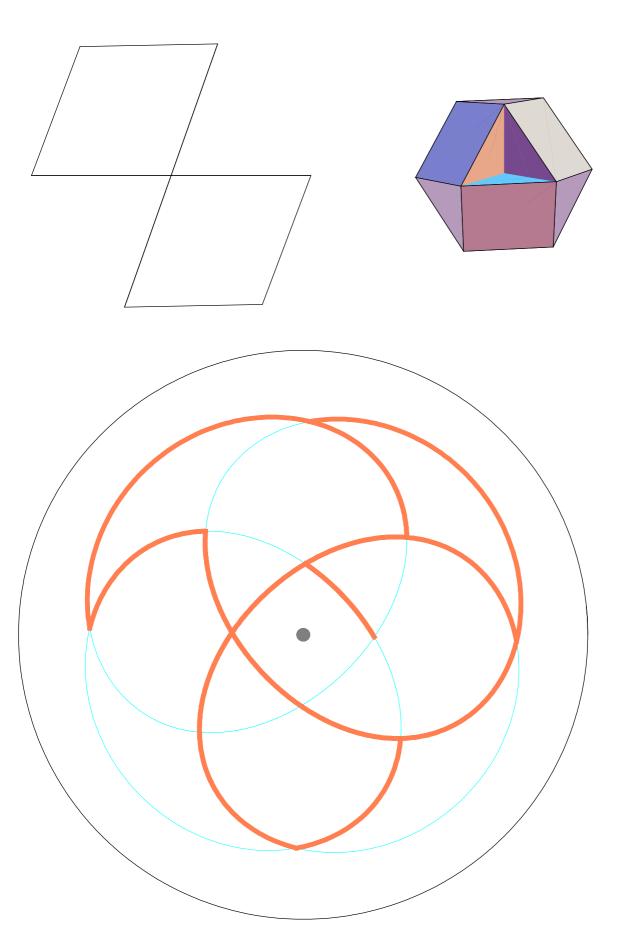
great cubicuboctahedron

$$\left\{\frac{8}{3}, 3, \frac{8}{3}, 4\right\}$$



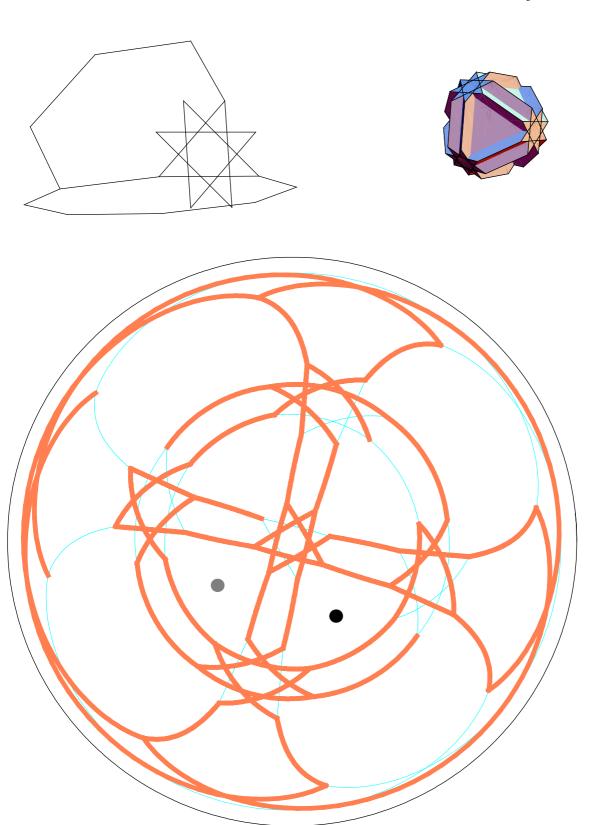
cubohemioctahedron

$$\left\{6, \frac{4}{3}, 6, 4\right\}$$



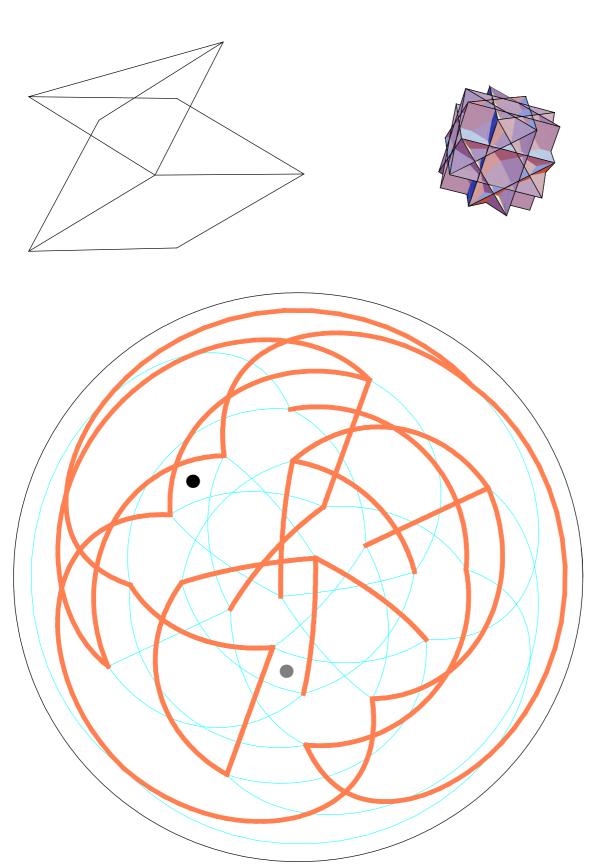
cubitruncated cuboctahedron

 $\left\{\frac{8}{3}, 6, 8\right\}$



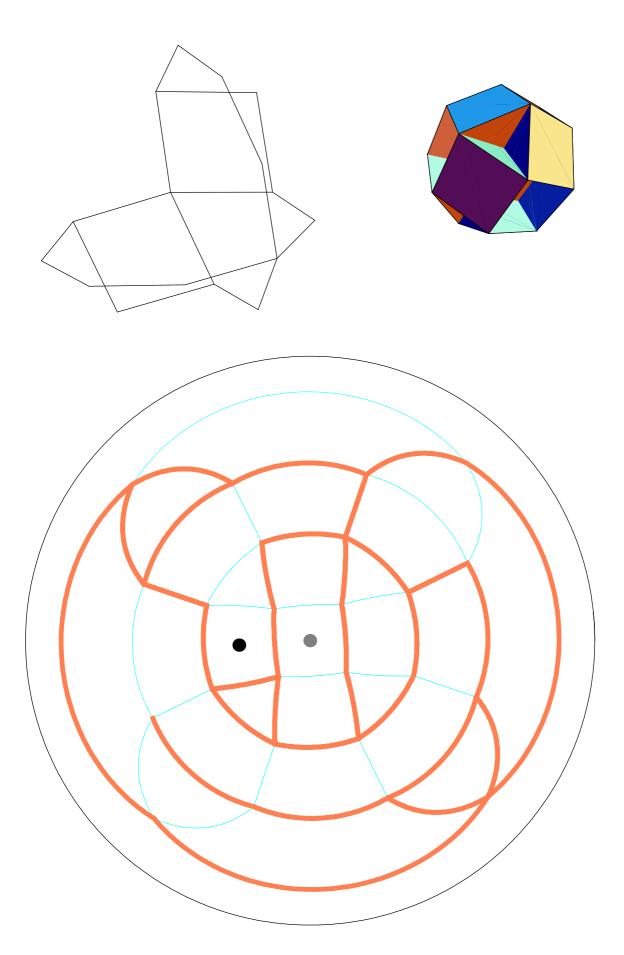
great rhombicuboctahedron

 $\left\{4, \frac{3}{2}, 4, 4\right\}$



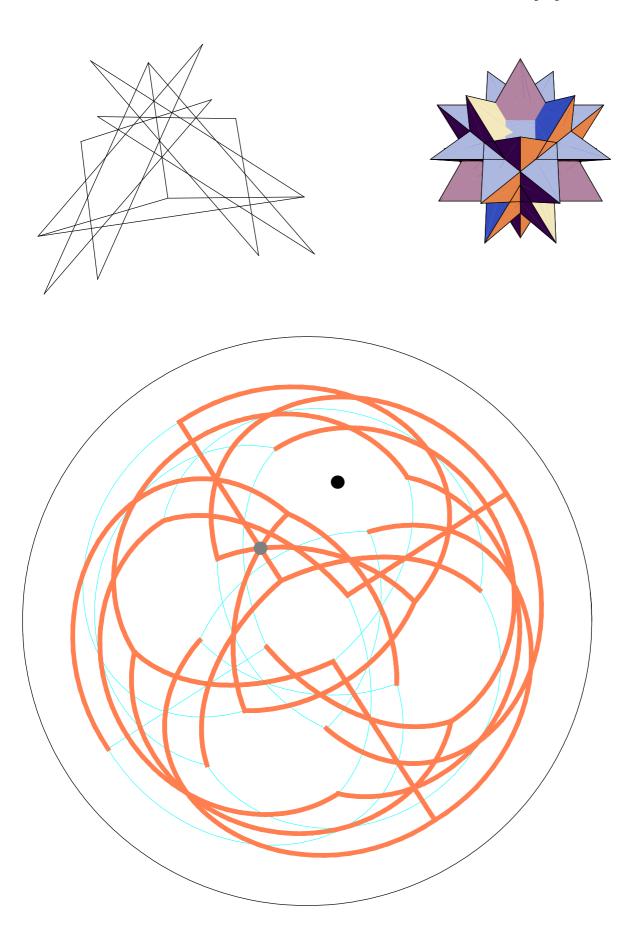
small rhombihexahedron

$$\left\{8, 4, \frac{8}{7}, \frac{4}{3}\right\}$$



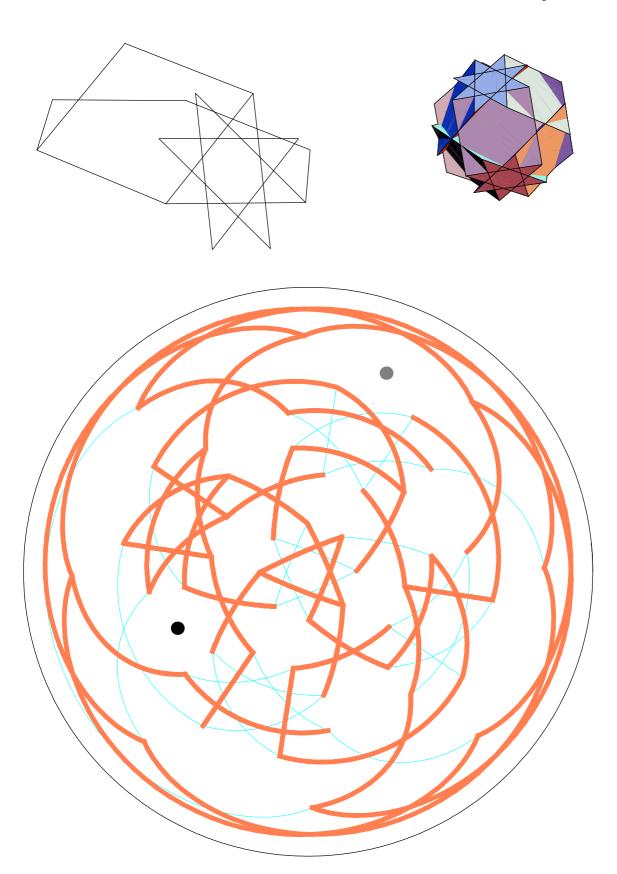
stellated truncated hexahedron

$$\left\{\frac{8}{3}, \frac{8}{3}, 3\right\}$$



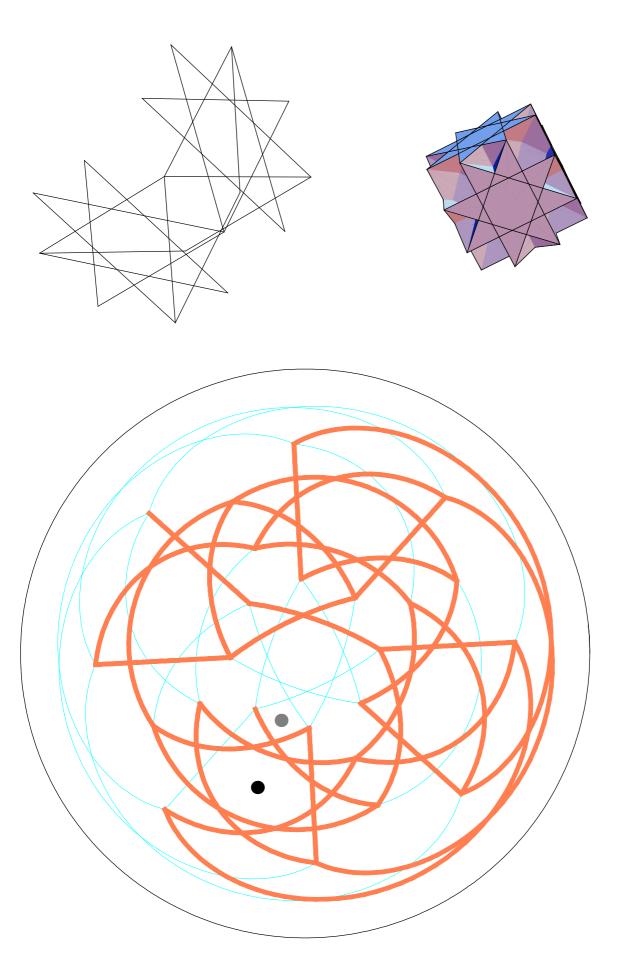
great truncated cuboctahedron

 $\left\{\frac{8}{3}, 4, 6\right\}$

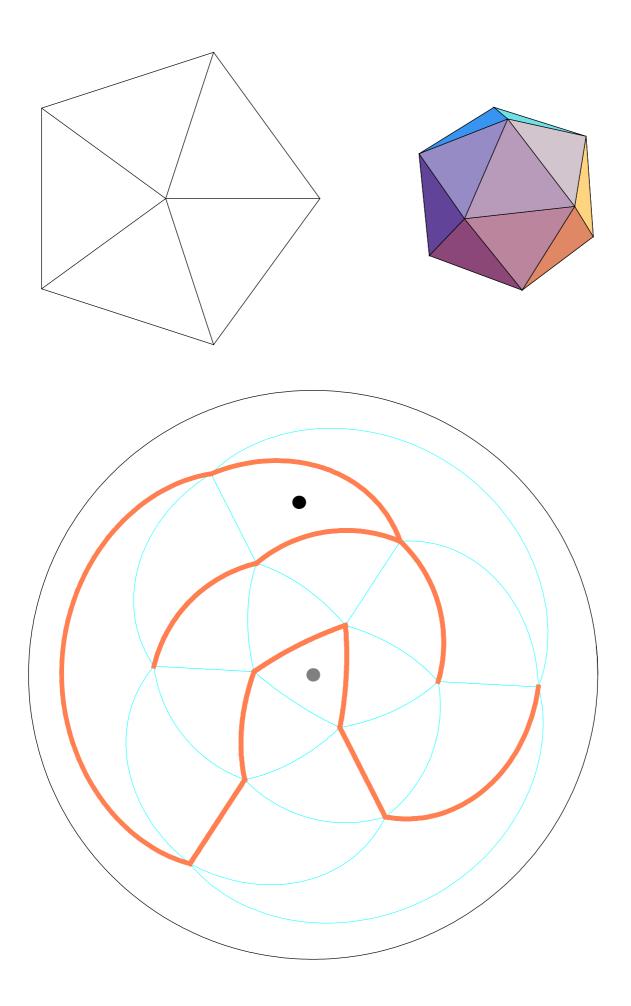


great rhombihexahedron

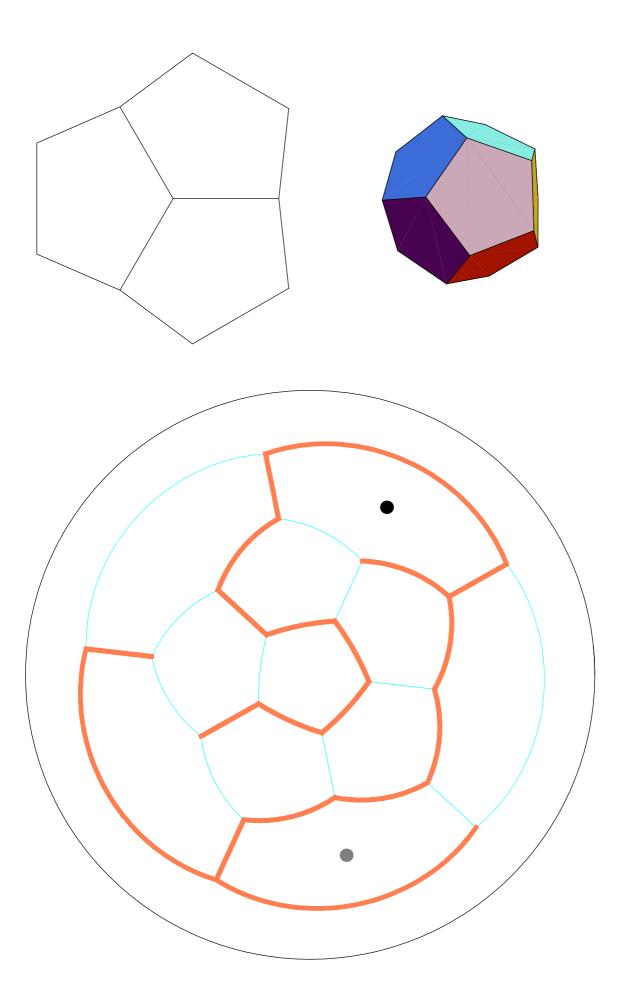
$$\left\{4, \frac{8}{3}, \frac{4}{3}, \frac{8}{5}\right\}$$



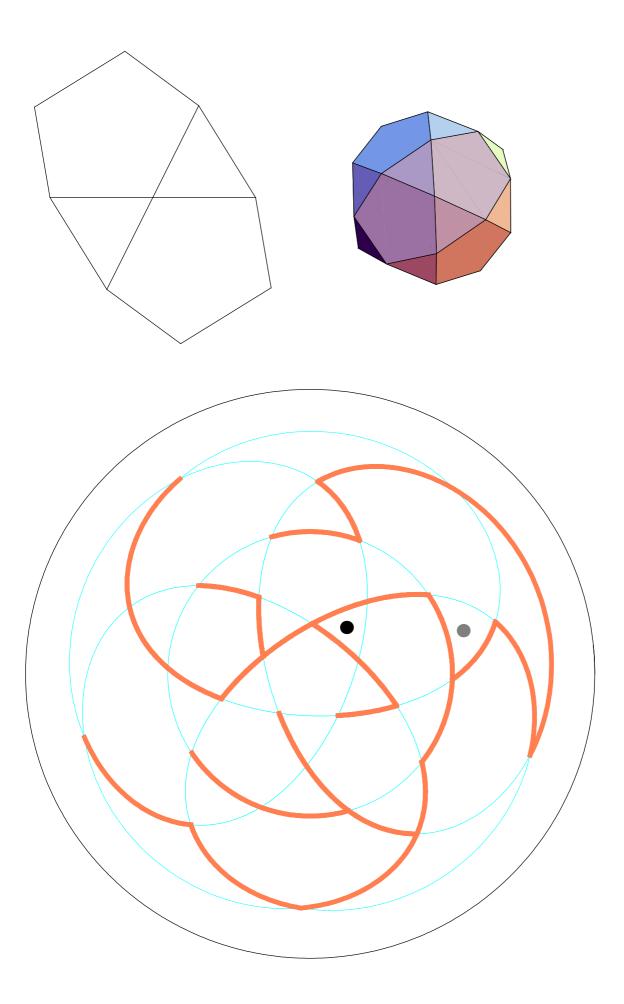
icosahedron ${3, 3, 3, 3, 3}$



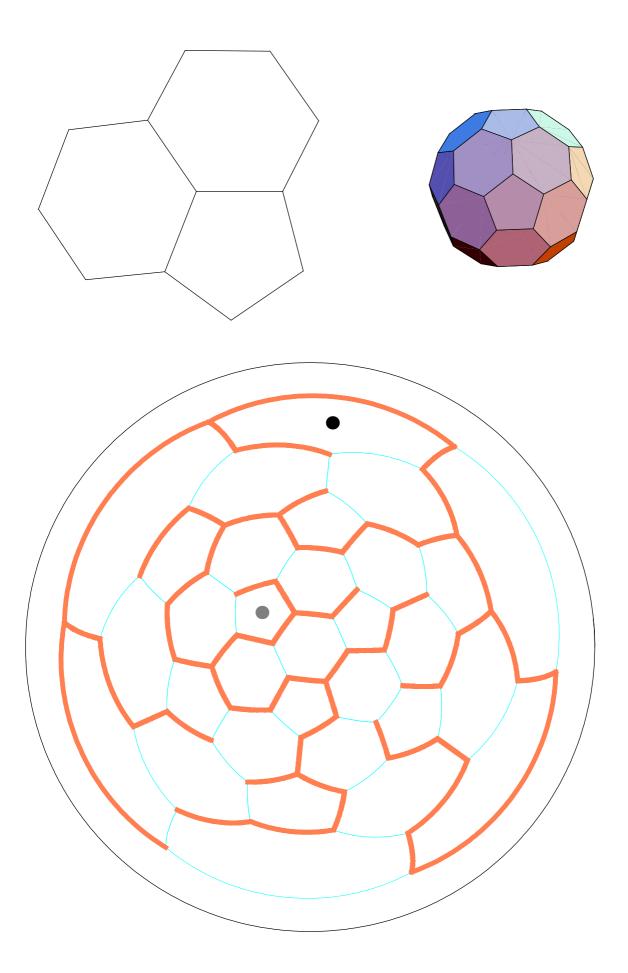
dodecahedron {5, 5, 5}



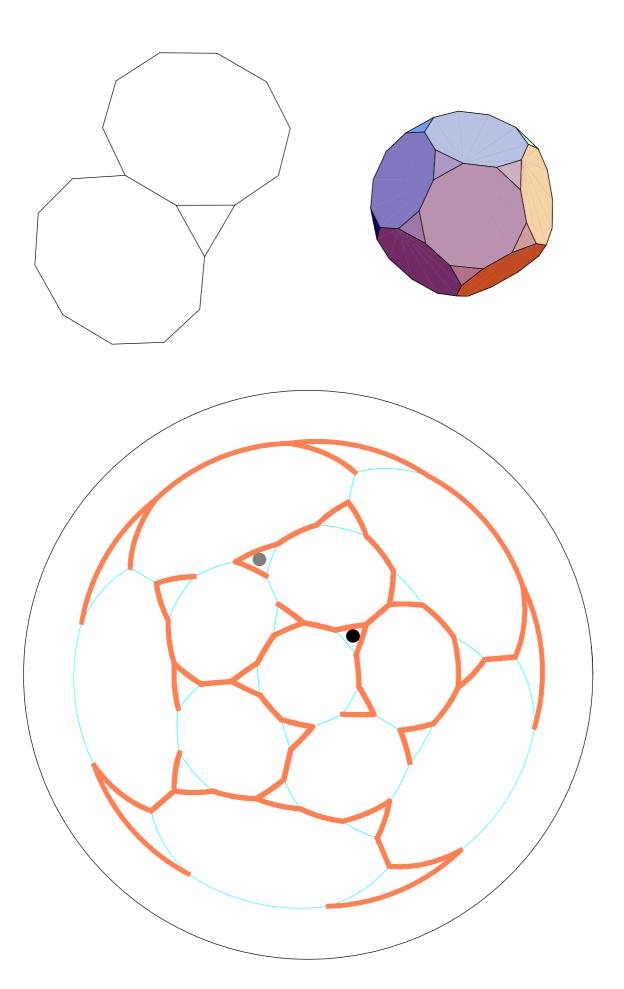
icosidodecahedron $\{3, 5, 3, 5\}$



truncated icosahedron $\{6, 6, 5\}$

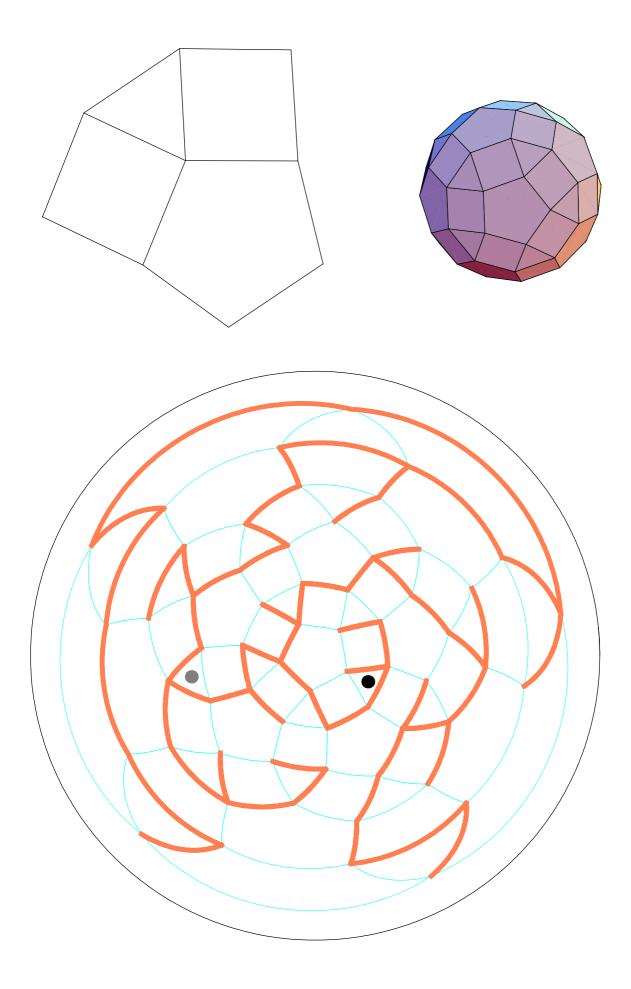


truncated dodecahedron {10, 10, 3}



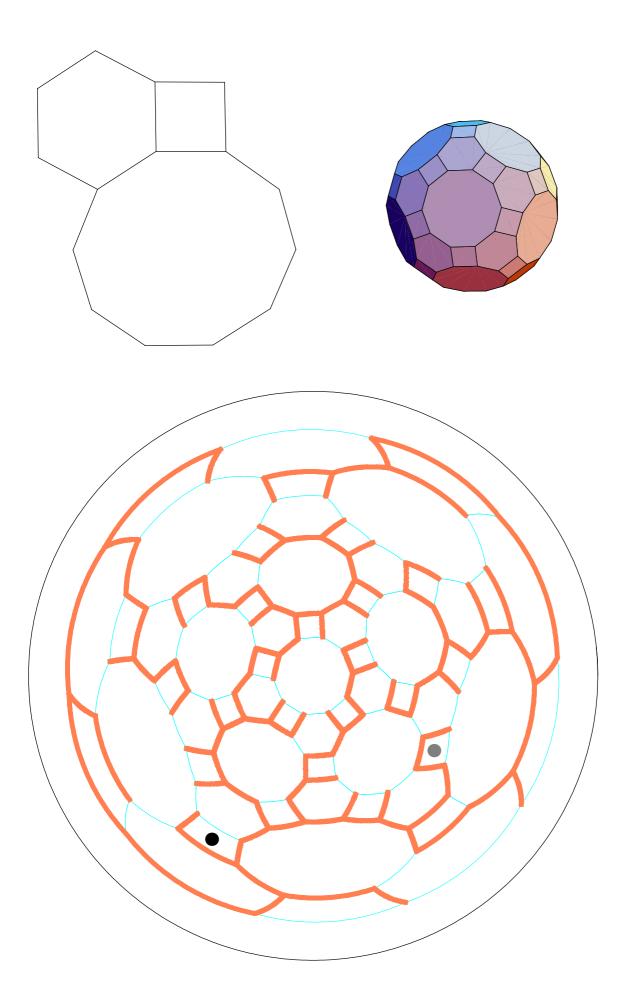
rhombicosidodecahedron

{4, 3, 4, 5}

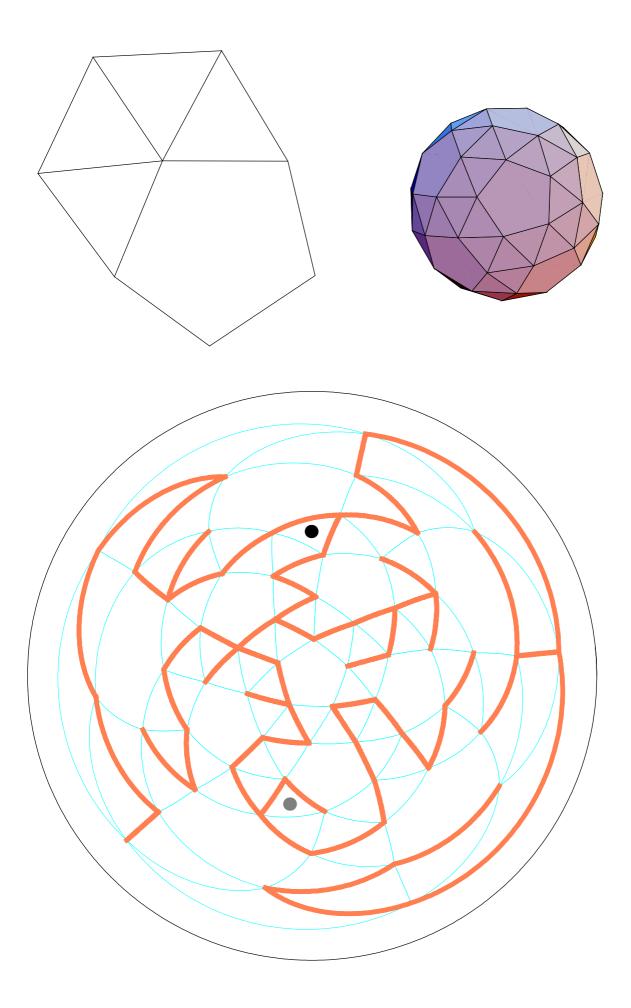


truncated icosidodecahedron

{4, 6, 10}

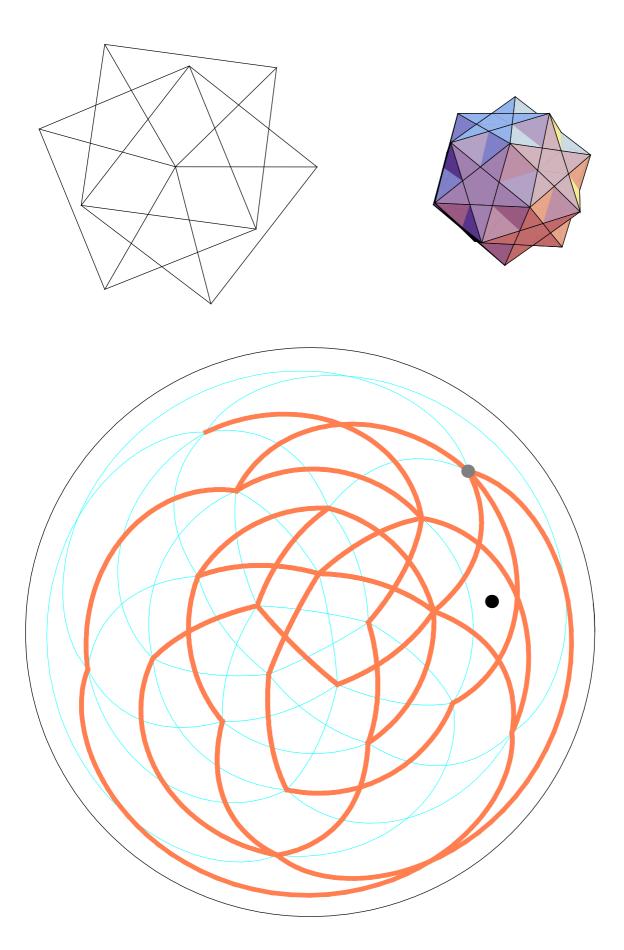


snub dodecahedron $\{3, 3, 3, 3, 5\}$



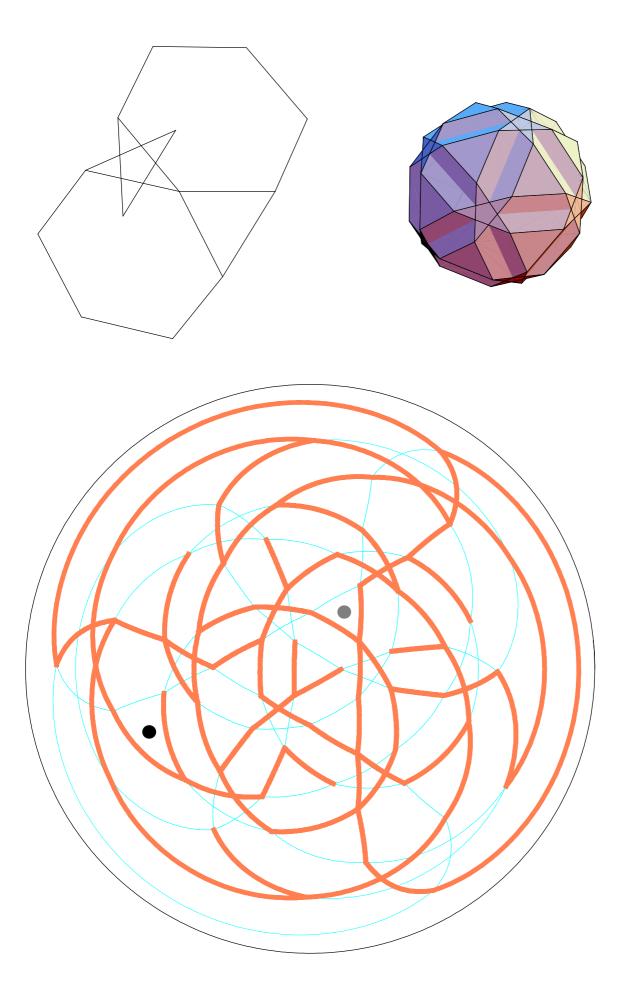
small ditrigonal icosidodecahedron

$$\left\{\frac{5}{2}, 3, \frac{5}{2}, 3, \frac{5}{2}, 3\right\}$$



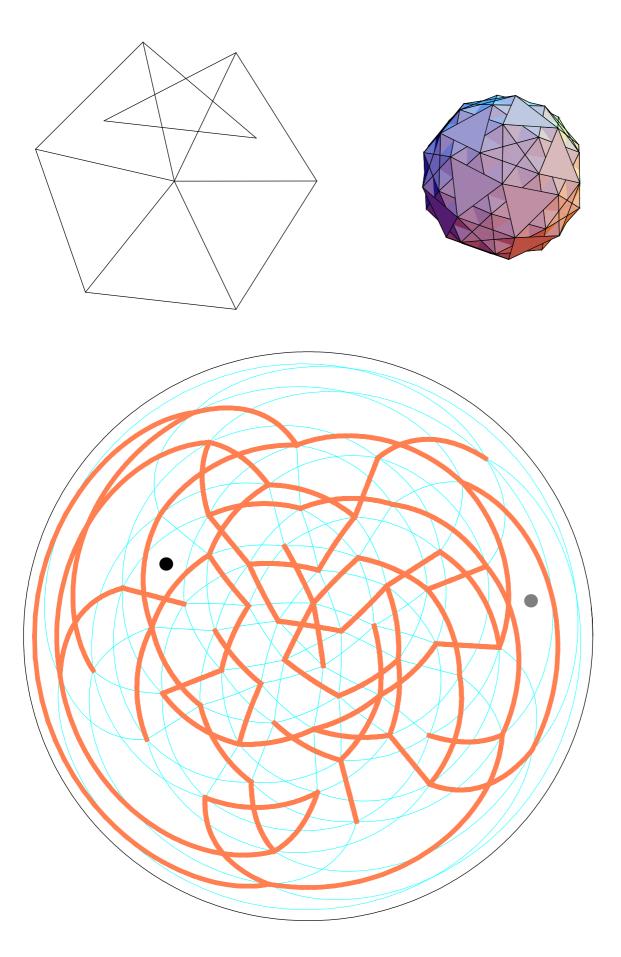
small icosicosidodecahedron

$$\left\{6, \frac{5}{2}, 6, 3\right\}$$



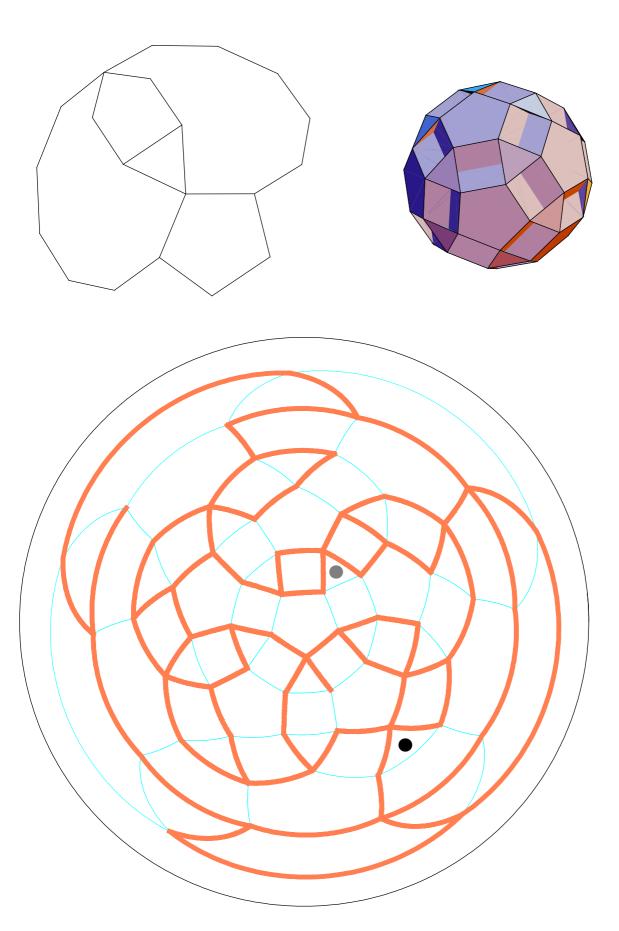
small snub icosicosidodecahedron

$${3, \frac{5}{2}, 3, 3, 3, 3}$$



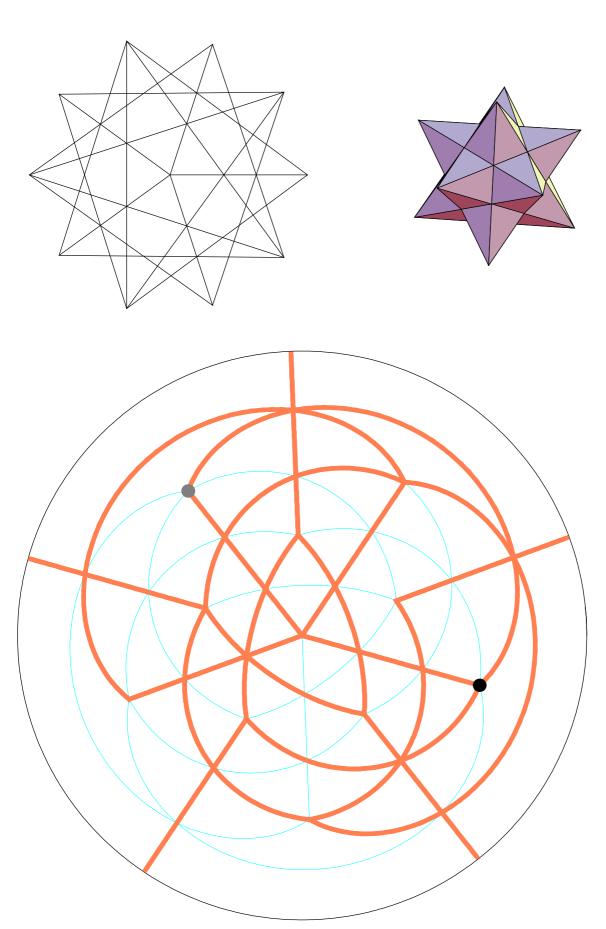
small dodecicosidodecahedron

$$\left\{10, \frac{3}{2}, 10, 5\right\}$$

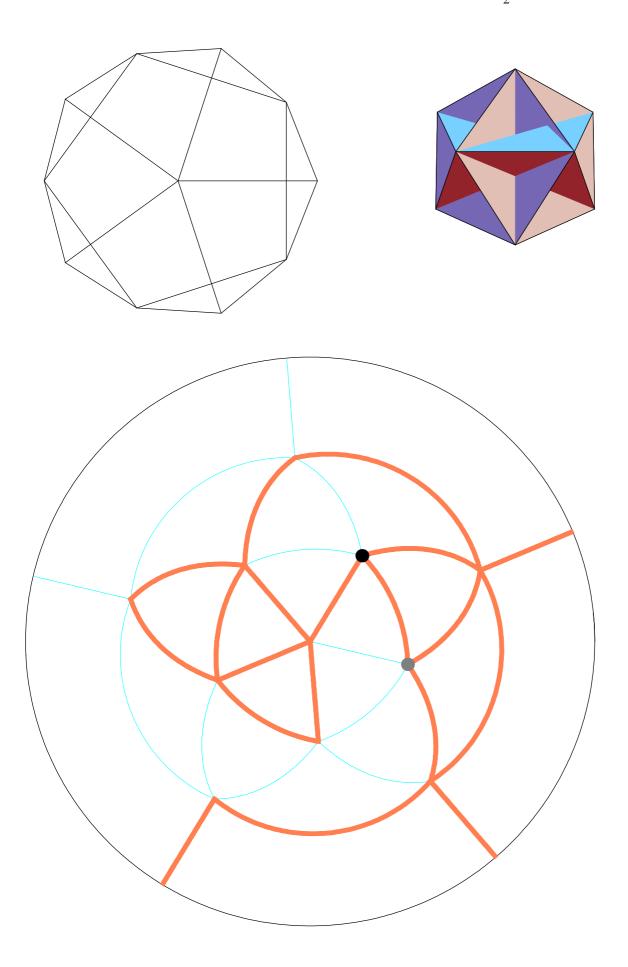


small stellated dodecahedron

$$\left\{\frac{5}{2}, \frac{5}{2}, \frac{5}{2}, \frac{5}{2}, \frac{5}{2}\right\}$$

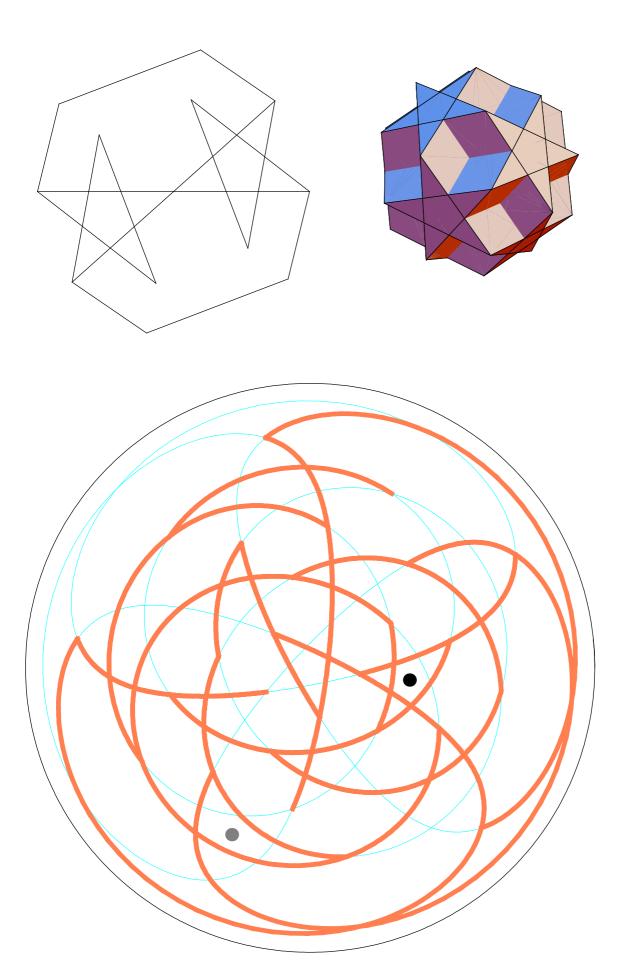


great dodecahedron $\frac{1}{2}\left\{5,\,5,\,5,\,5\right\}$



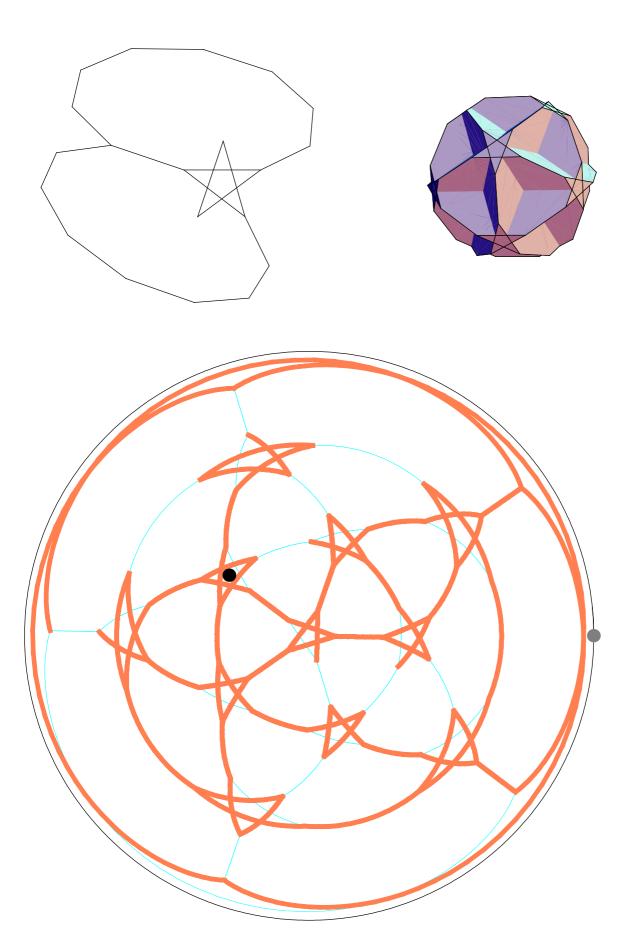
dodecadodecahedron

$$\left\{\frac{5}{2}, 5, \frac{5}{2}, 5\right\}$$



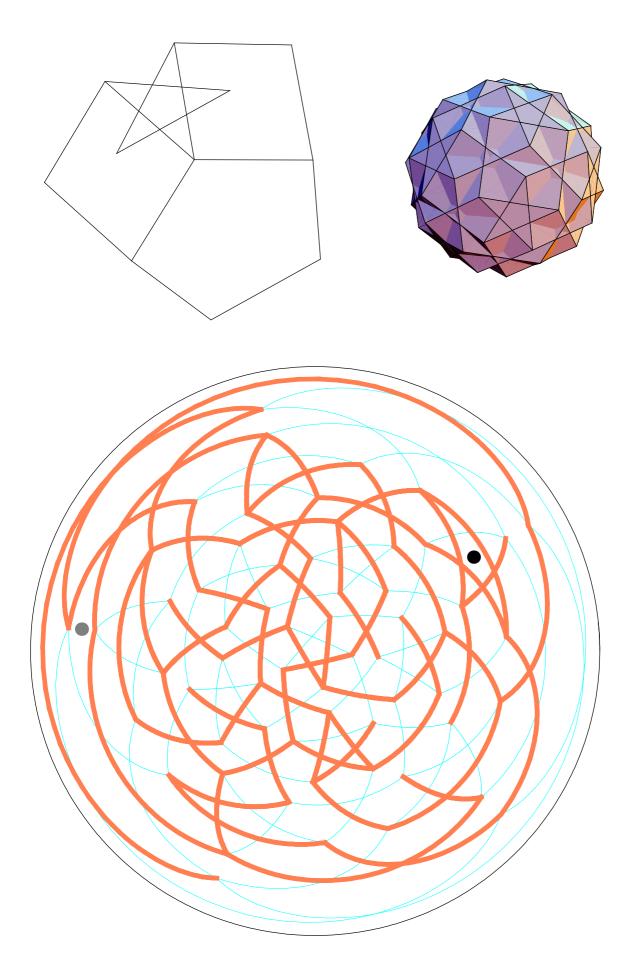
truncated great dodecahedron

$$\left\{10, 10, \frac{5}{2}\right\}$$



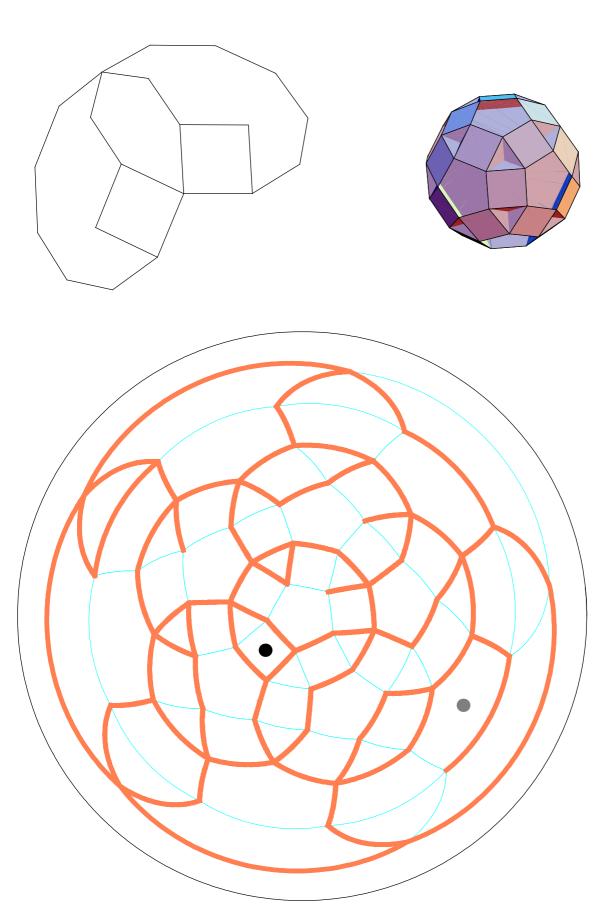
rhombidodecadodecahedron

$$\left\{4, \frac{5}{2}, 4, 5\right\}$$



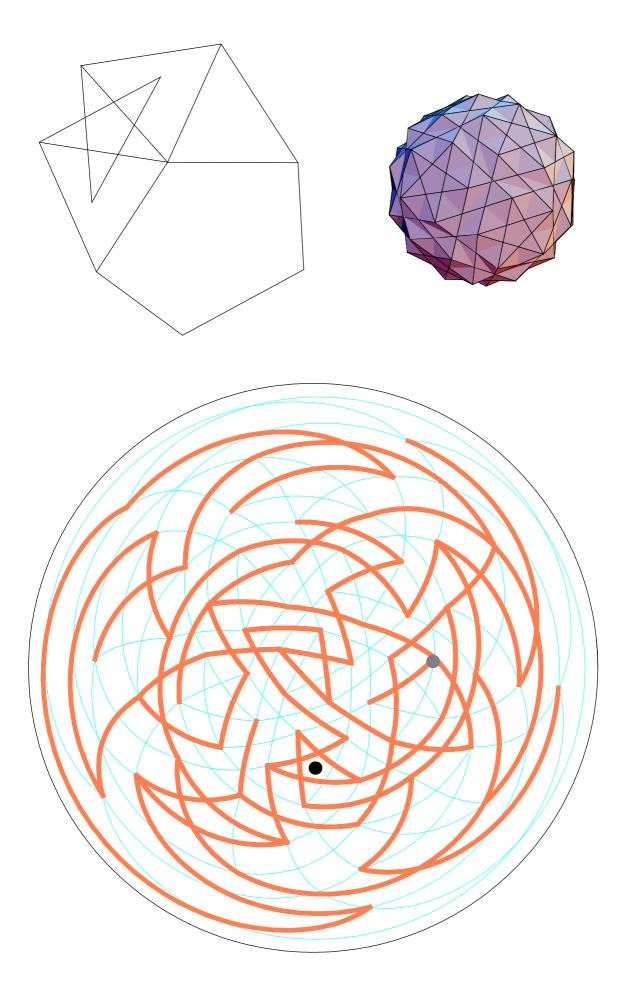
small rhombidodecahedron

$$\left\{10, 4, \frac{10}{9}, \frac{4}{3}\right\}$$



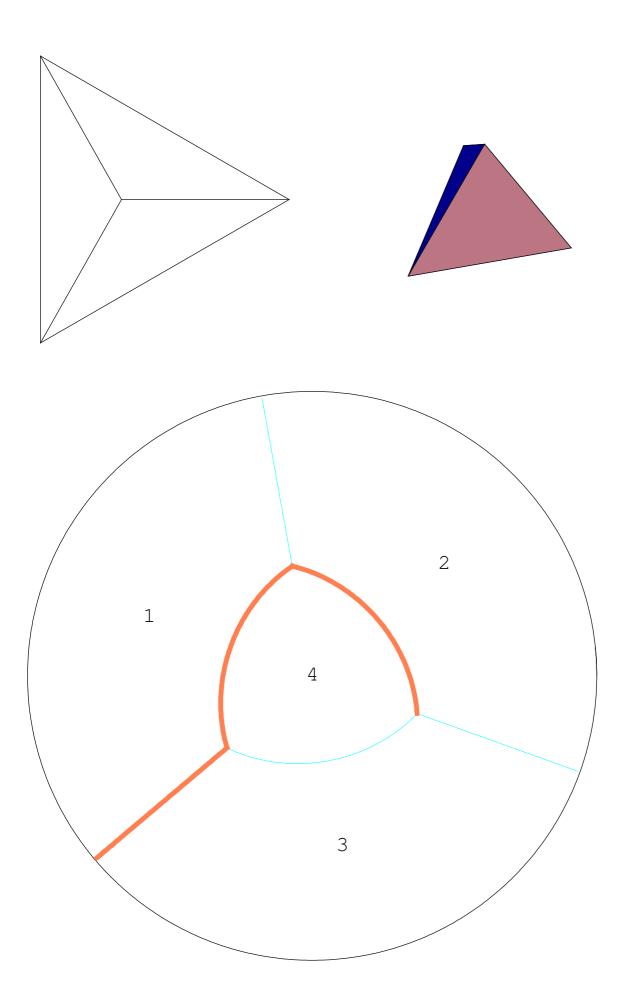
snub dodecadodecahedron

$${3, 3, \frac{5}{2}, 3, 5}$$

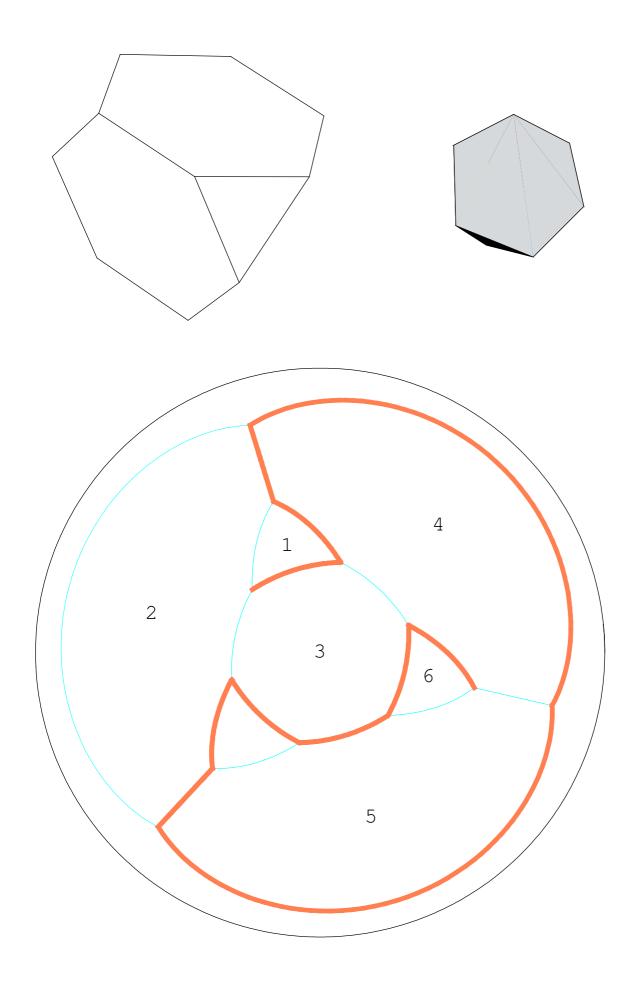


Solutions

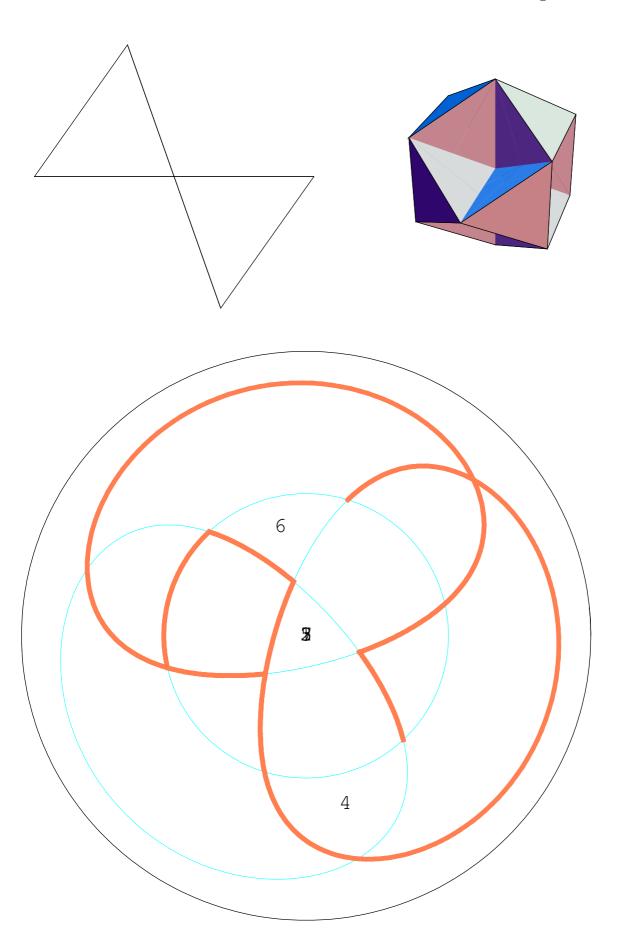
tetrahedron ${3,3,3}$



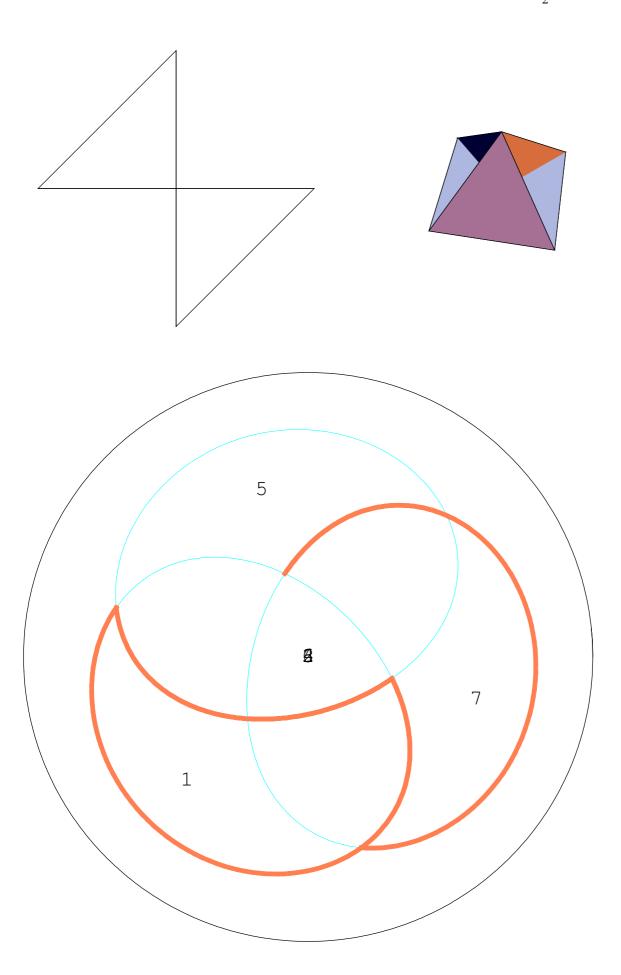
truncated tetrahedron $\{6, 6, 3\}$



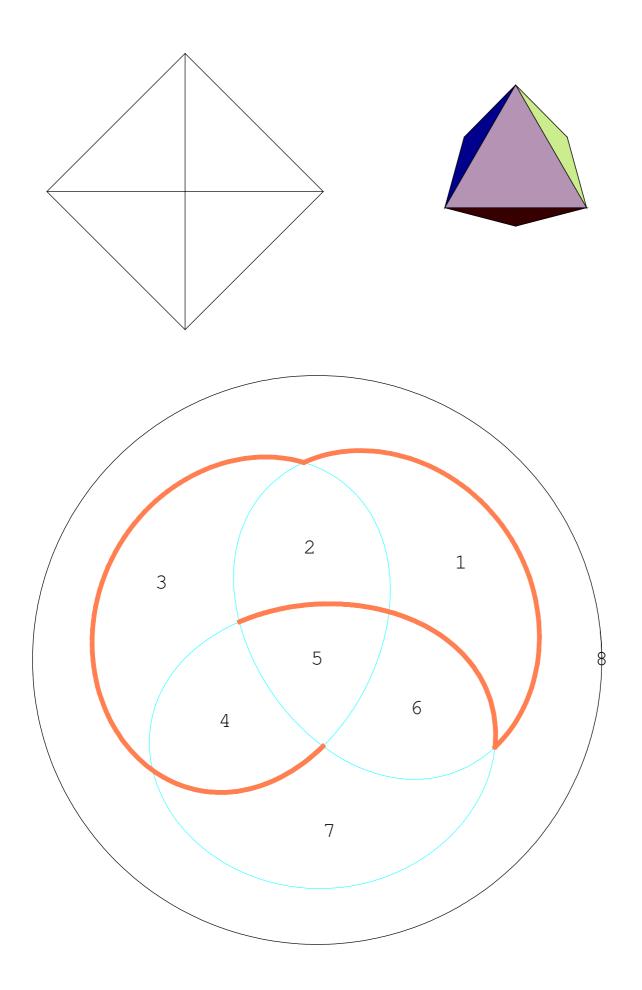
octahemioctahedron $\left\{6,\,\frac{3}{2},\,6,\,3\right\}$



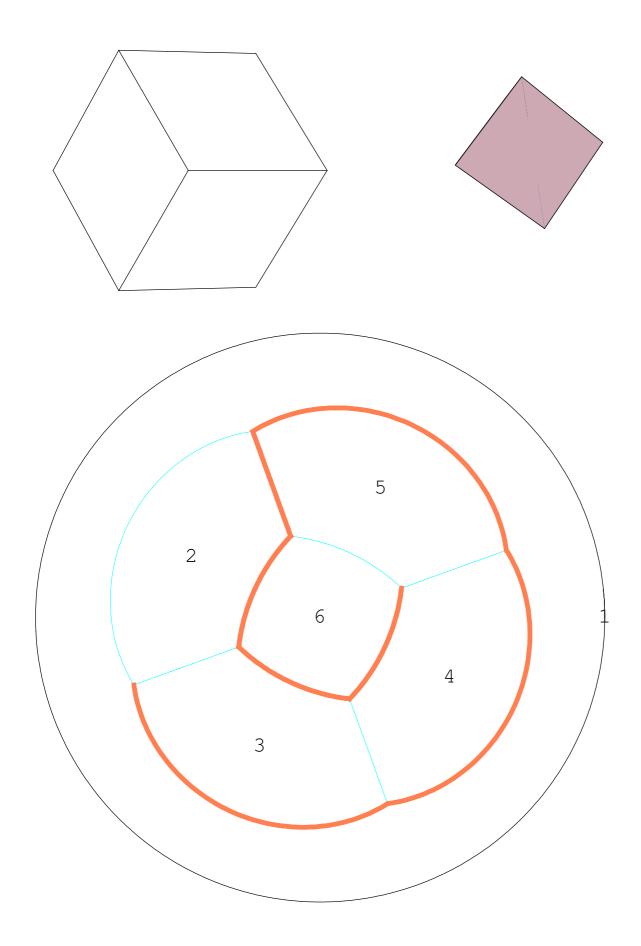
tetrahemihexahedron $\left\{4,\,\frac{3}{2},\,4,\,3\right\}$



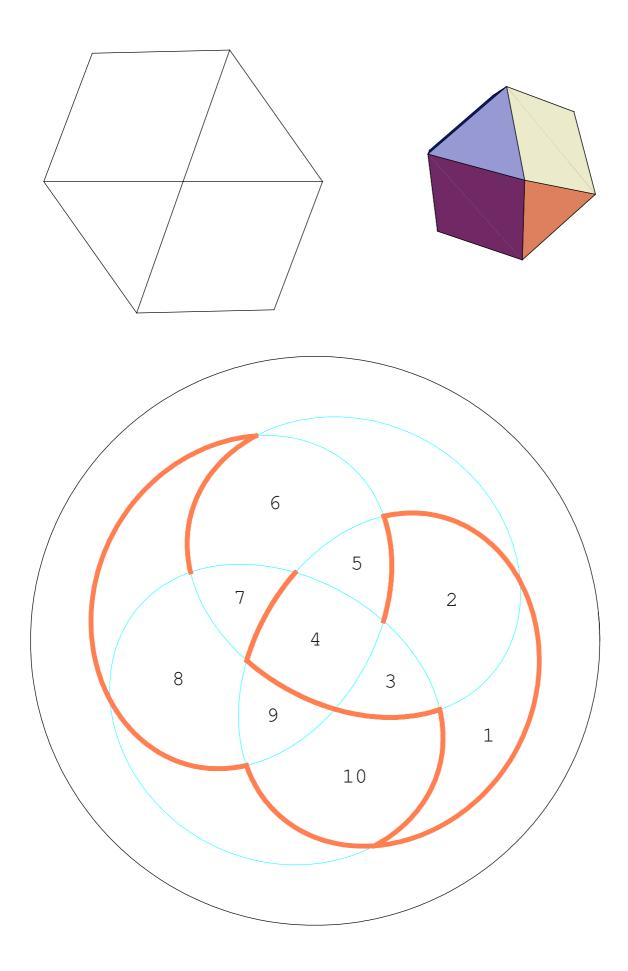
octahedron $\{3, 3, 3, 3\}$



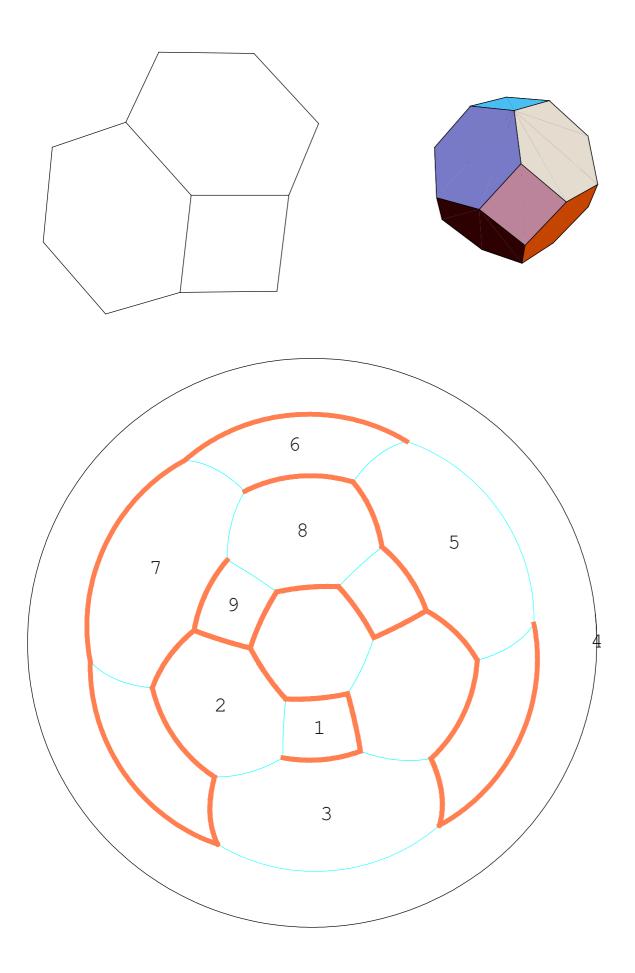
cube {4, 4, 4}



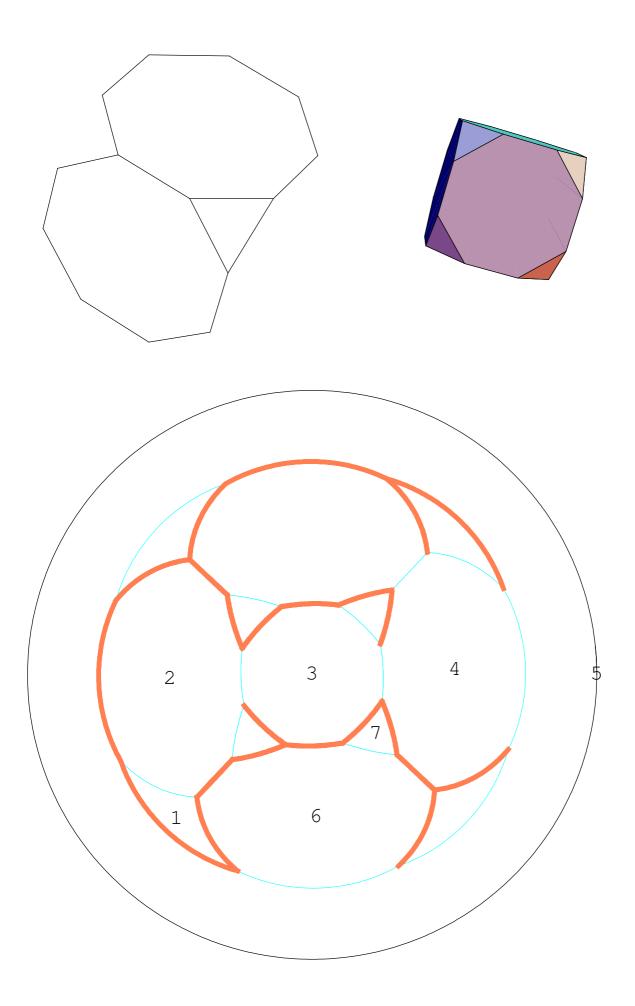
 $\qquad \qquad \text{cuboctahedron} \\ \qquad \{3,4,3,4\}$

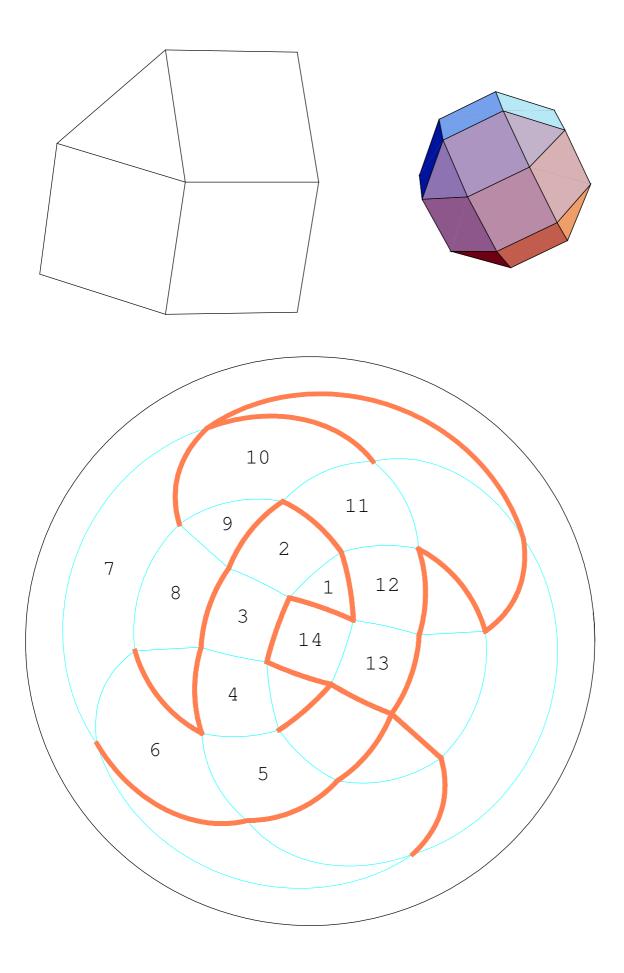


truncated octahedron $\{6, 6, 4\}$

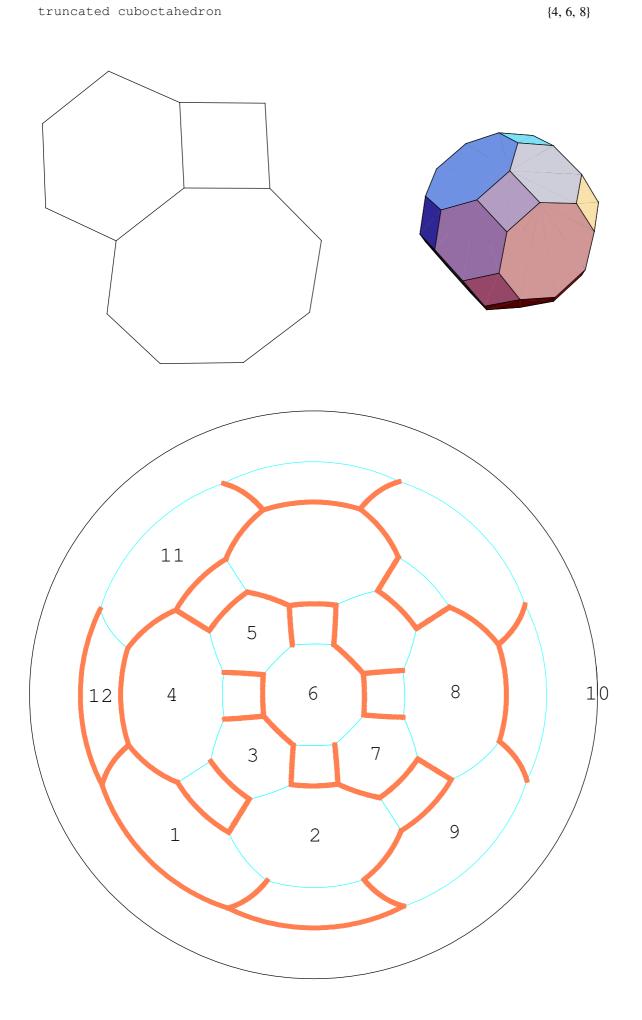


{8, 8, 3} truncated cube

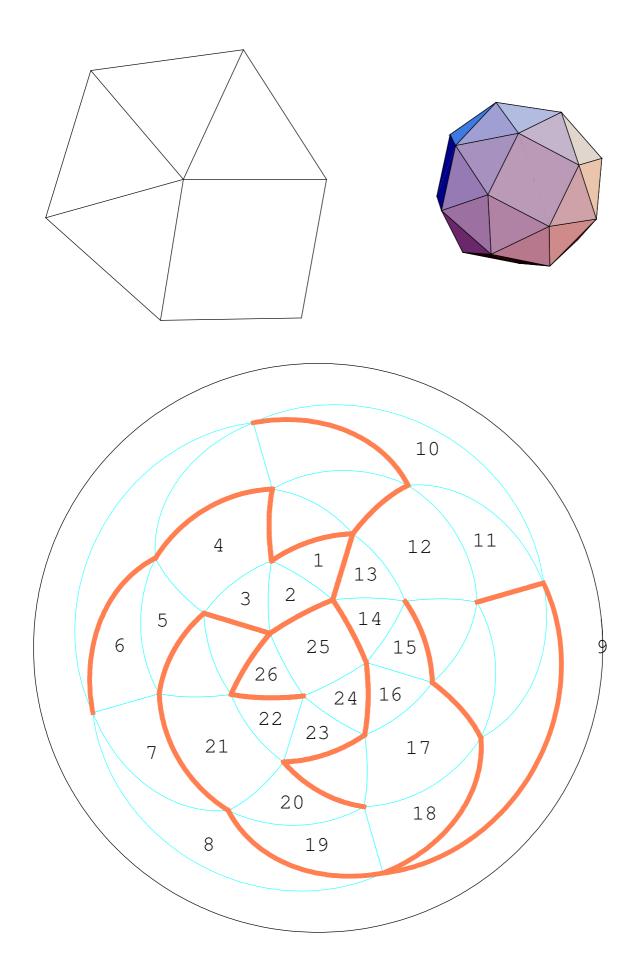




truncated cuboctahedron

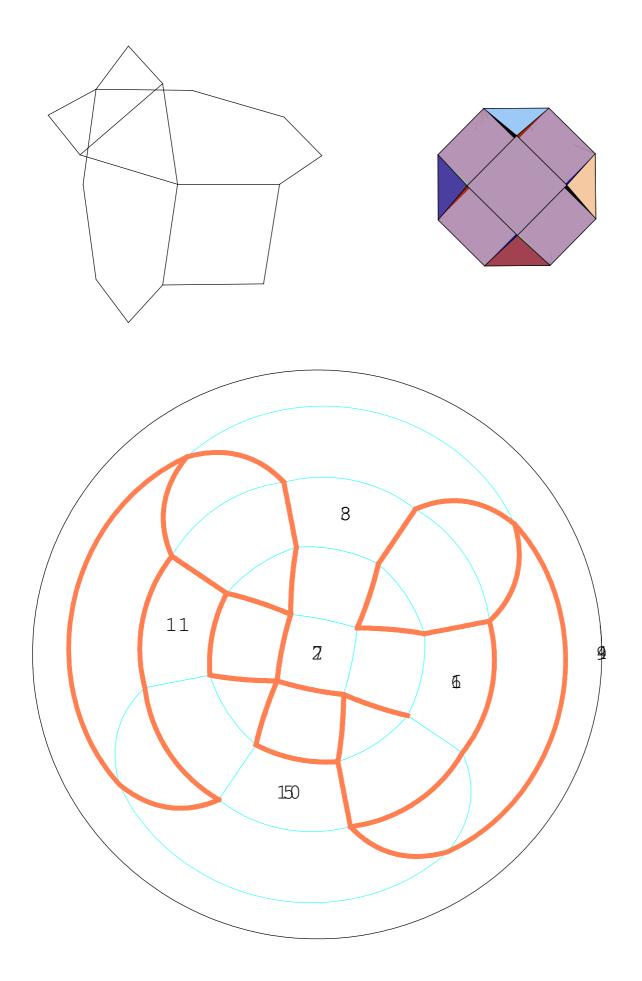


snub cube ${3, 3, 3, 3, 4}$



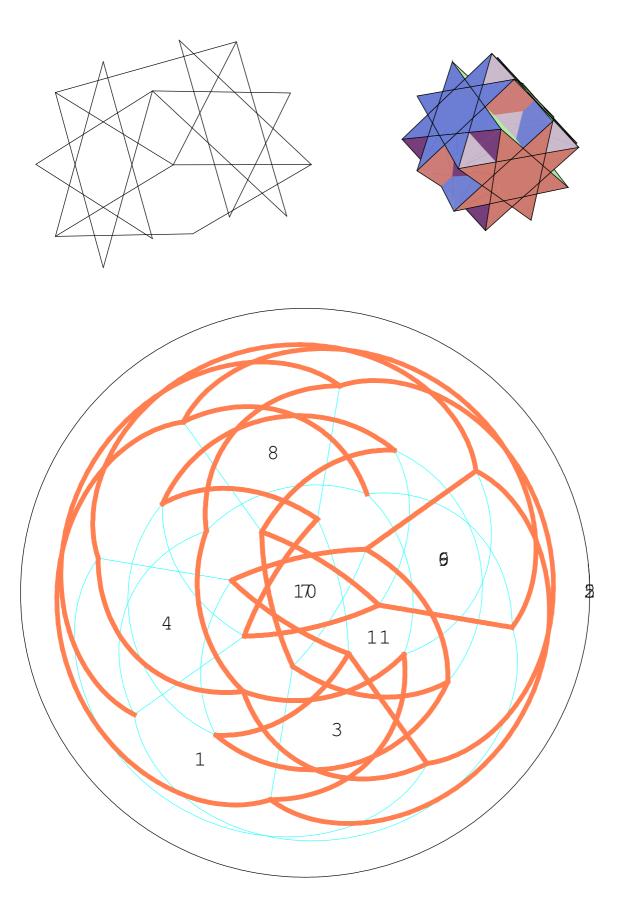
small cubicuboctahedron

$$\left\{8, \frac{3}{2}, 8, 4\right\}$$



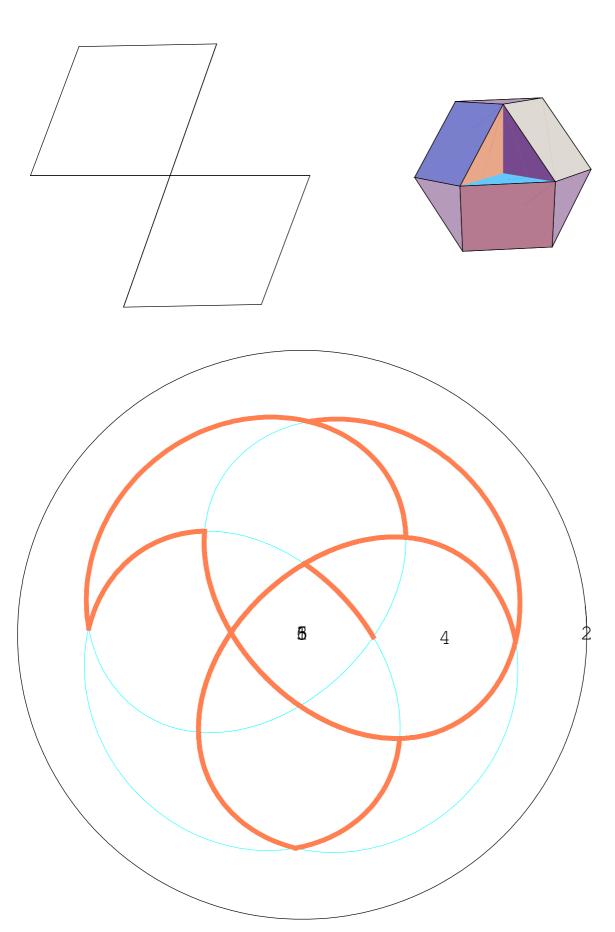
great cubicuboctahedron

$$\left\{\frac{8}{3}, 3, \frac{8}{3}, 4\right\}$$



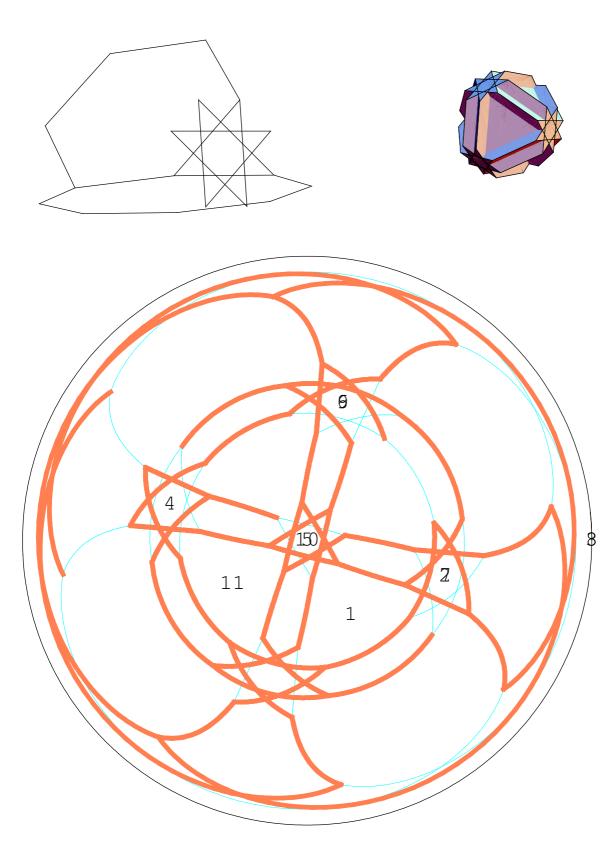
cubohemioctahedron

$$\left\{6, \frac{4}{3}, 6, 4\right\}$$



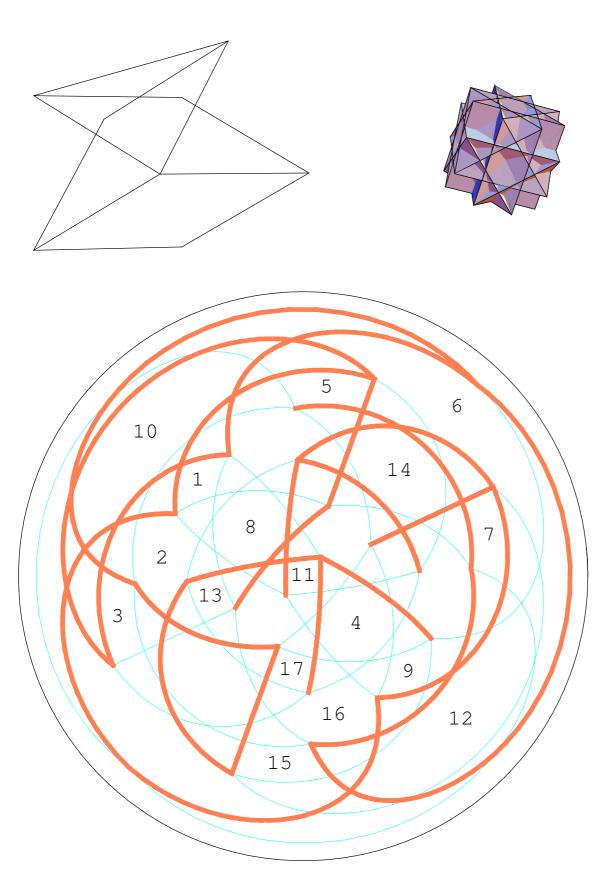
cubitruncated cuboctahedron

 $\left\{\frac{8}{3}, 6, 8\right\}$



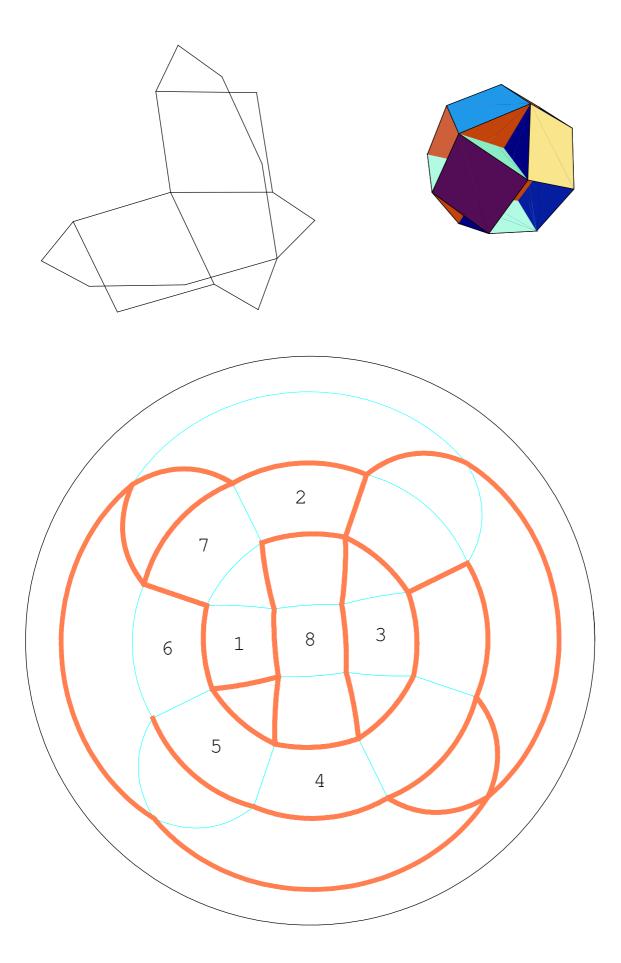
great rhombicuboctahedron

 $\left\{4, \frac{3}{2}, 4, 4\right\}$



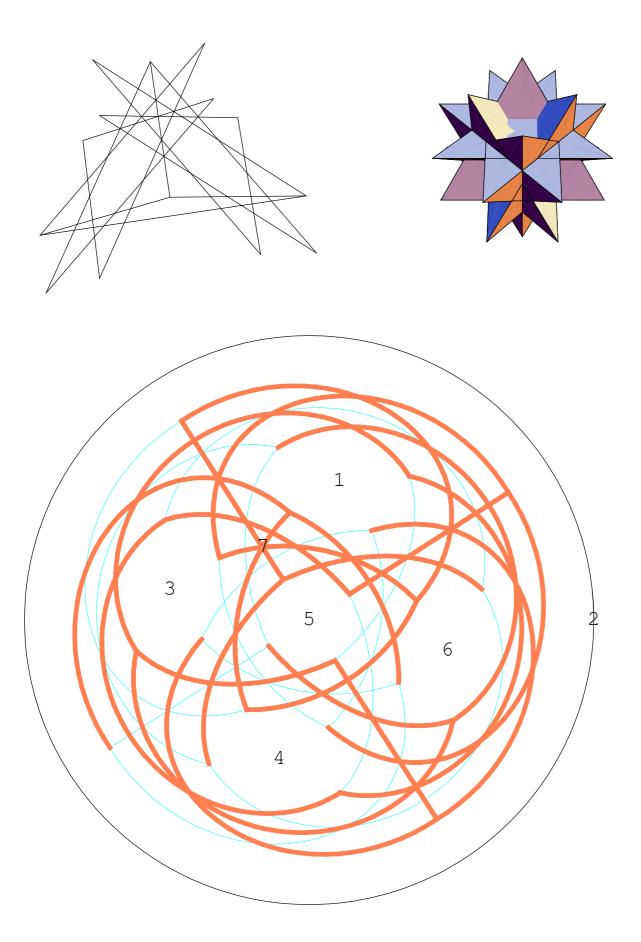
small rhombihexahedron

$$\left\{8, 4, \frac{8}{7}, \frac{4}{3}\right\}$$



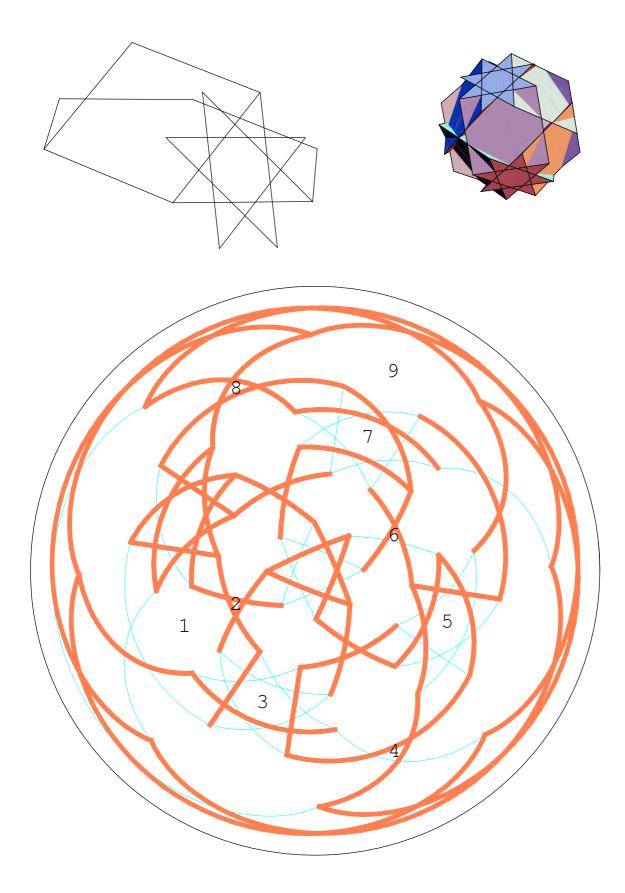
stellated truncated hexahedron

$$\left\{\frac{8}{3}, \frac{8}{3}, 3\right\}$$



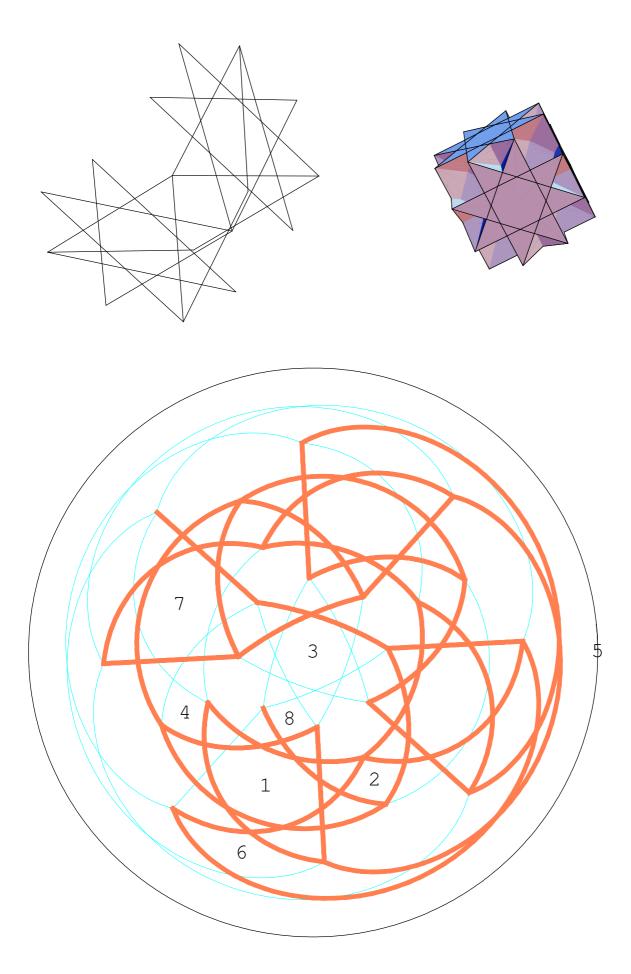
great truncated cuboctahedron

 $\left\{\frac{8}{3}, 4, 6\right\}$

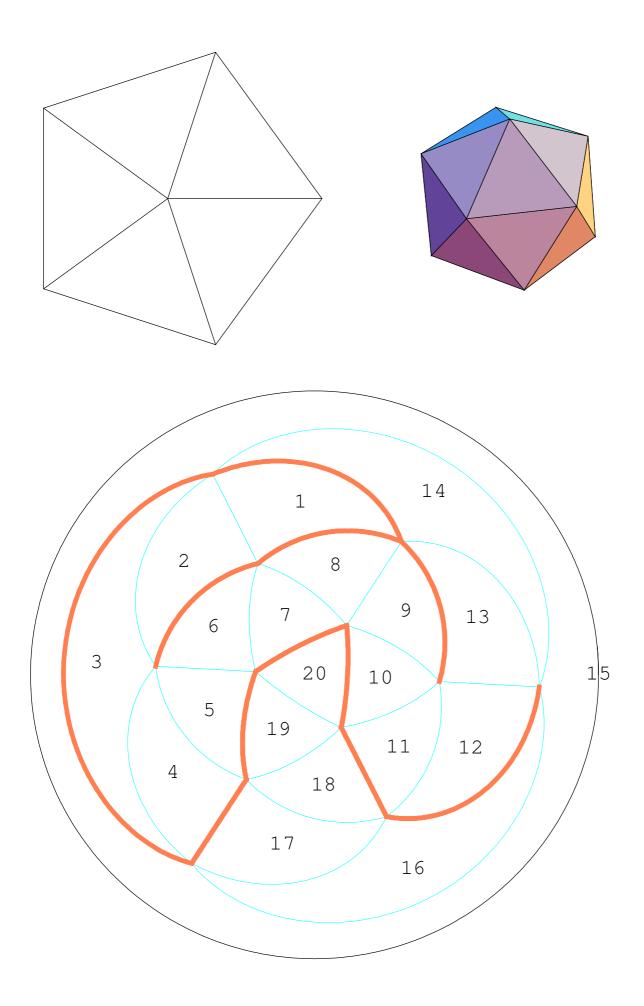


great rhombihexahedron

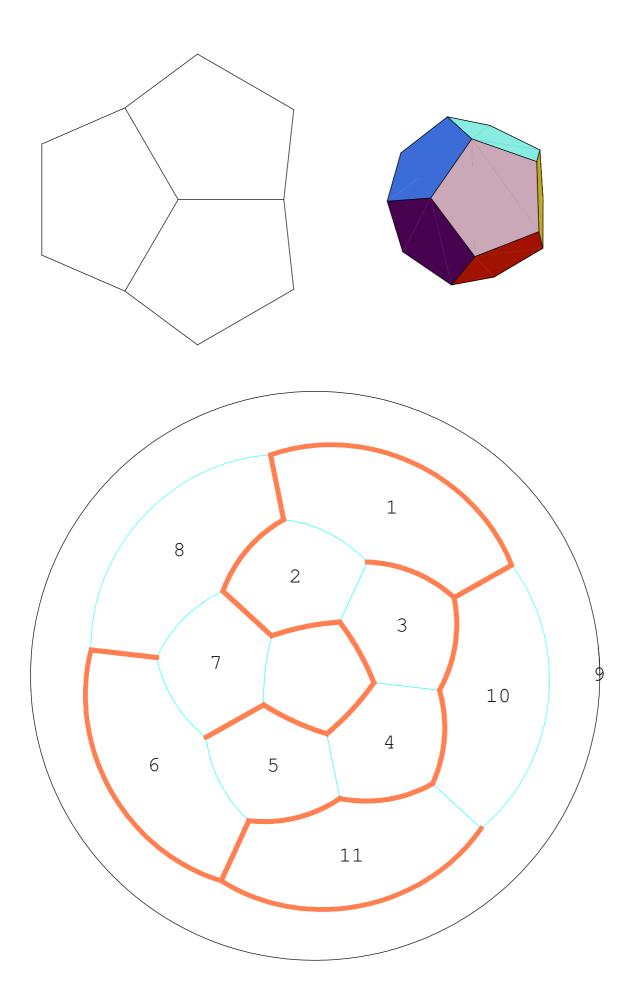
$$\left\{4, \frac{8}{3}, \frac{4}{3}, \frac{8}{5}\right\}$$



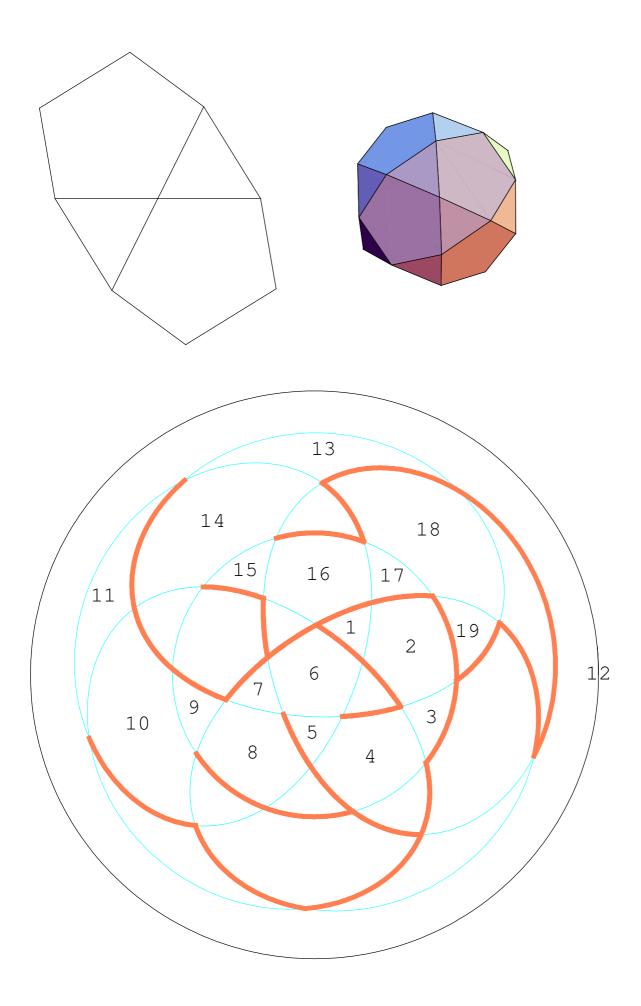
icosahedron ${3, 3, 3, 3, 3}$



dodecahedron {5, 5, 5}

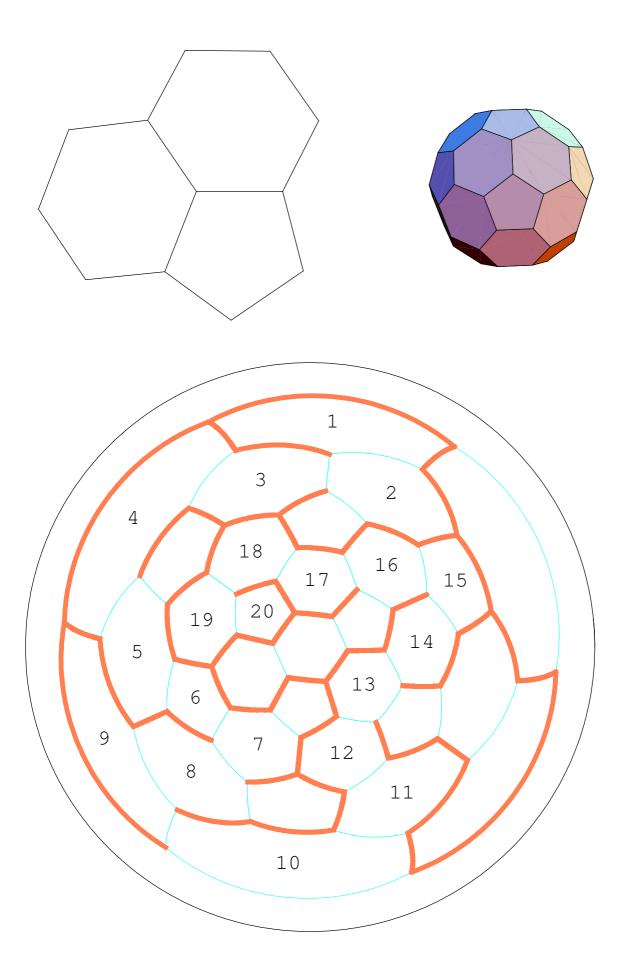


icosidodecahedron $\{3, 5, 3, 5\}$

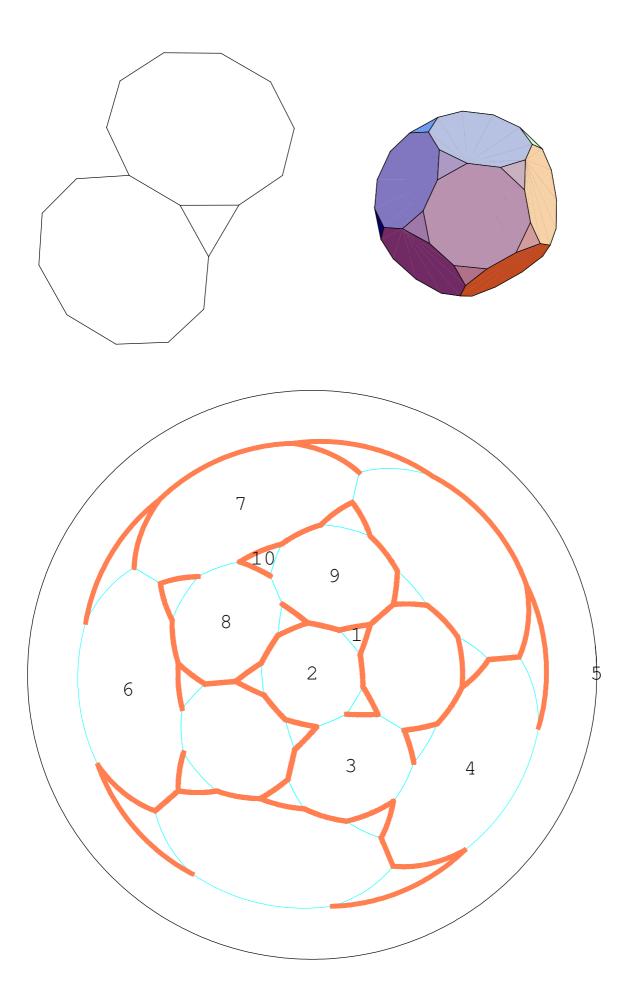


truncated icosahedron

 $\{6, 6, 5\}$

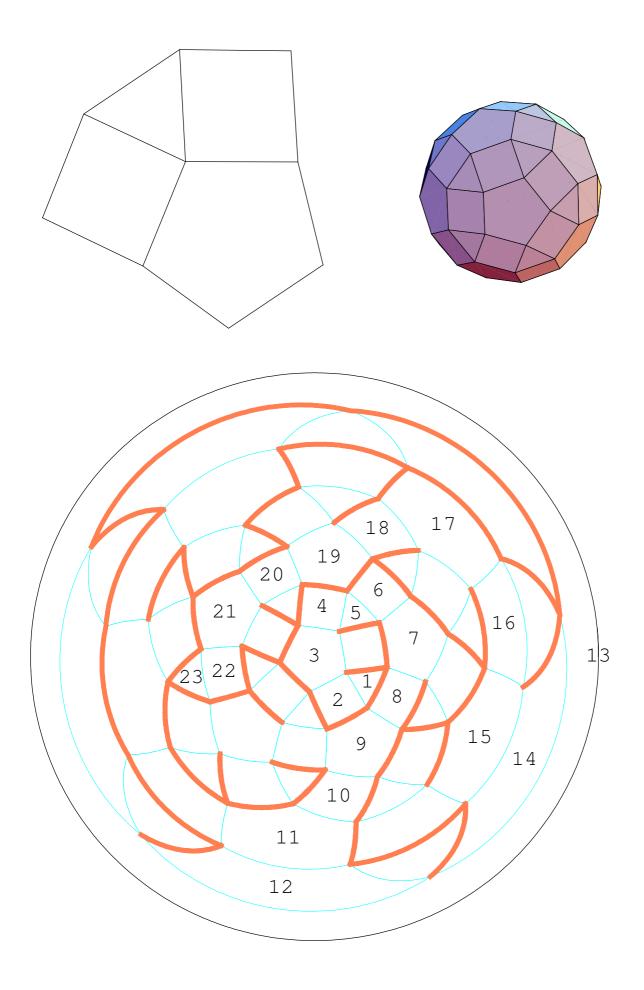


truncated dodecahedron {10, 10, 3}



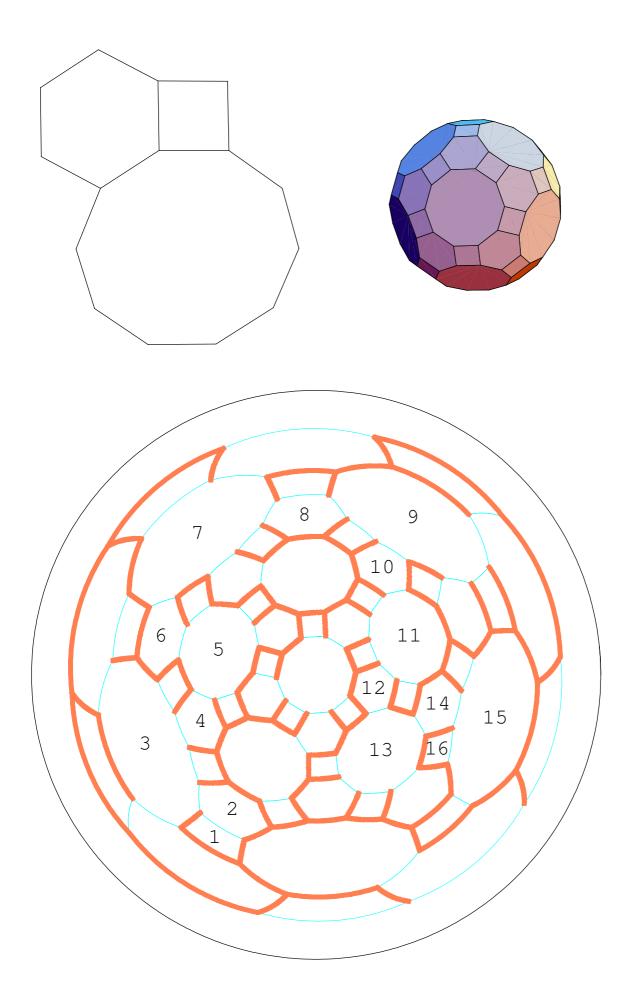
rhombicosidodecahedron

{4, 3, 4, 5}

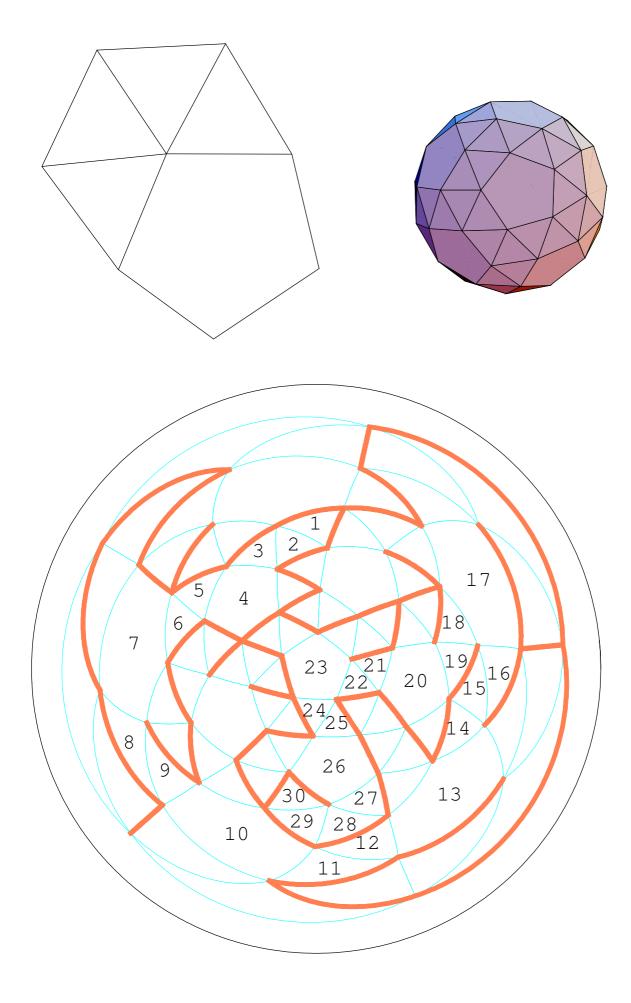


truncated icosidodecahedron

{4, 6, 10}

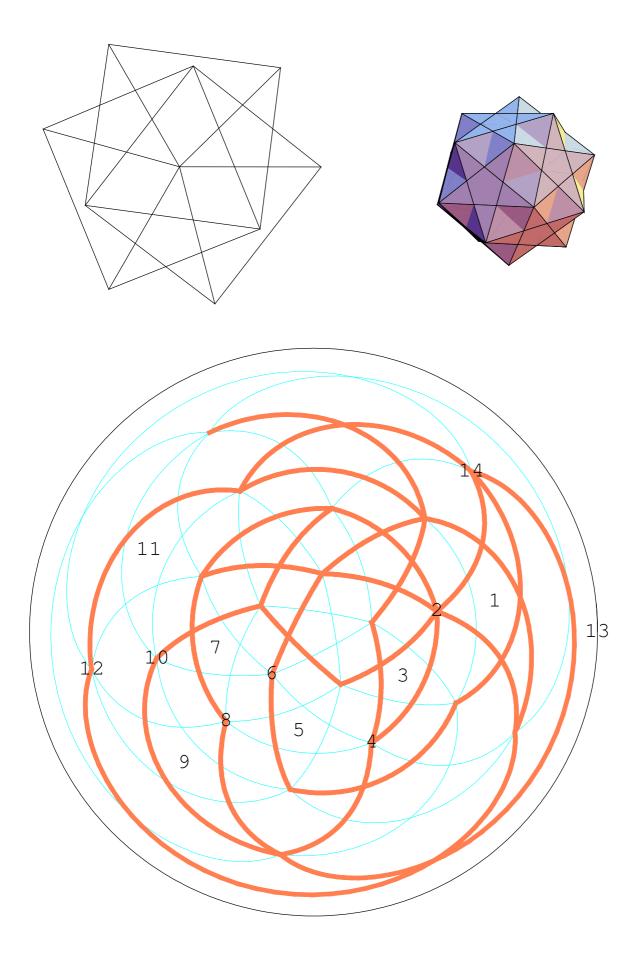


snub dodecahedron $\{3, 3, 3, 3, 5\}$



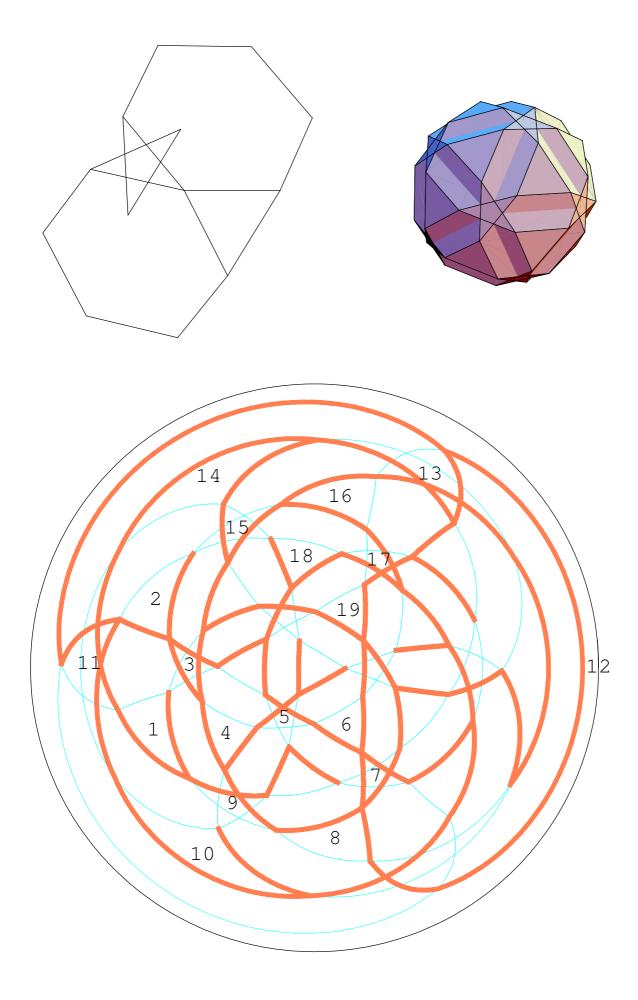
small ditrigonal icosidodecahedron

$$\left\{\frac{5}{2}, 3, \frac{5}{2}, 3, \frac{5}{2}, 3\right\}$$



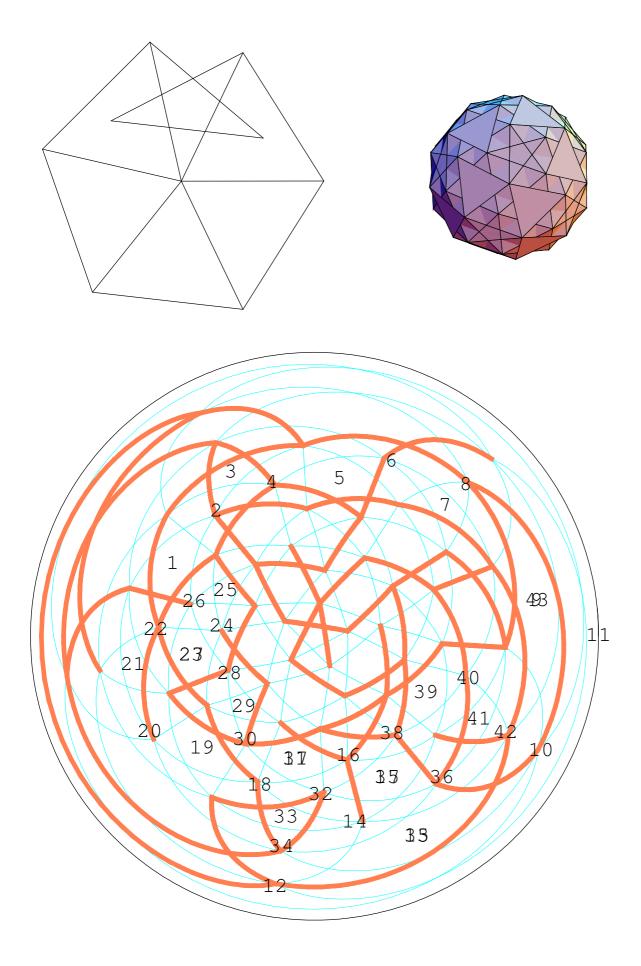
small icosicosidodecahedron

$$\left\{6, \frac{5}{2}, 6, 3\right\}$$



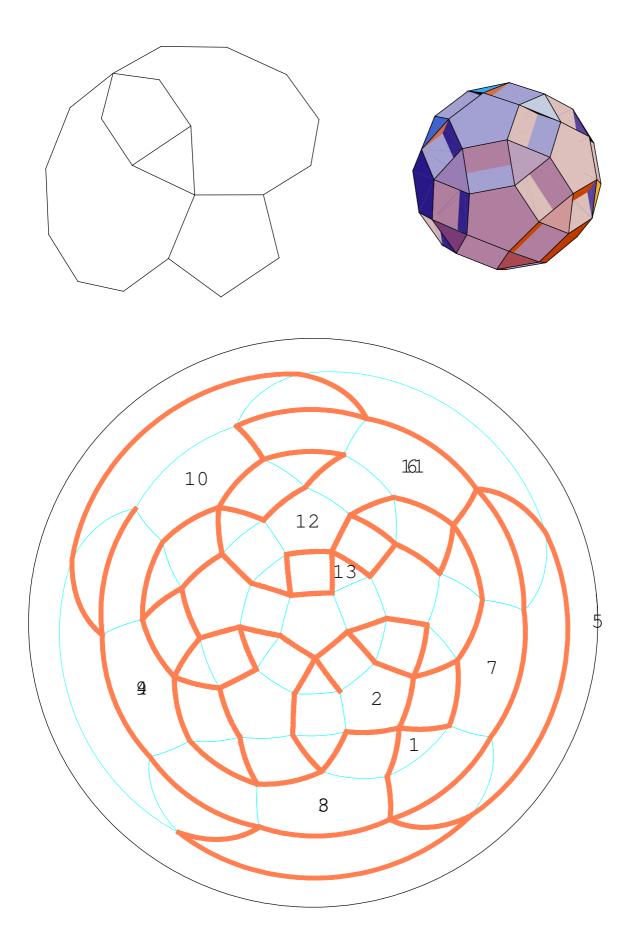
small snub icosicosidodecahedron

$${3, \frac{5}{2}, 3, 3, 3, 3}$$



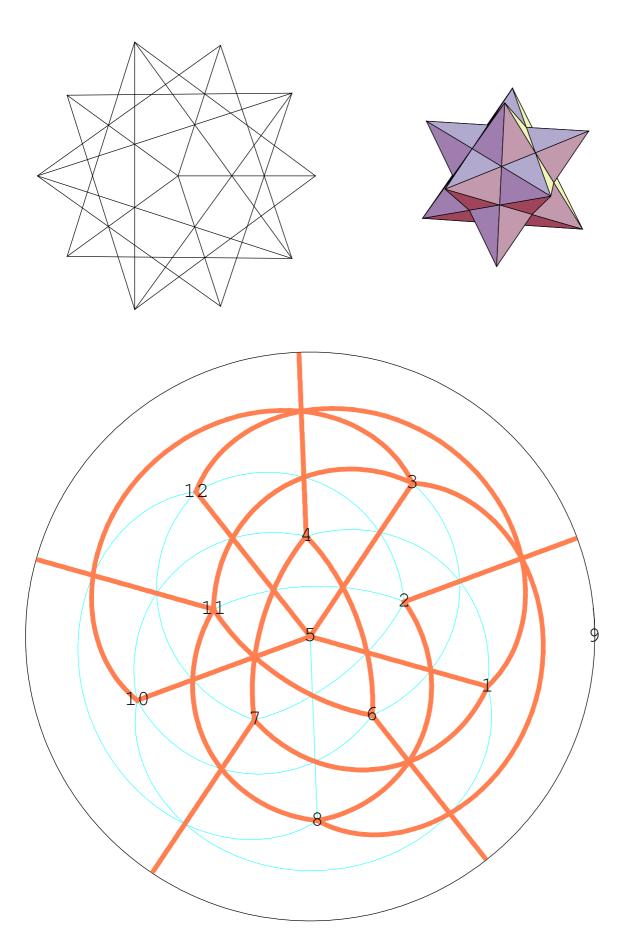
small dodecicosidodecahedron

$$\left\{10, \frac{3}{2}, 10, 5\right\}$$



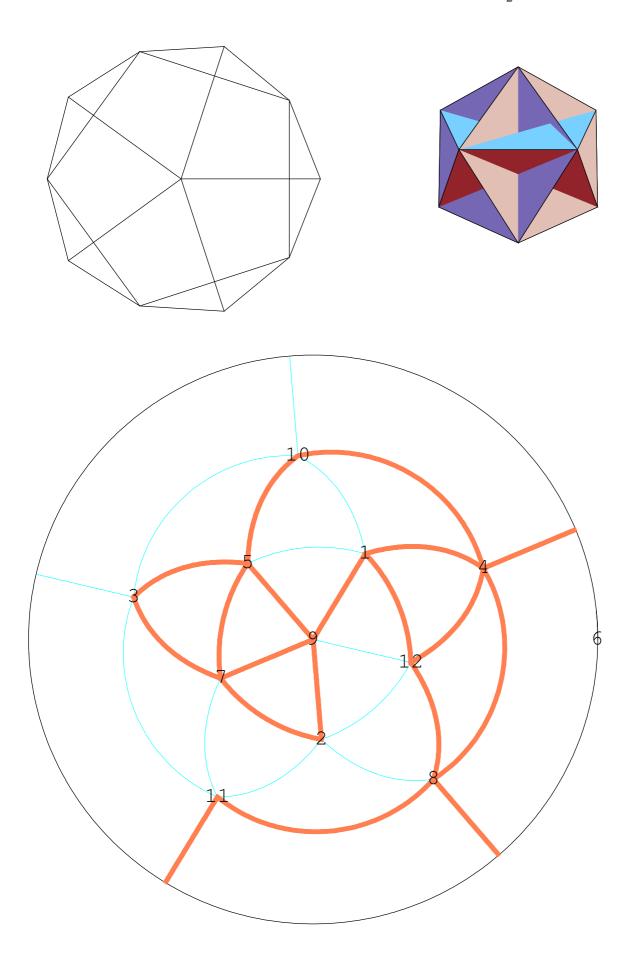
small stellated dodecahedron

$$\left\{\frac{5}{2}, \frac{5}{2}, \frac{5}{2}, \frac{5}{2}, \frac{5}{2}\right\}$$



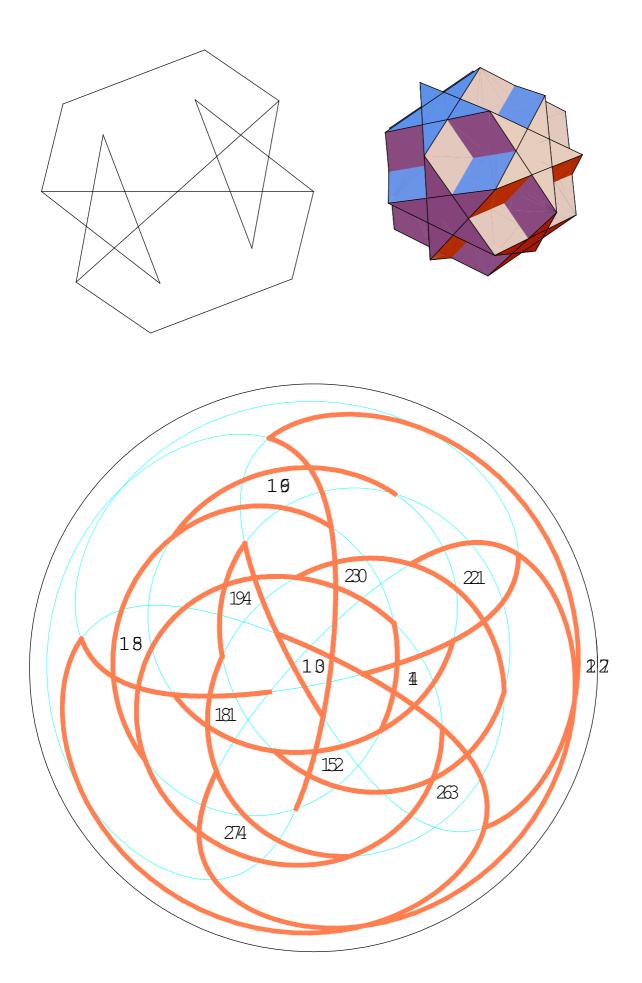
great dodecahedron

$$\frac{1}{2}$$
 {5, 5, 5, 5, 5}



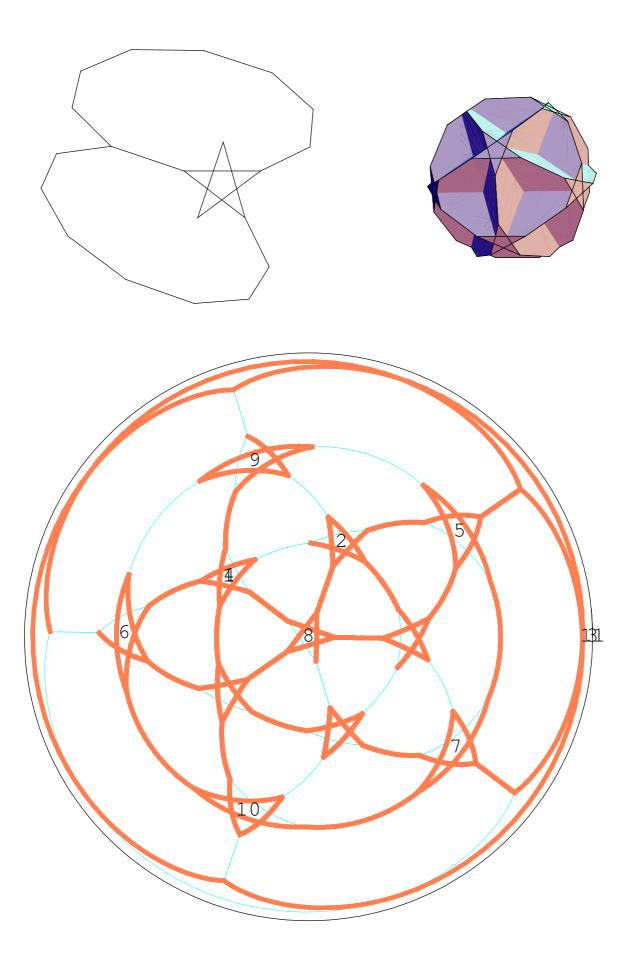
dodecadodecahedron

$$\left\{\frac{5}{2}, 5, \frac{5}{2}, 5\right\}$$



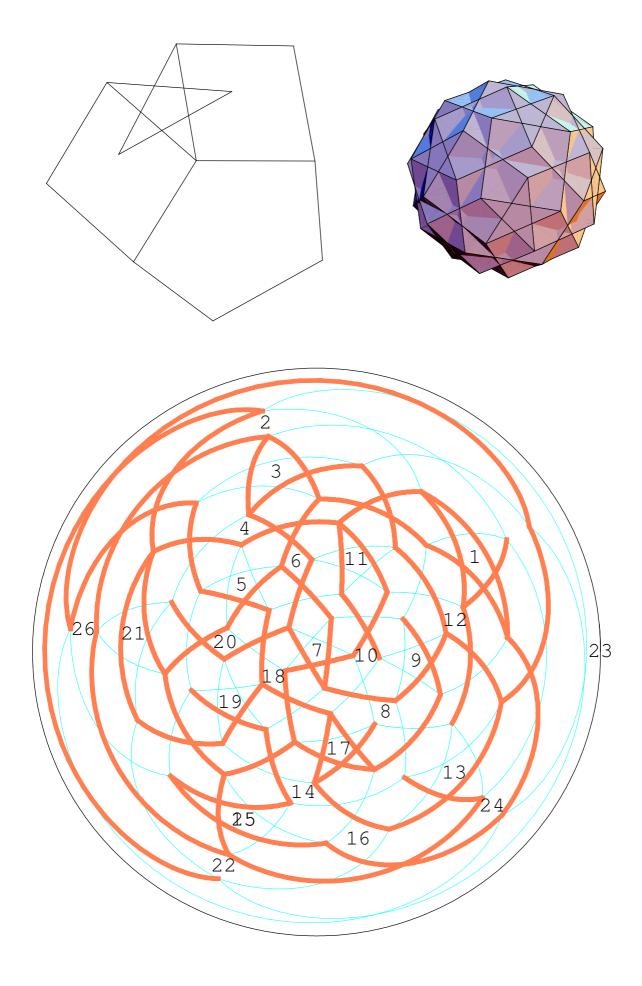
truncated great dodecahedron

$$\left\{10, 10, \frac{5}{2}\right\}$$



rhombidodecadodecahedron

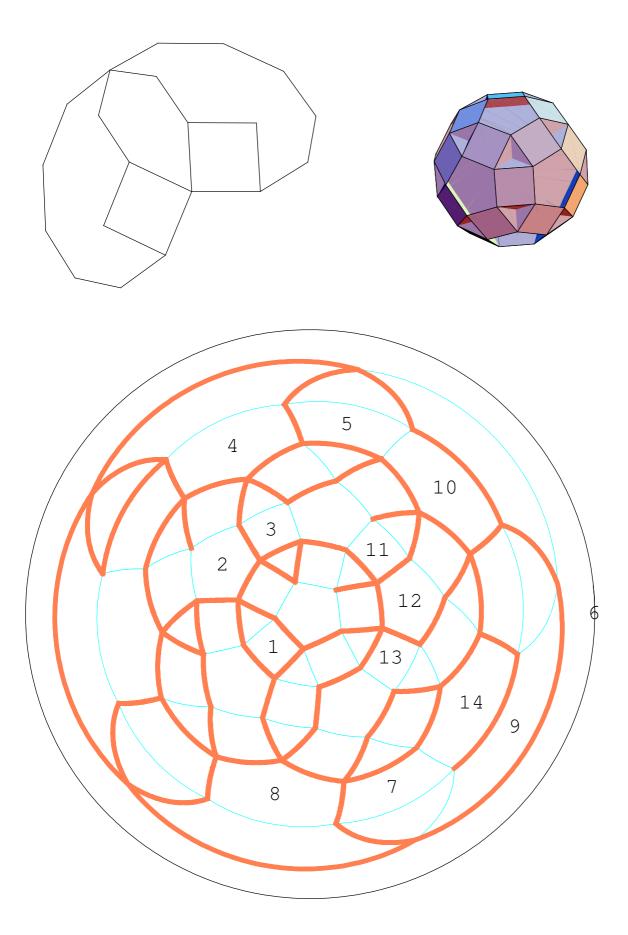
$$\left\{4, \frac{5}{2}, 4, 5\right\}$$



39.

small rhombidodecahedron

$$\{10, 4, \frac{10}{9}, \frac{4}{3}\}$$



snub dodecadodecahedron

 ${3, 3, \frac{5}{2}, 3, 5}$

