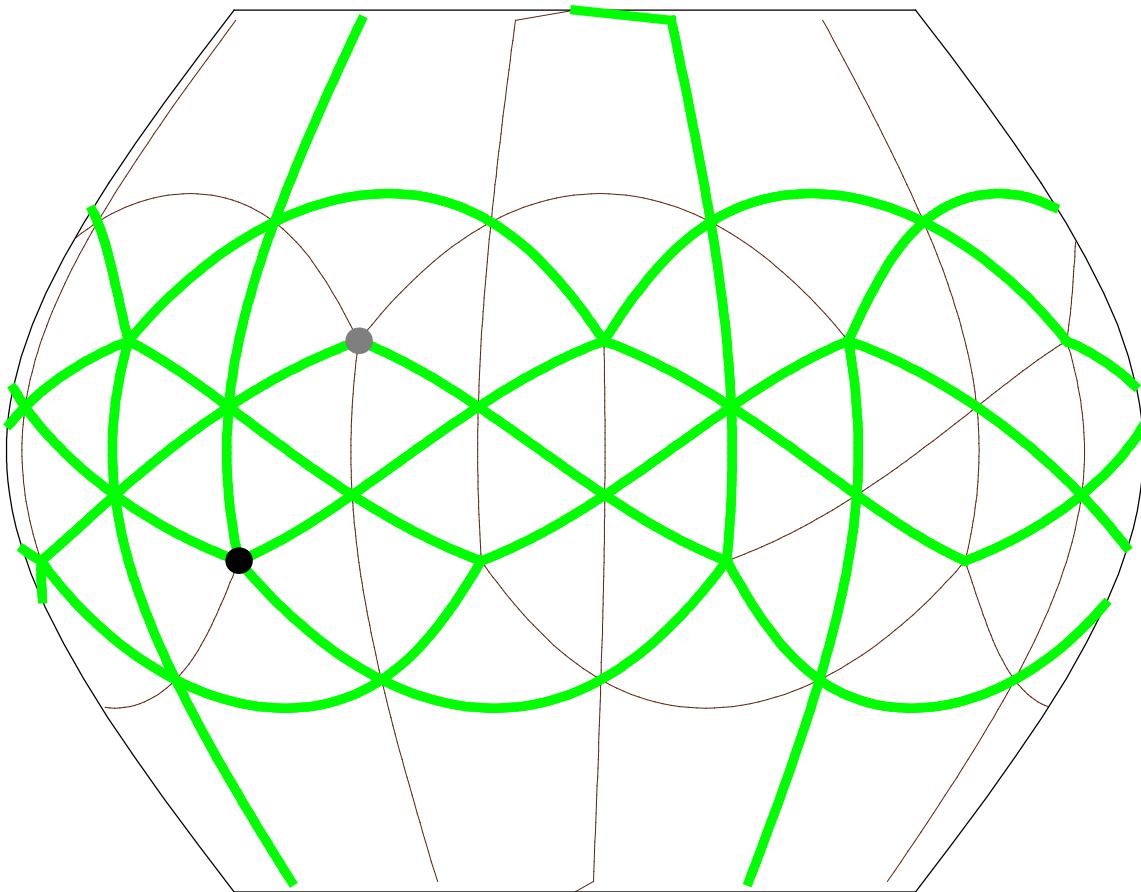
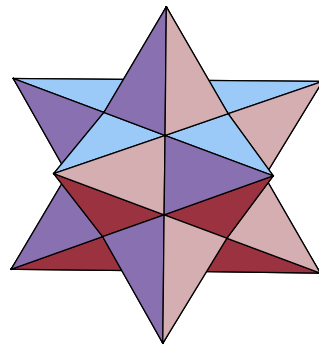
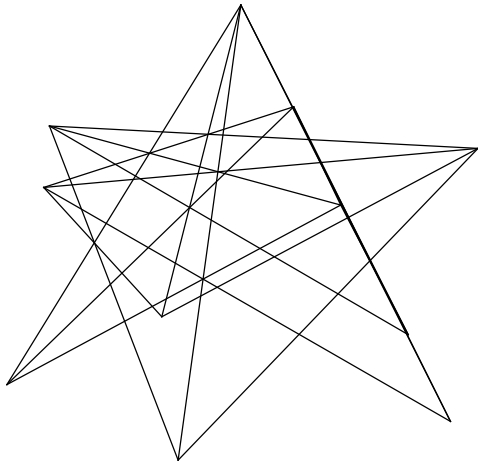


Izidor Hafner

Mazes for Superintelligent

Ginzburg projection

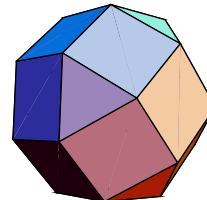
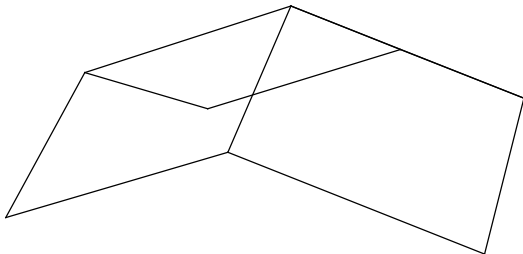


Introduction

Let us take an example. We are given a uniform polyhedron.

rhombicuboctahedron

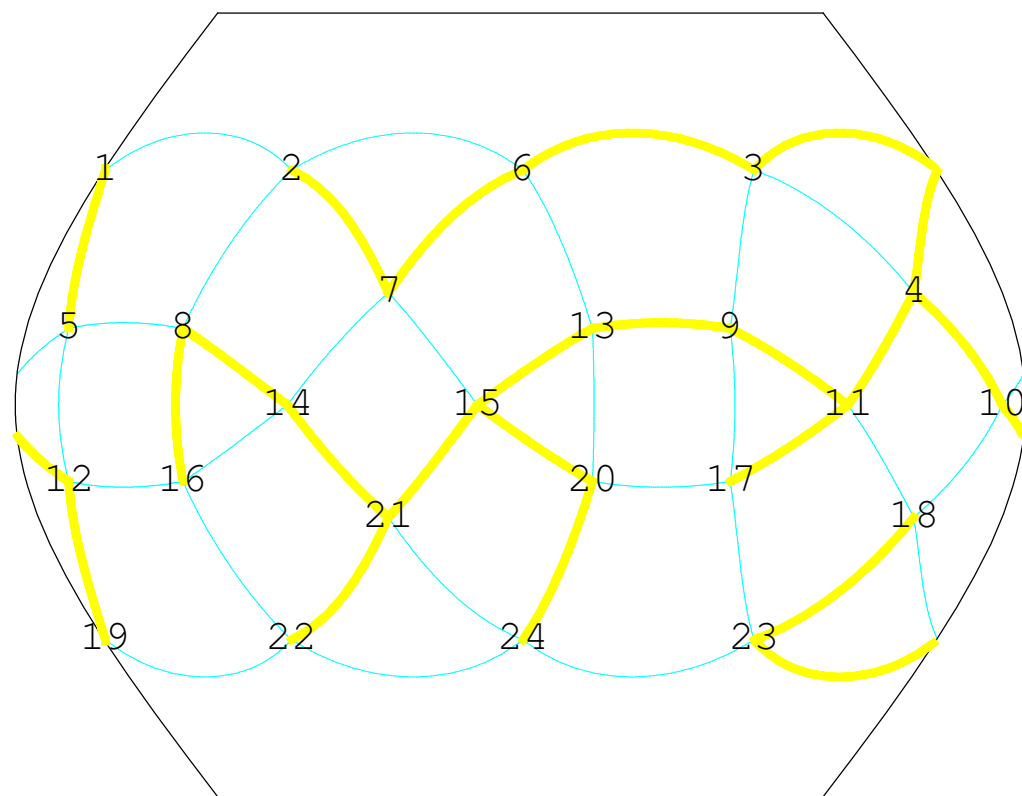
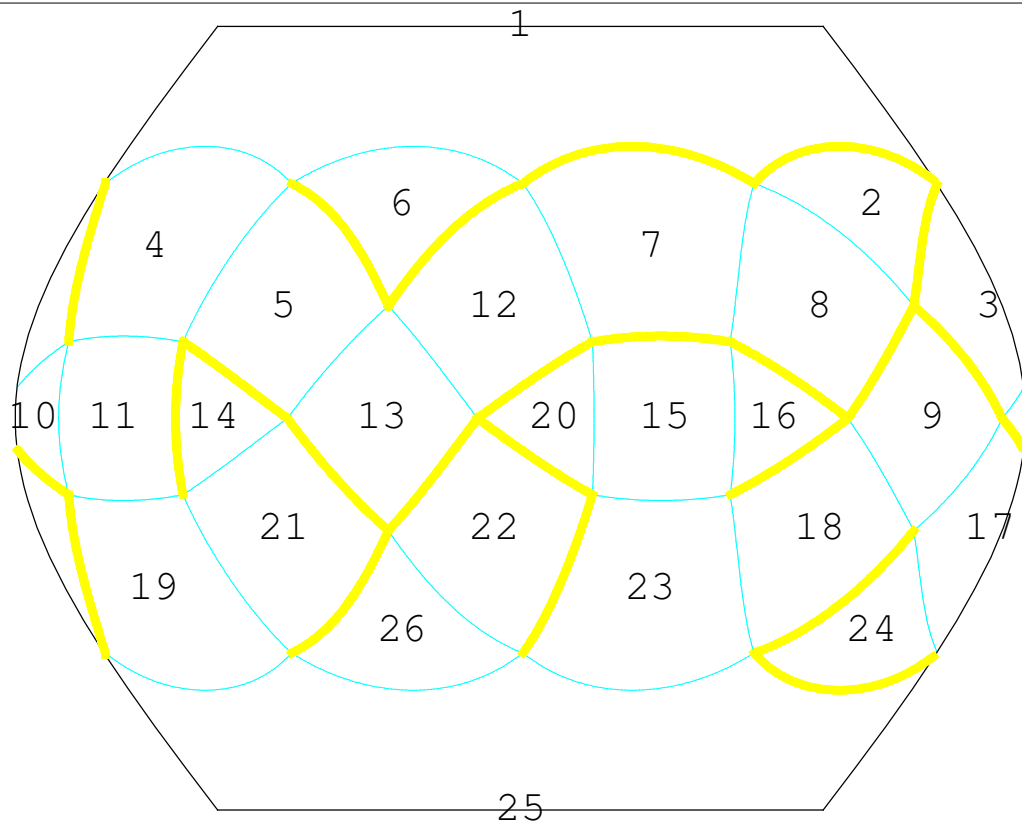
{4, 3, 4, 4}



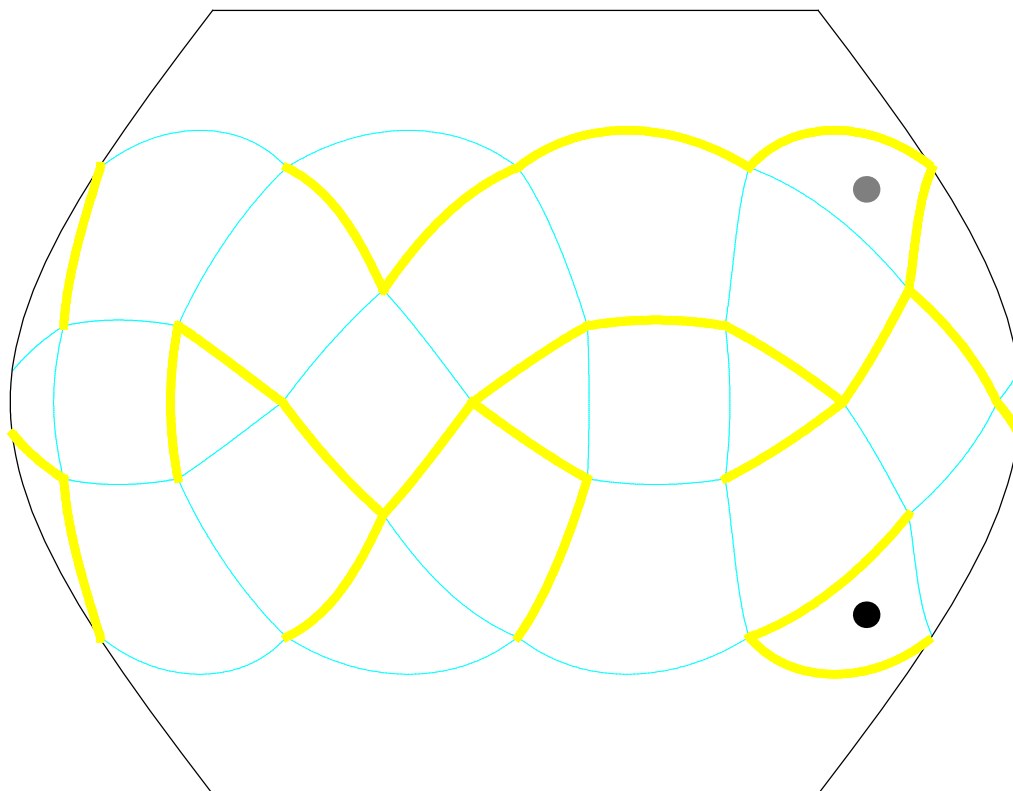
In Mathematica the polyhedron is given by a list of faces and with a list of coordinates of vertices [Roman E. Maeder, The Mathematica Programmer II, Academic Press 1996]. The list of faces consists of a list of lists, where a face is represented by a list of vertices, which is given by a matrix. Let us show the first five faces:

$$\begin{pmatrix} \{1, 2, 6, 3\} \\ \{1, 3, 4\} \\ \{1, 4, 10, 5\} \\ \{1, 5, 8, 2\} \\ \{2, 8, 14, 7\} \end{pmatrix}$$

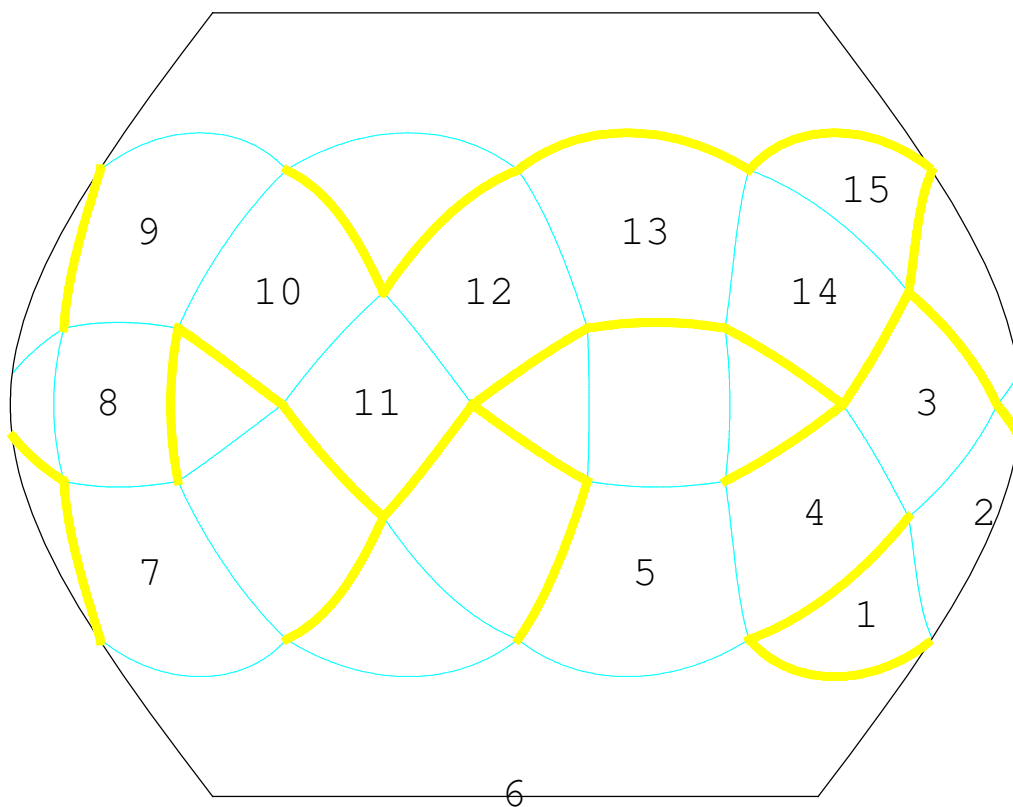
The next two figures represent faces and vertices. The polyhedron is projected onto a sphere and the sphere is projected by a cartographic projection.



The problem is to find the path from the black dot to gray dot, where thick lines represent walls of a maze.



The solution is given by a list of faces passed from the black to gray dot.

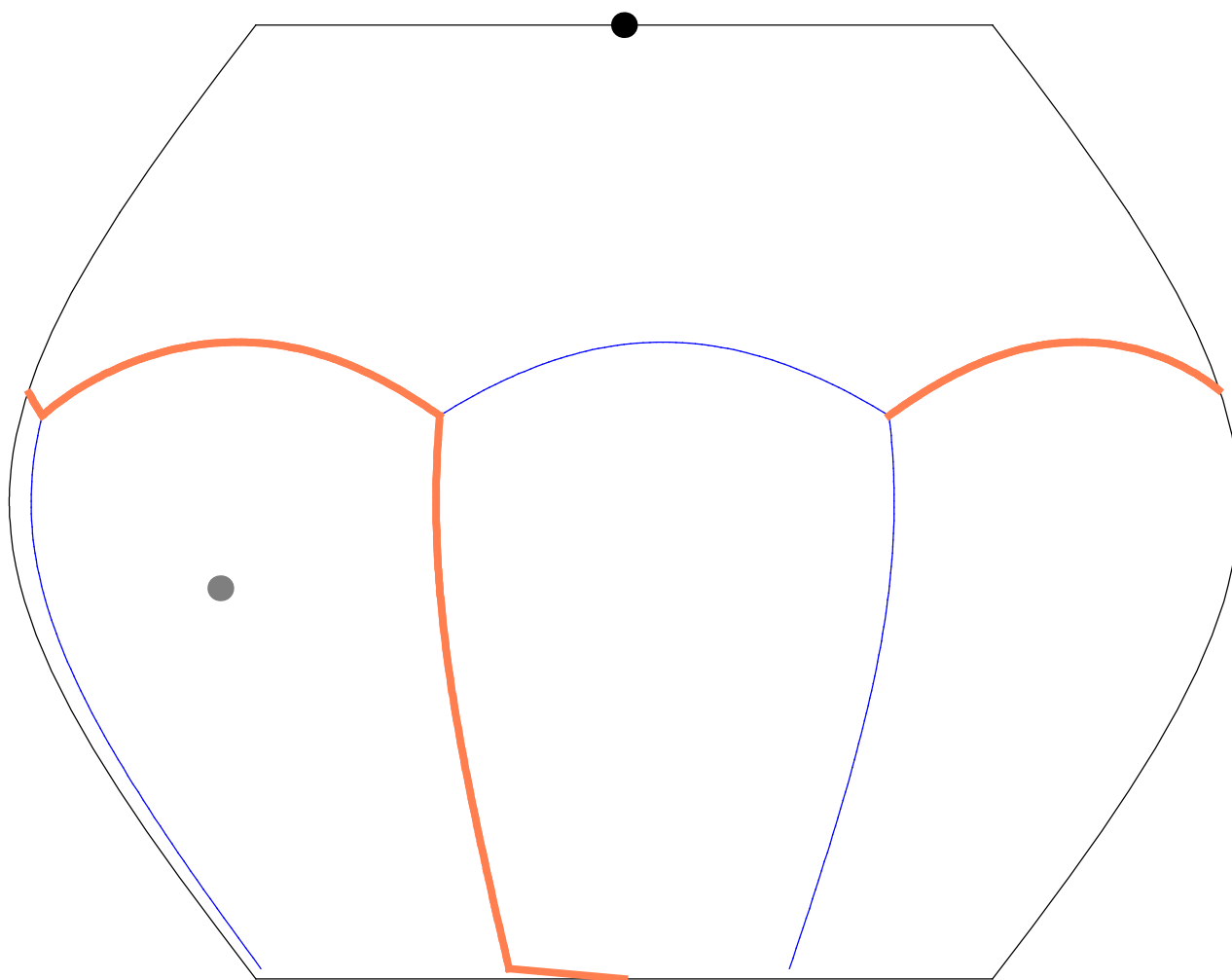
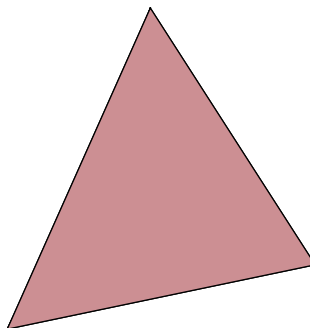
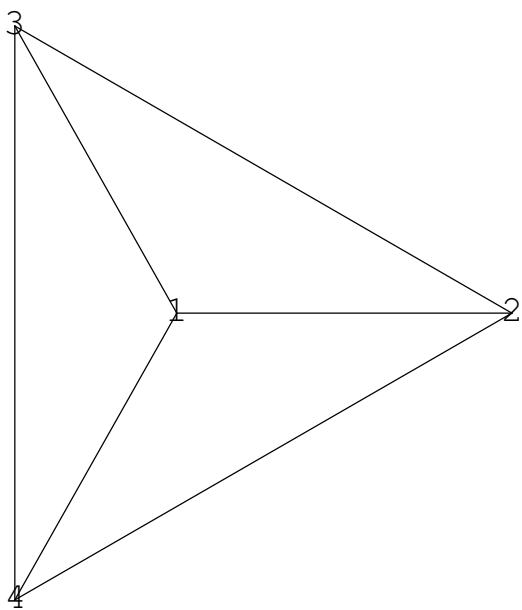


Problems

1.

tetrahedron

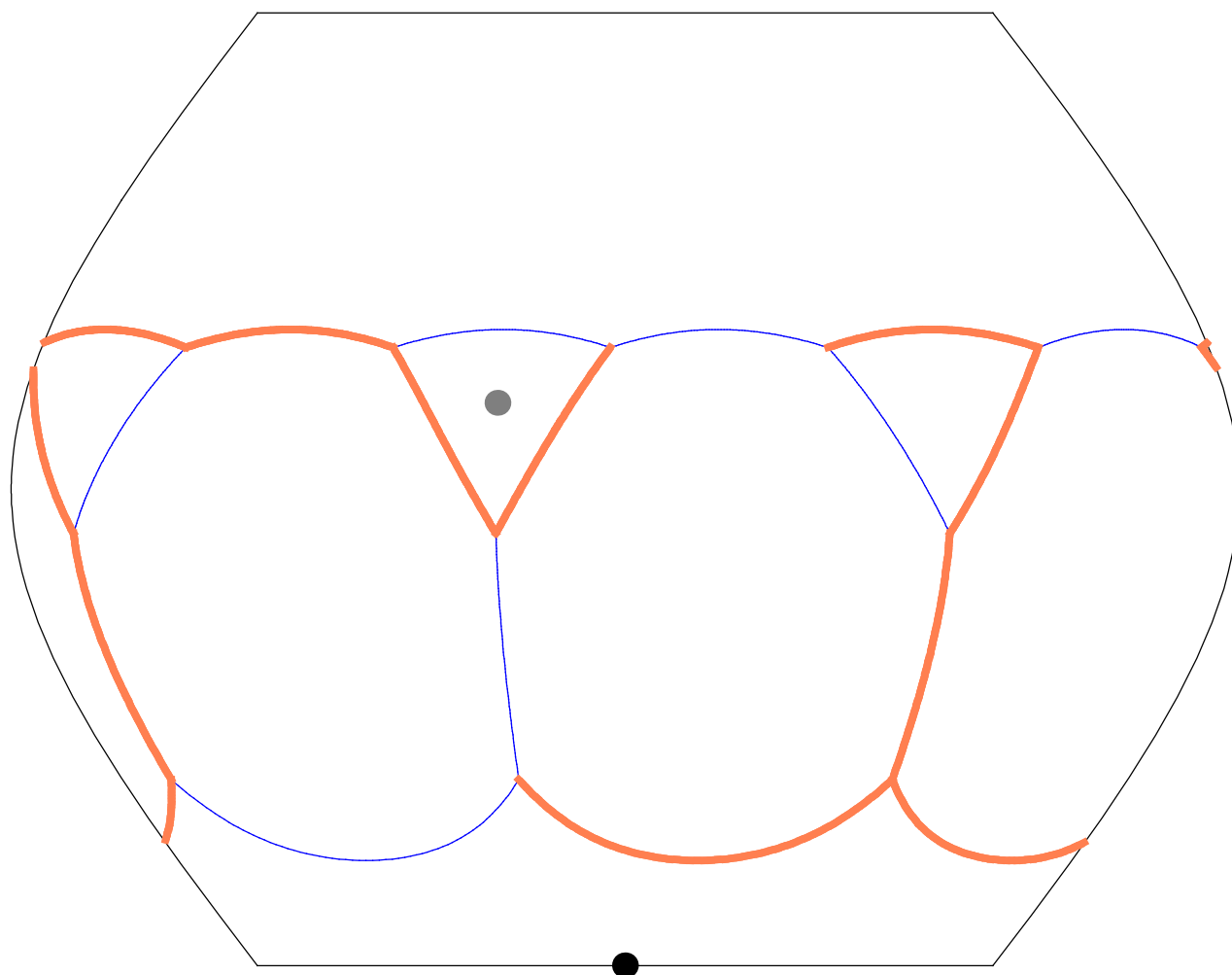
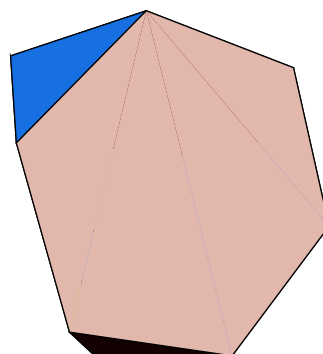
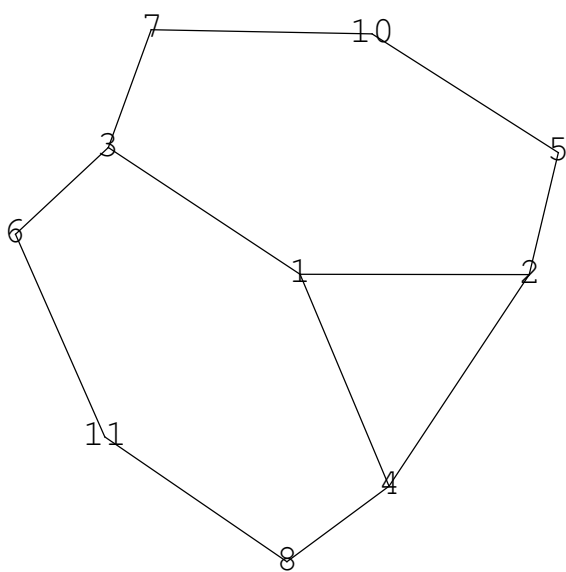
{3, 3, 3}



2.

truncated tetrahedron

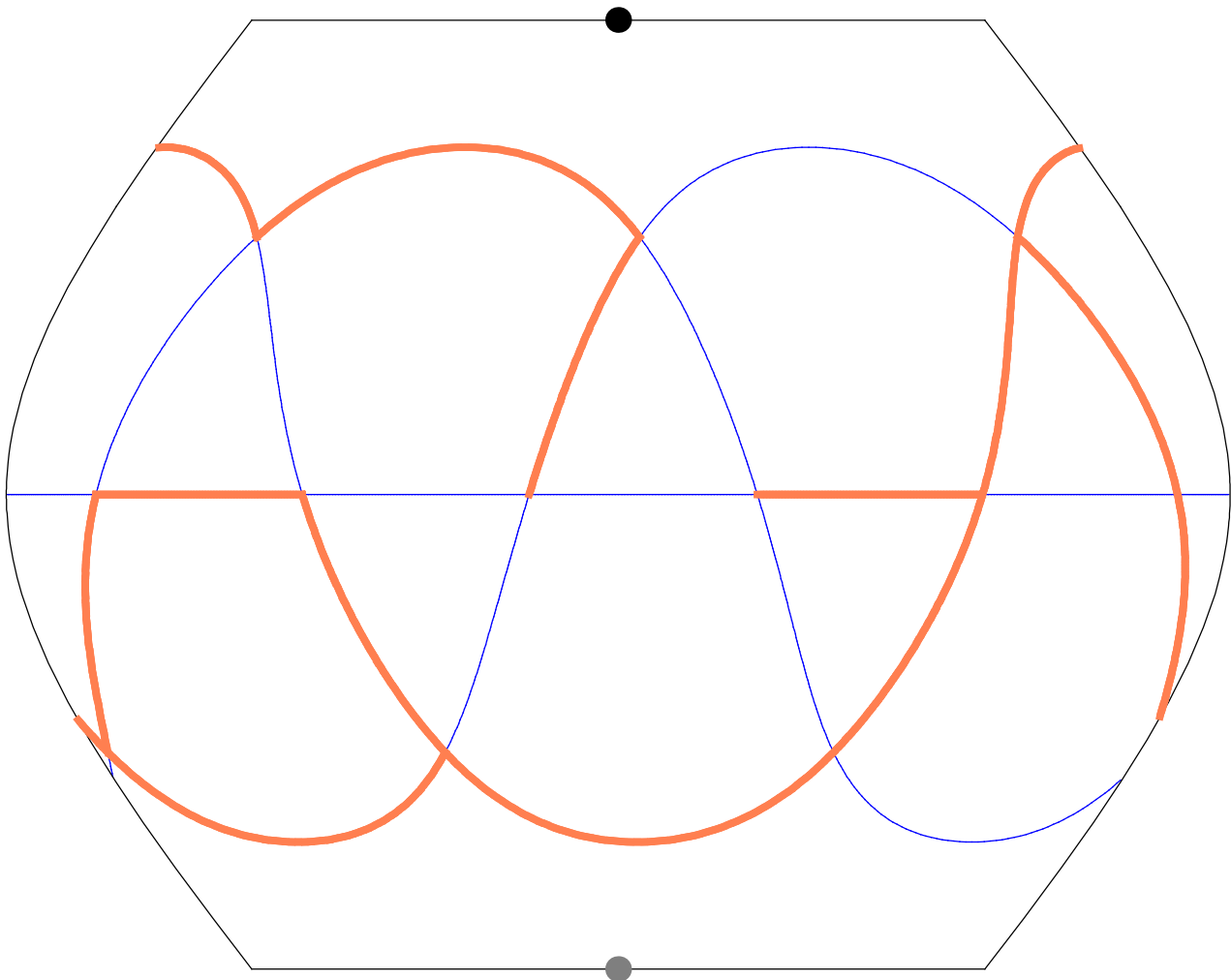
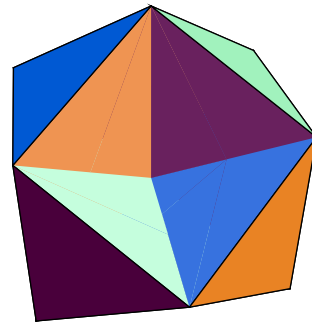
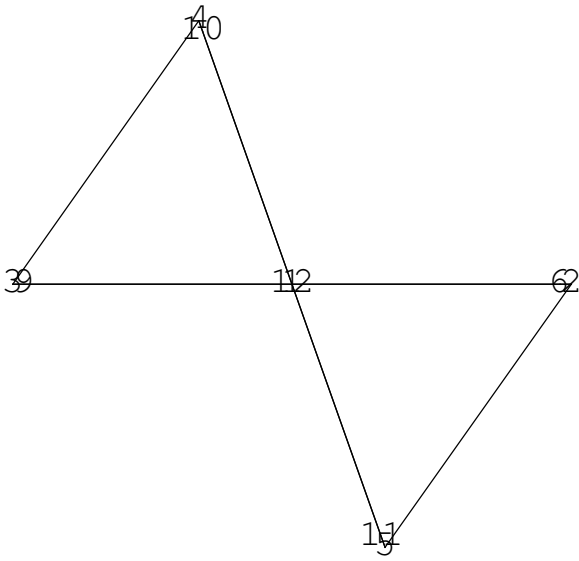
{6, 6, 3}



3.

octahemioctahedron

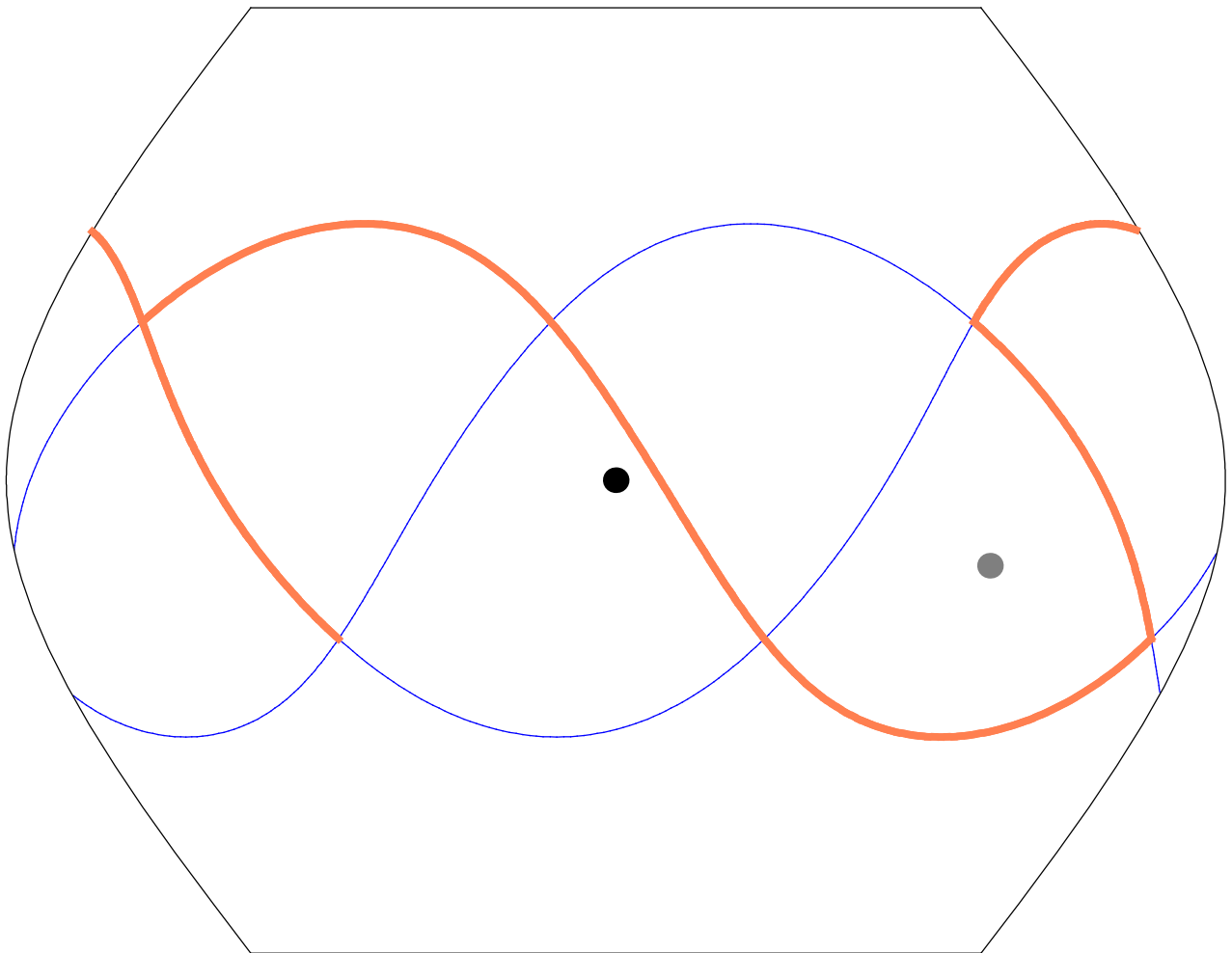
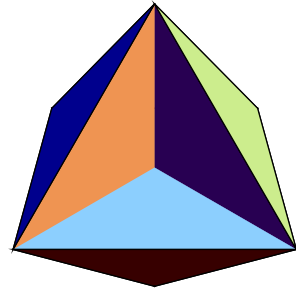
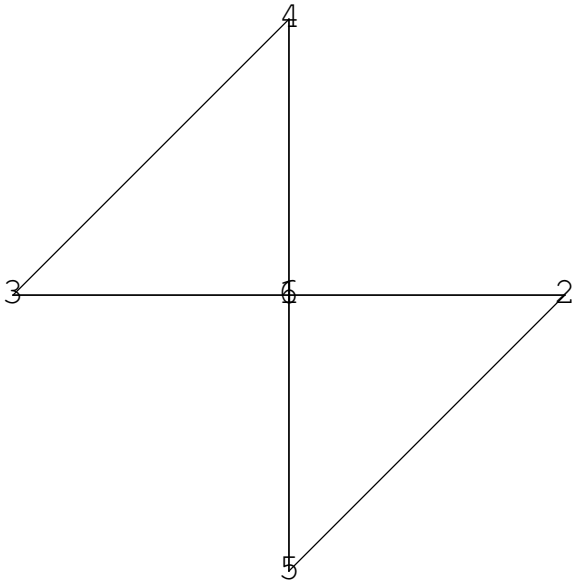
$$\{6, \frac{3}{2}, 6, 3\}$$



4.

tetrahemihexahedron

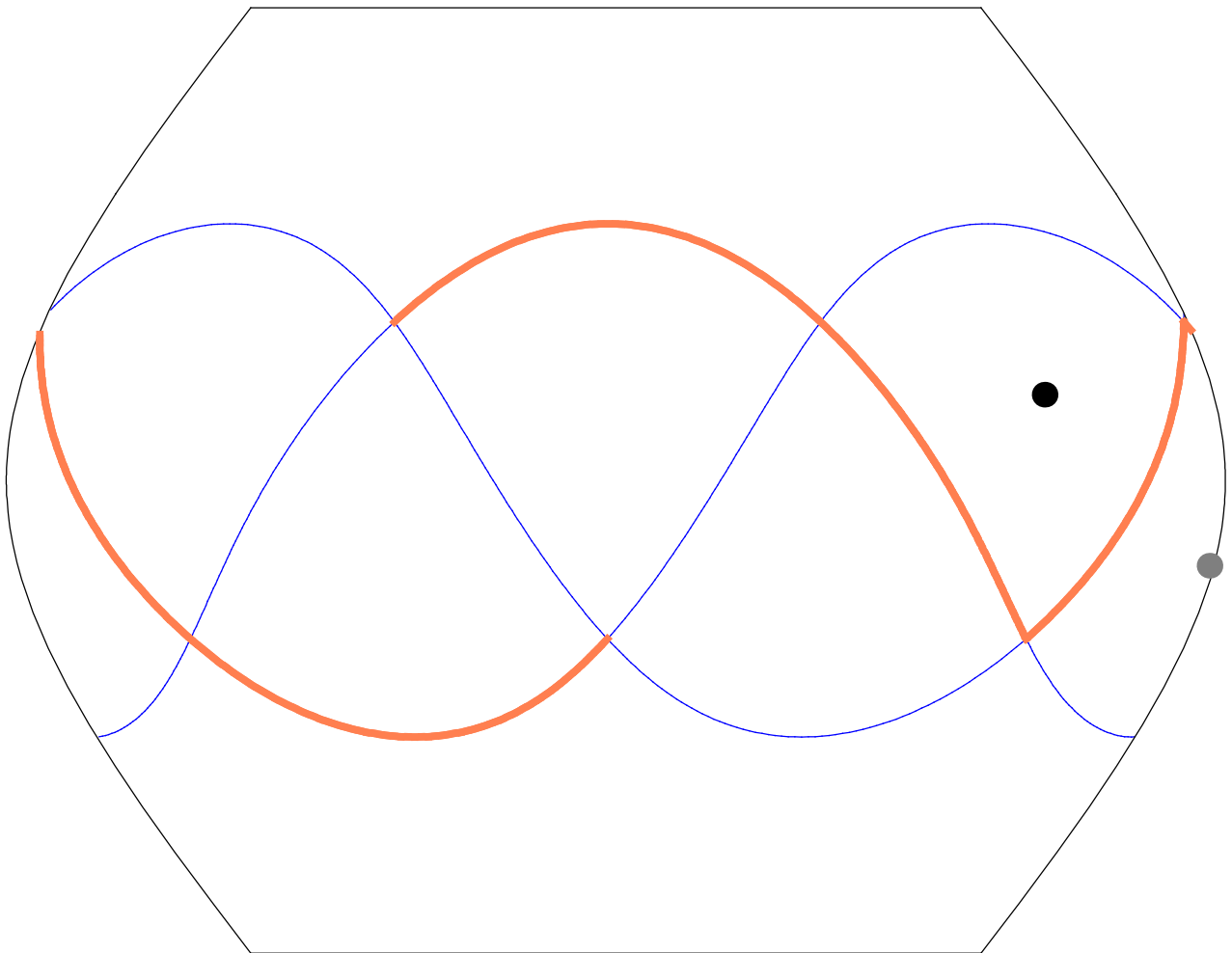
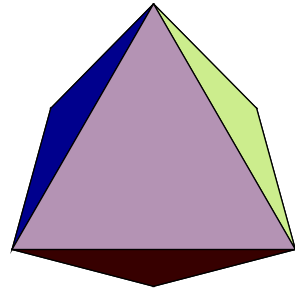
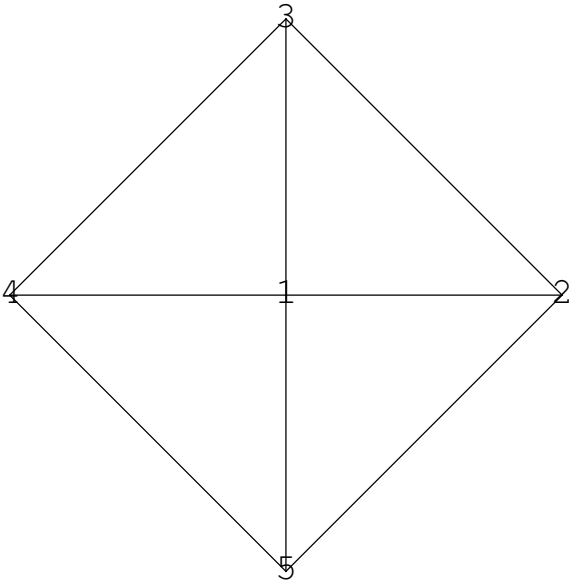
$$\left\{4, \frac{3}{2}, 4, 3\right\}$$



5.

octahedron

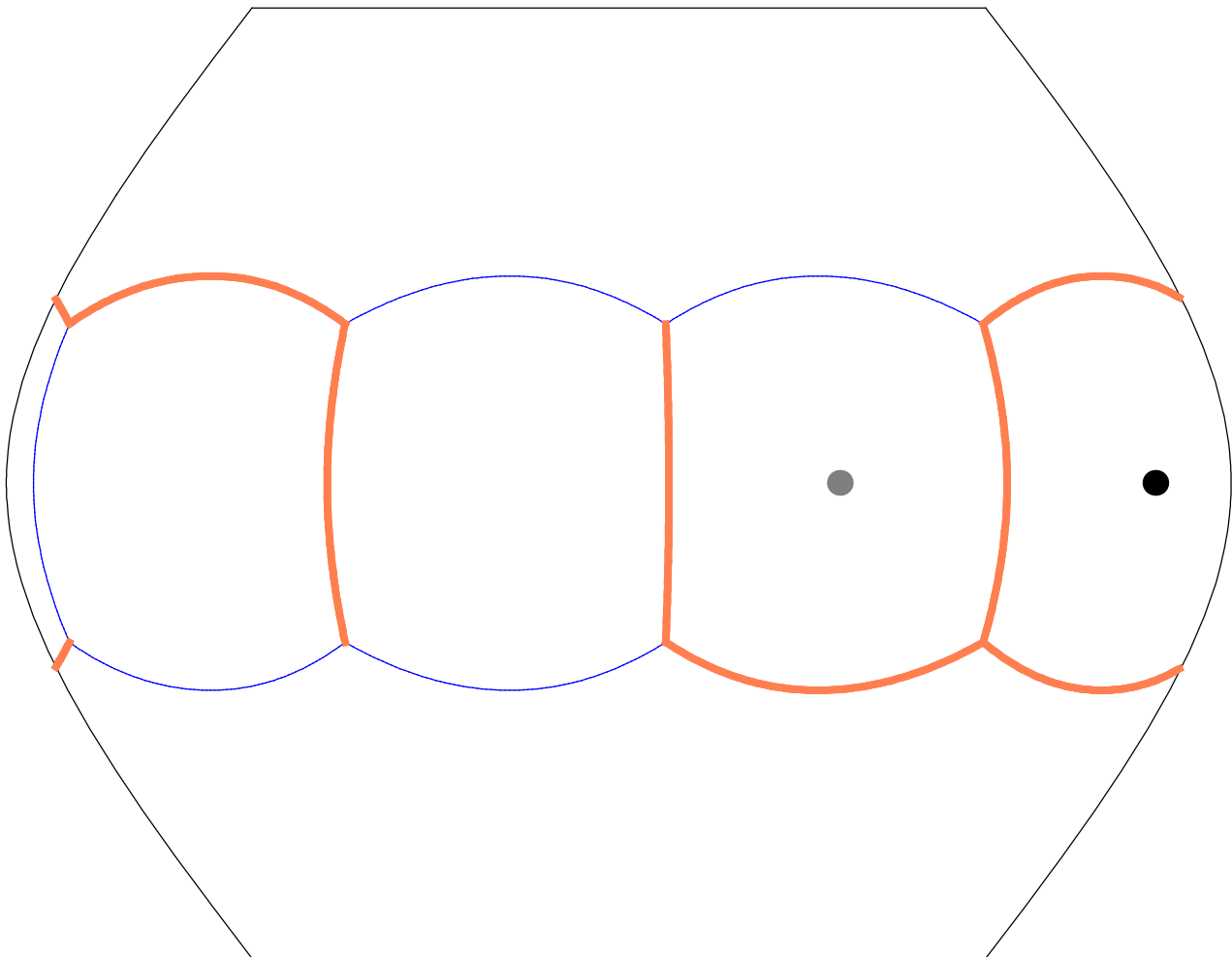
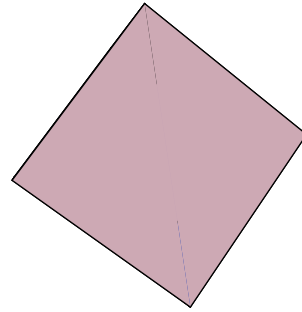
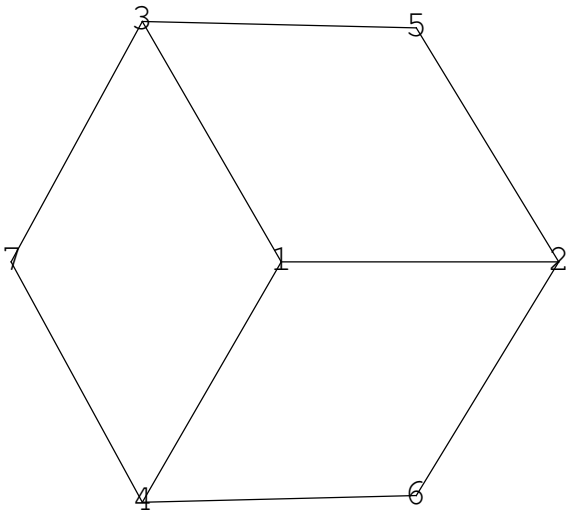
{3, 3, 3, 3}



6.

cube

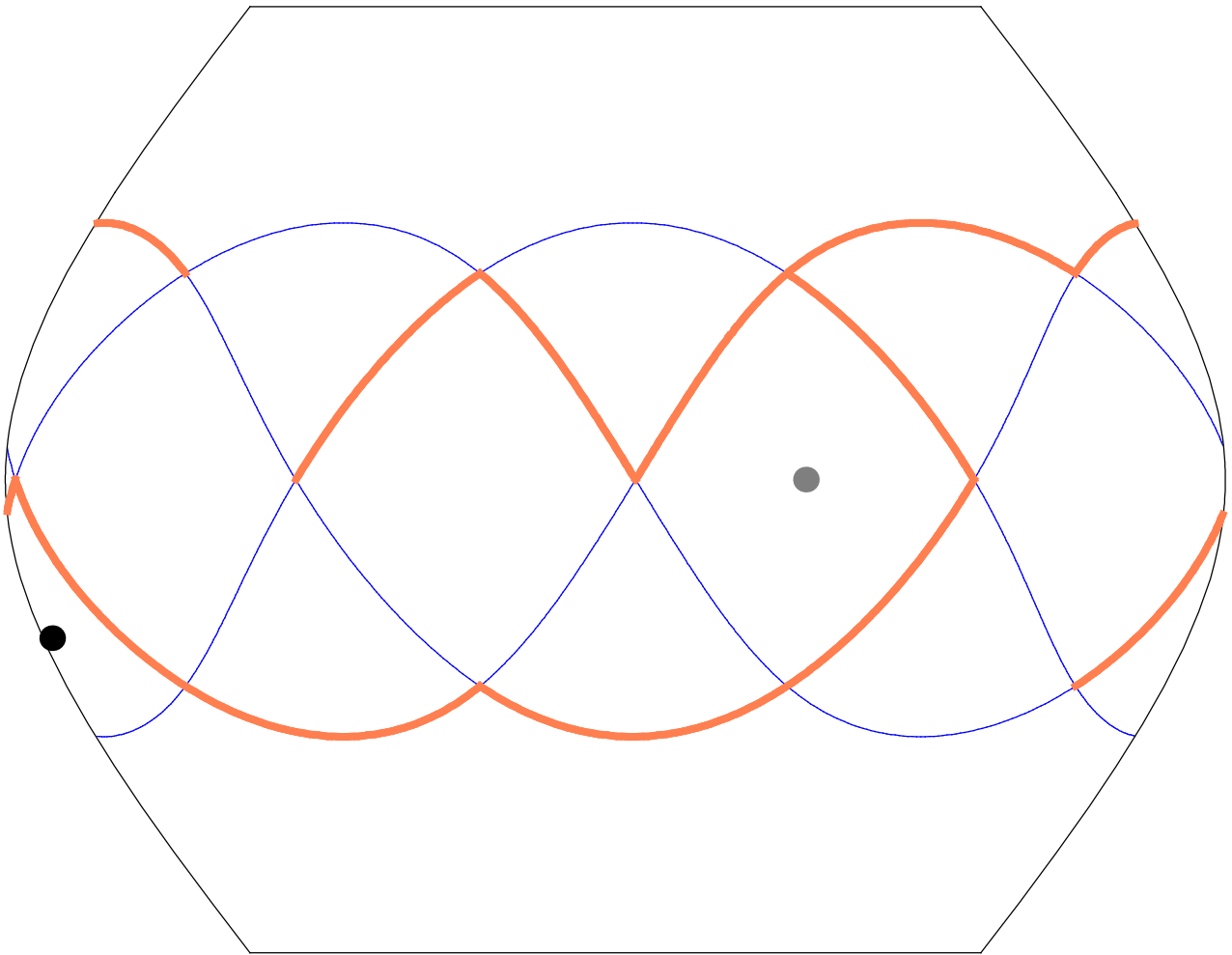
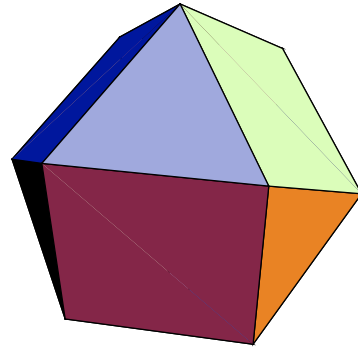
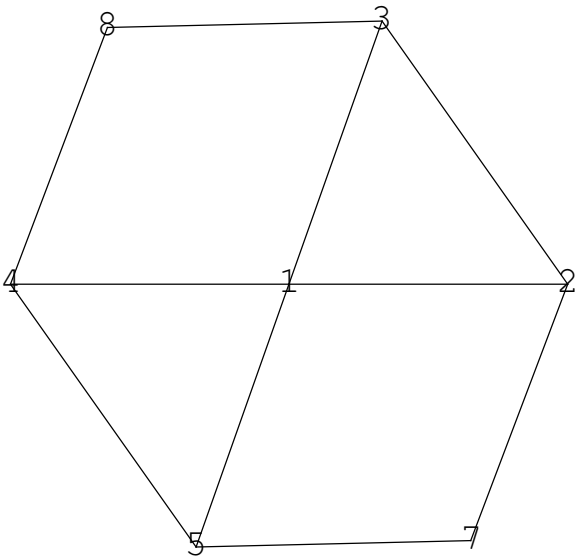
{4, 4, 4}



7.

cuboctahedron

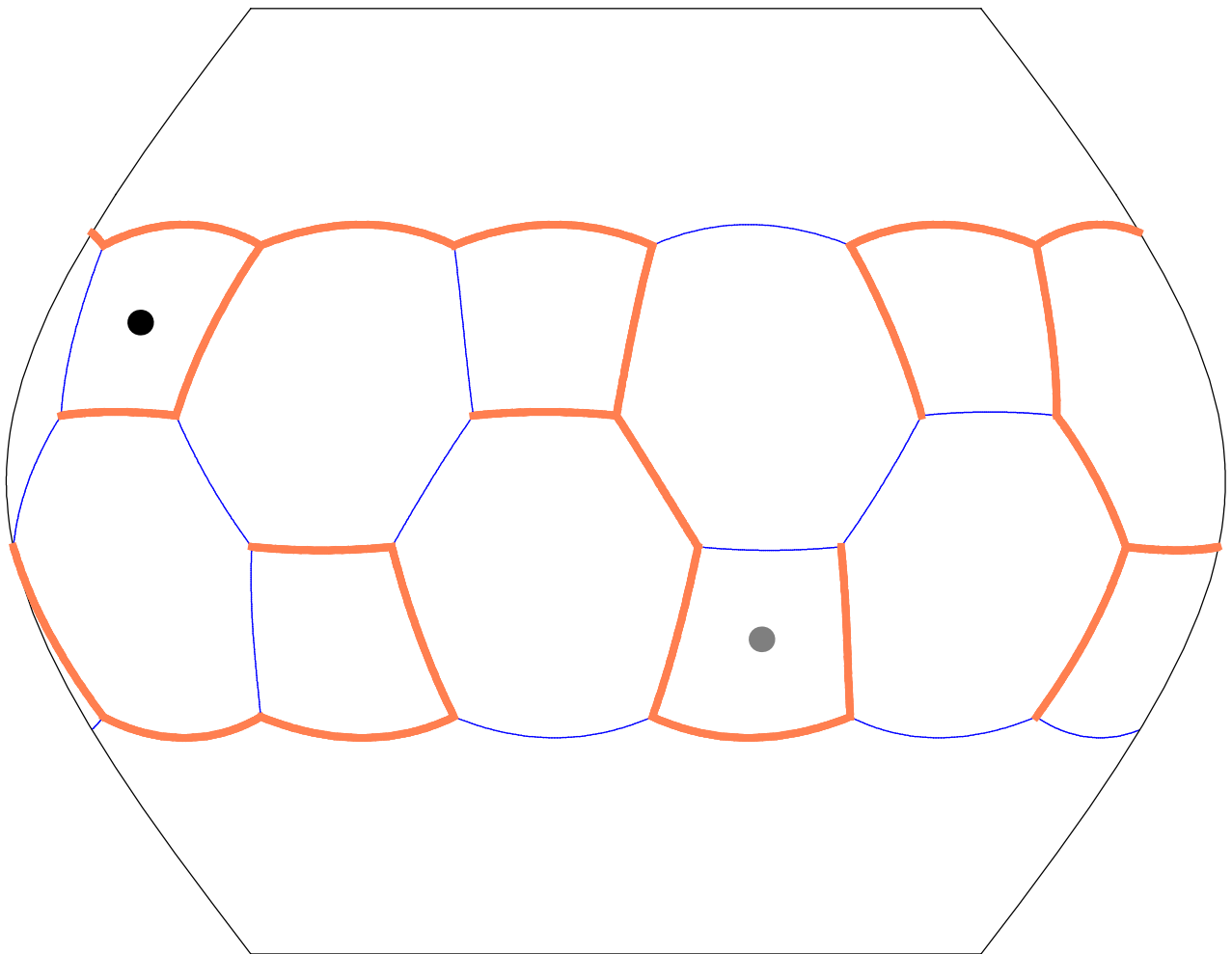
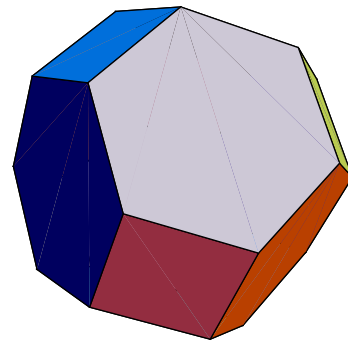
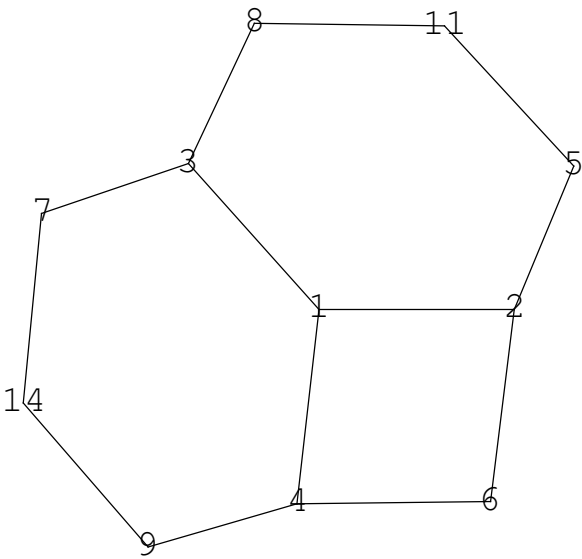
{3, 4, 3, 4}



8.

truncated octahedron

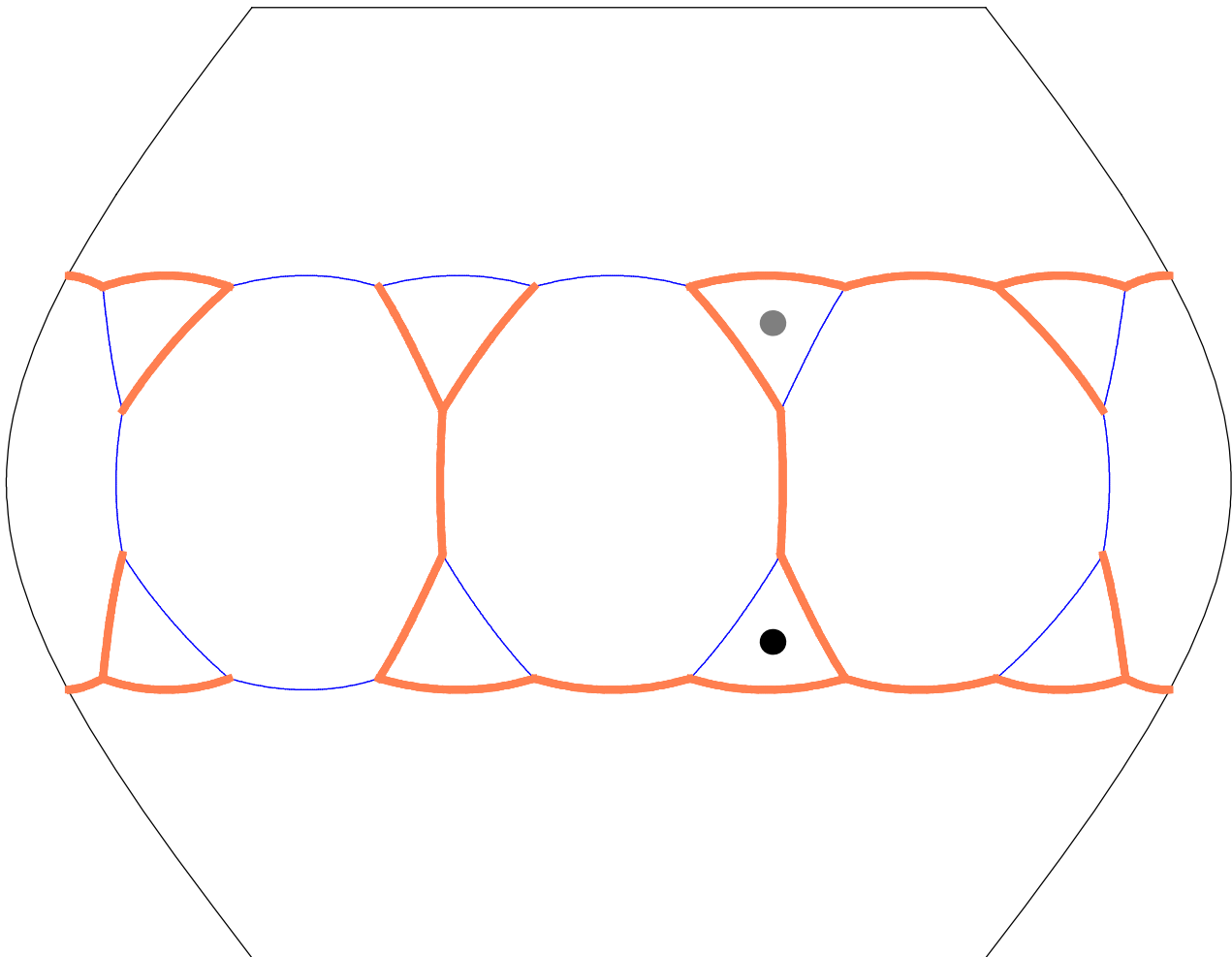
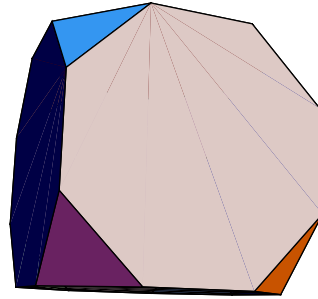
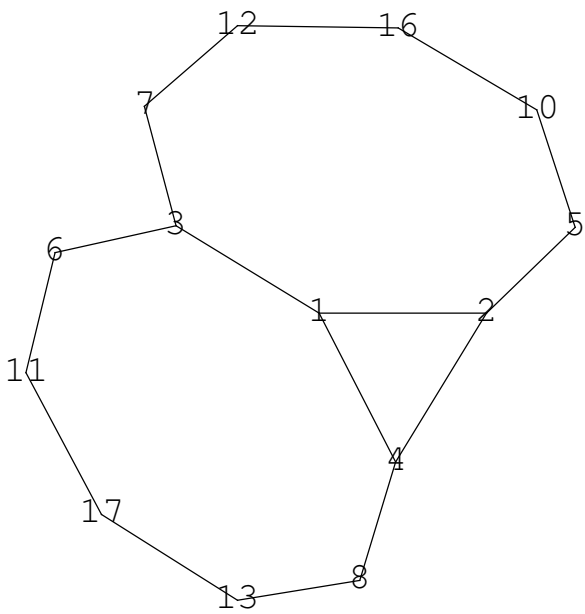
{6, 6, 4}



9.

truncated cube

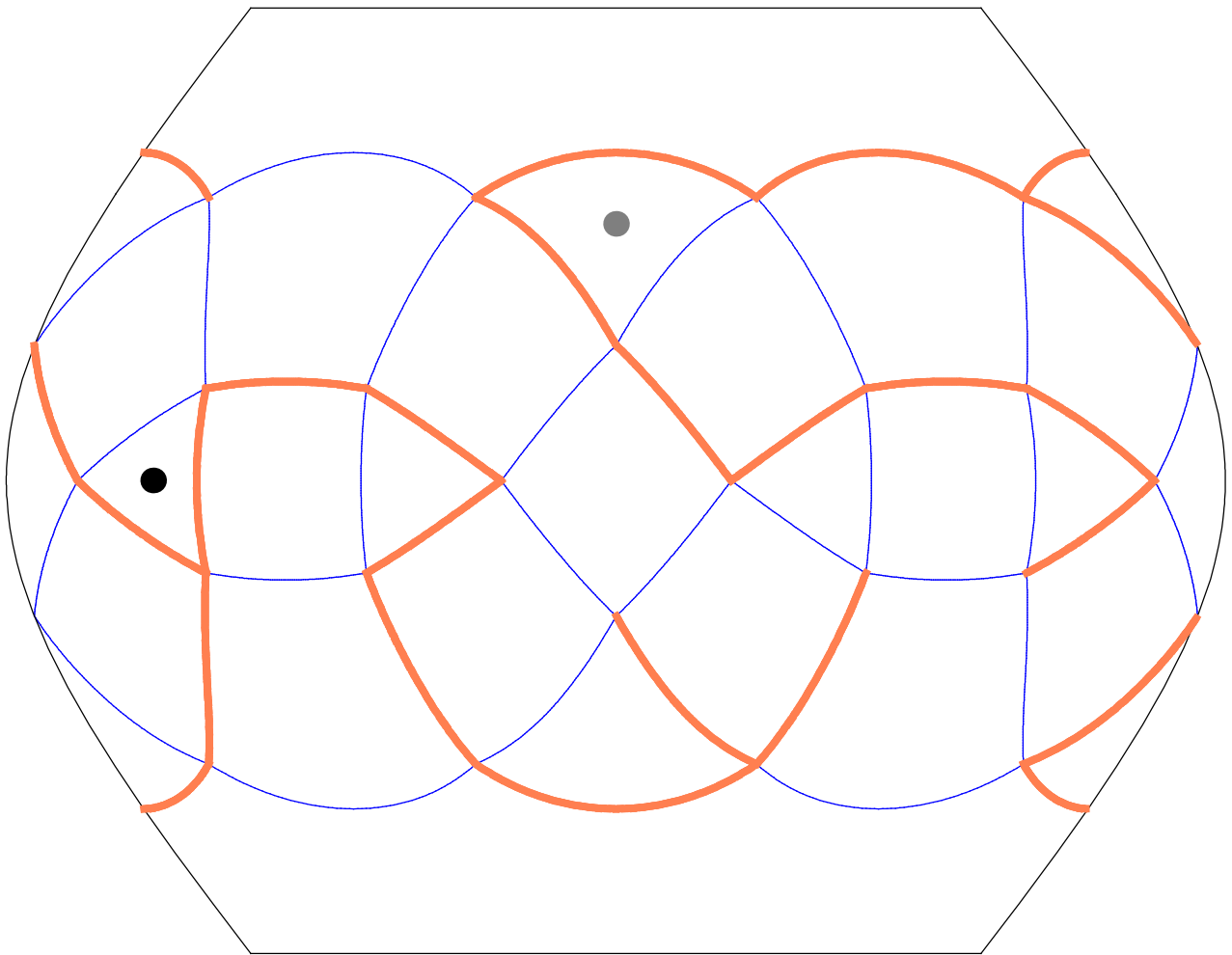
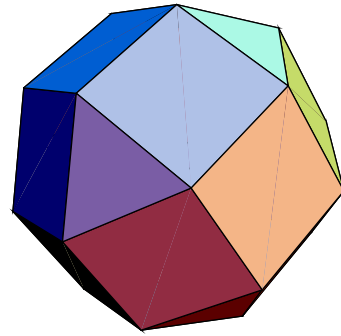
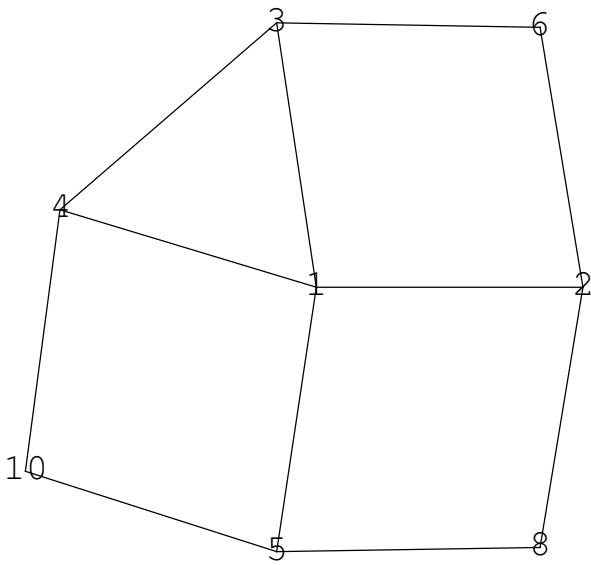
{8, 8, 3}



10.

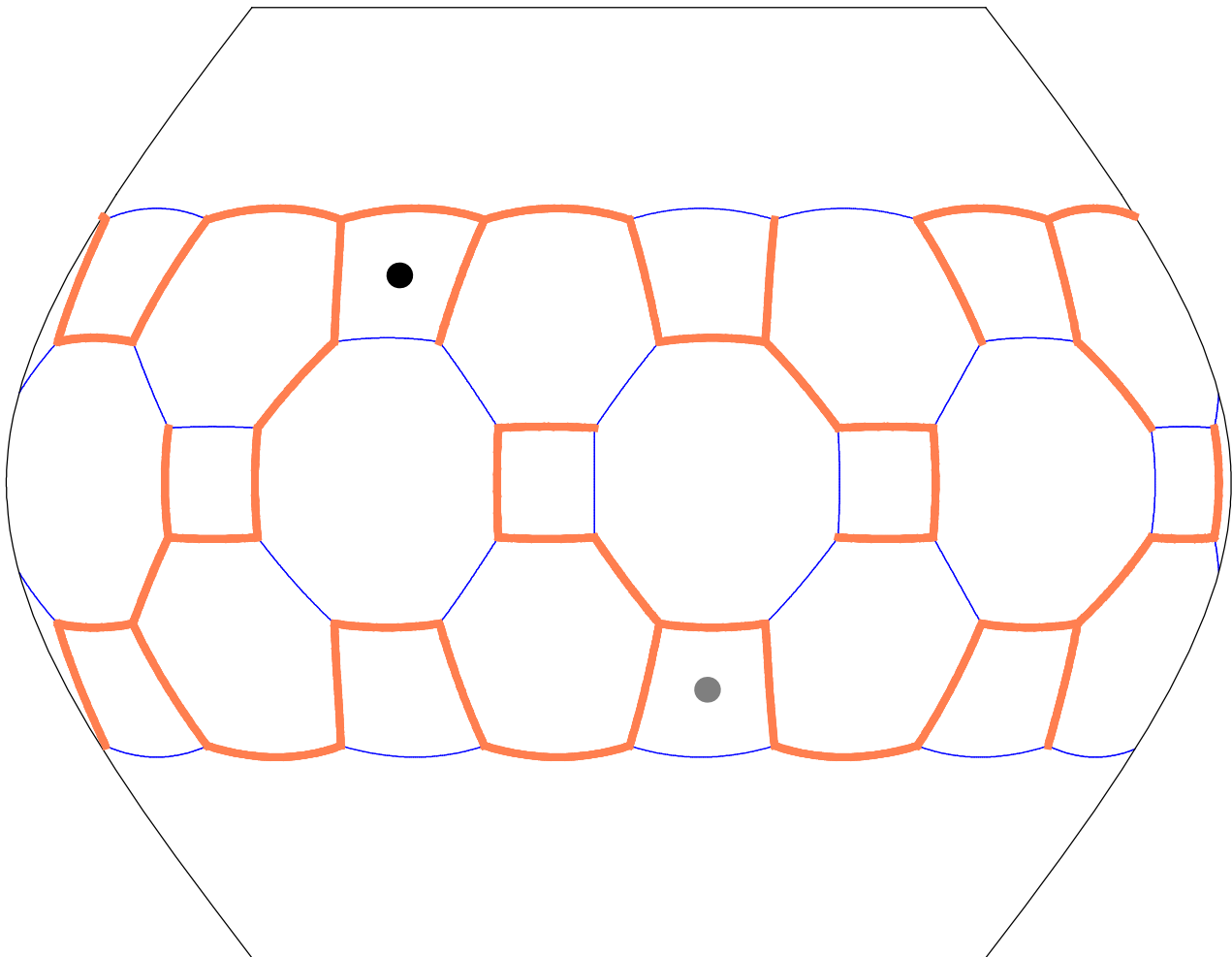
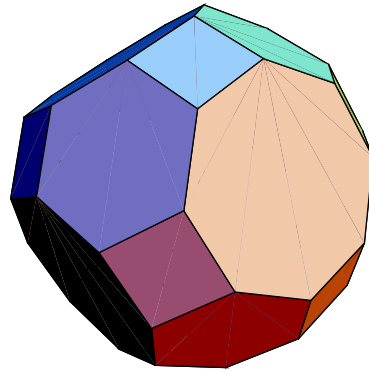
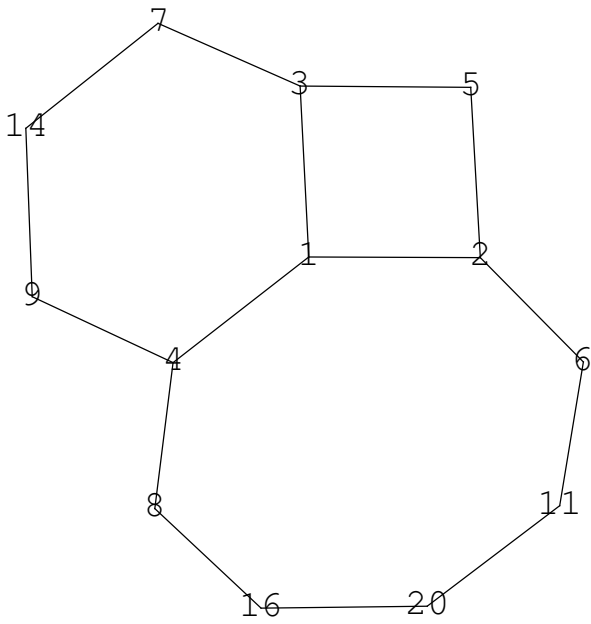
rhombicuboctahedron

{4, 3, 4, 4}



11.

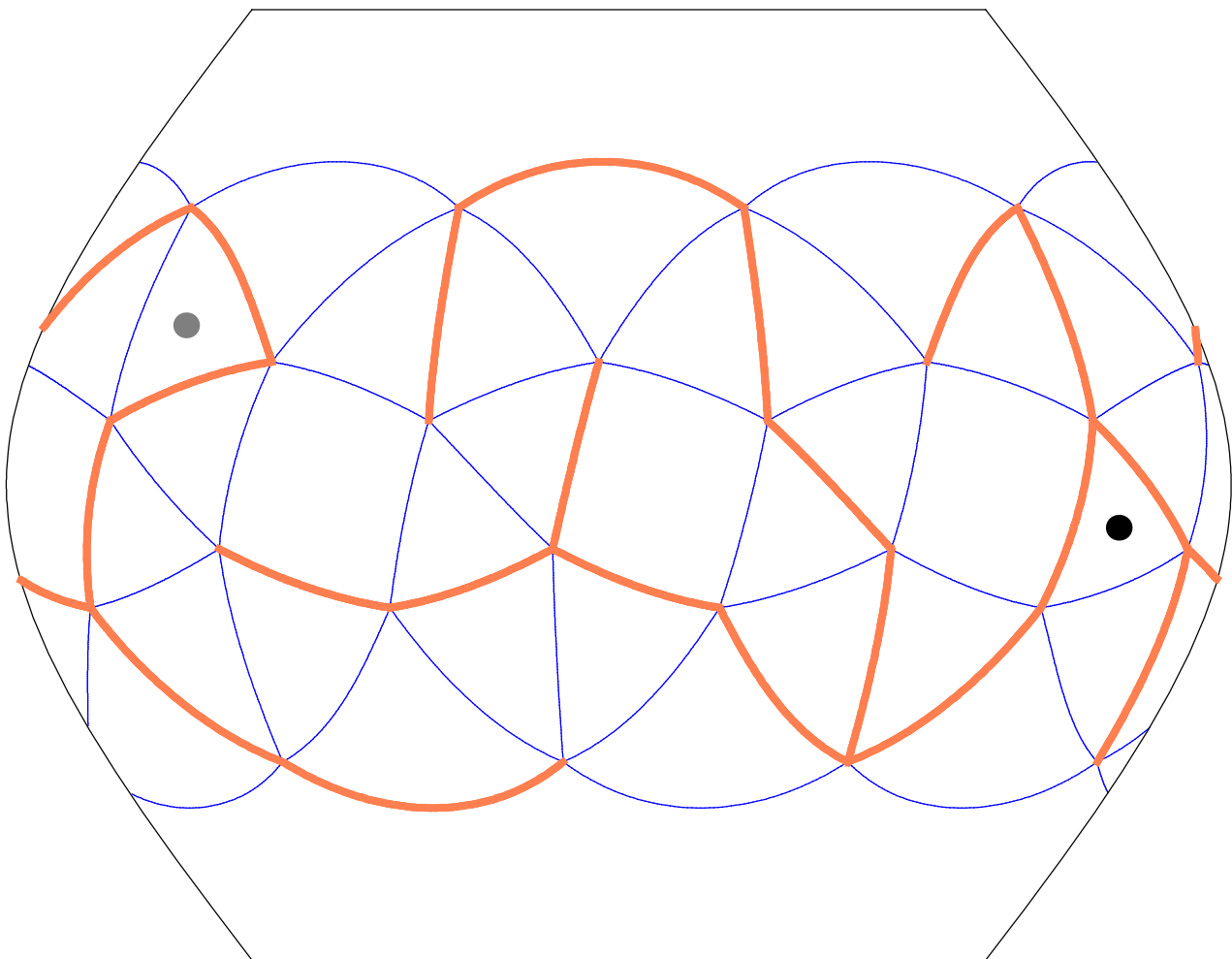
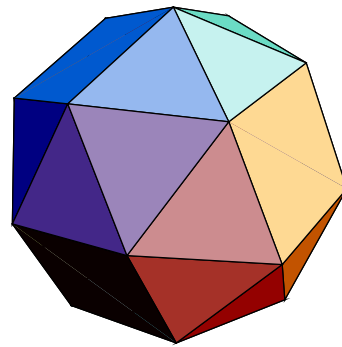
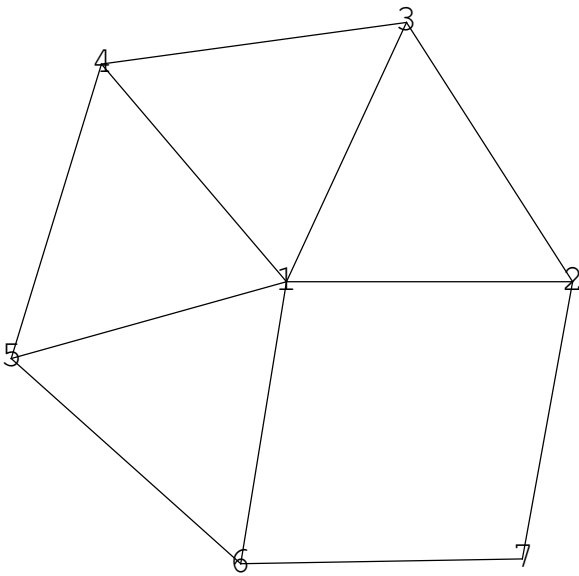
truncated cuboctahedron

 $\{4, 6, 8\}$ 

12.

snub cube

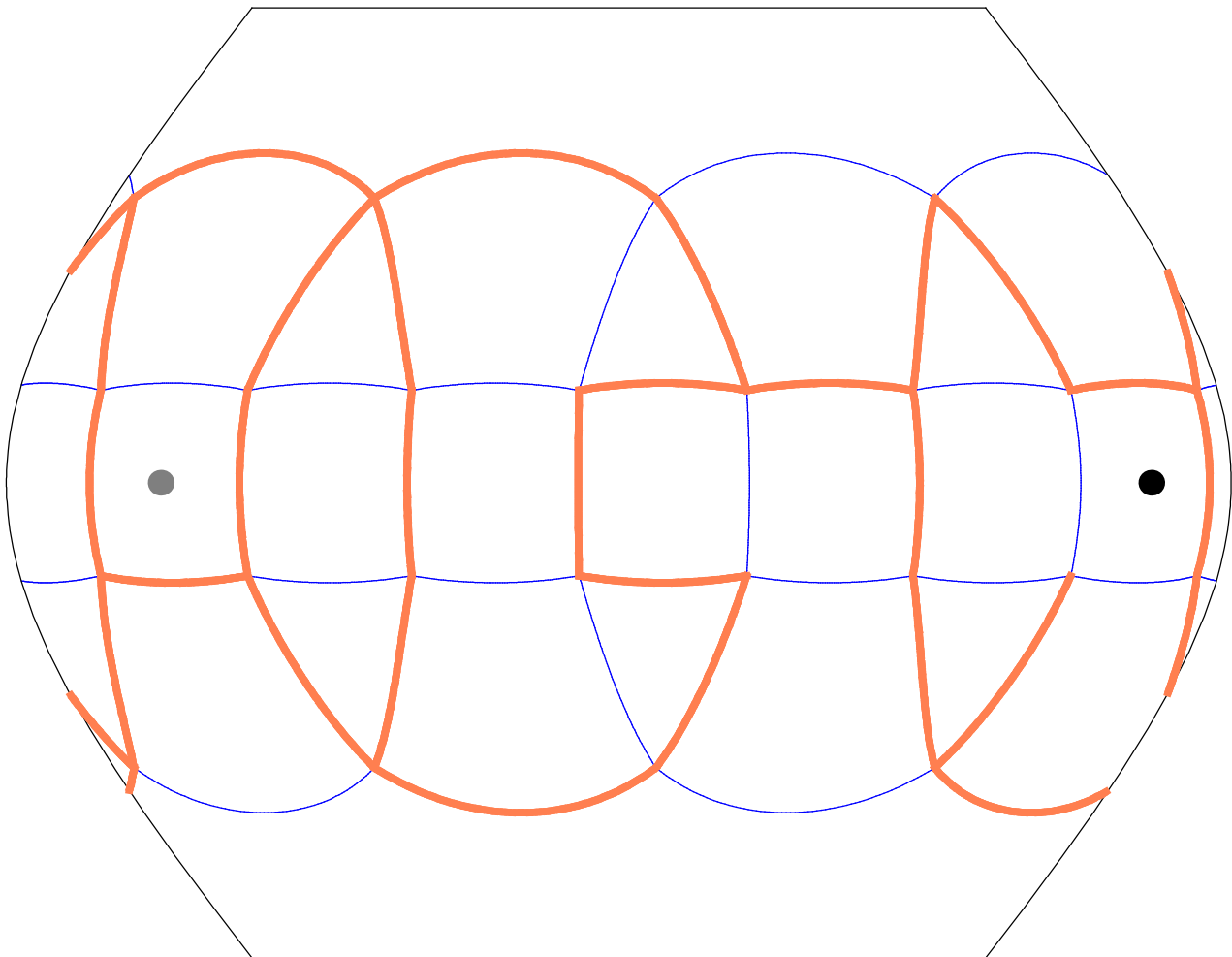
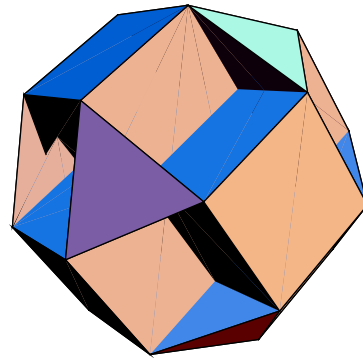
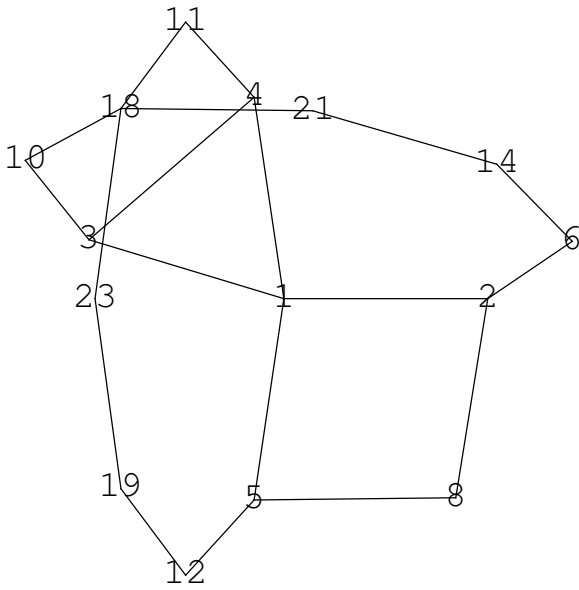
{3, 3, 3, 3, 4}



13.

small cubicuboctahedron

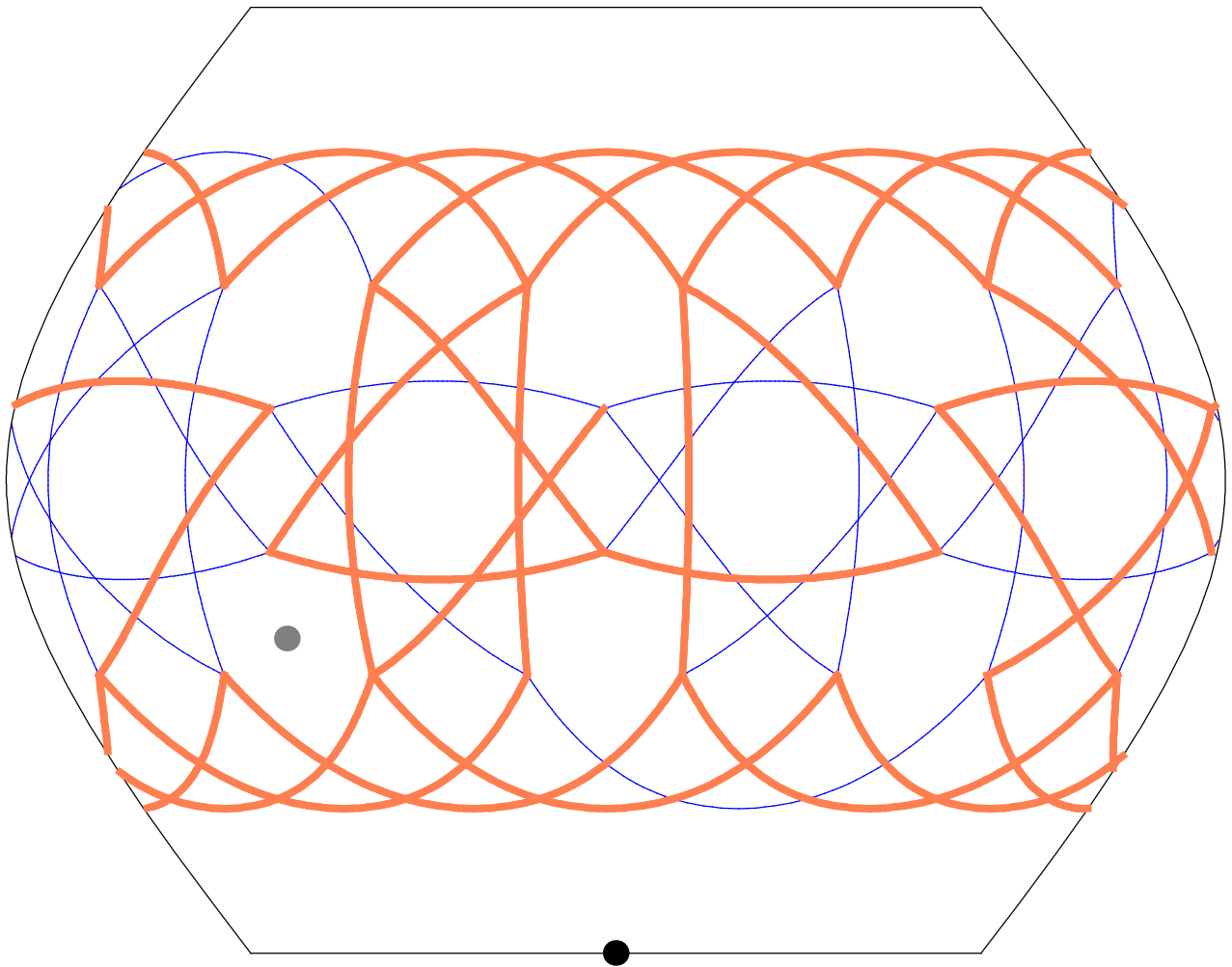
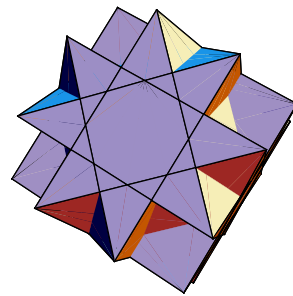
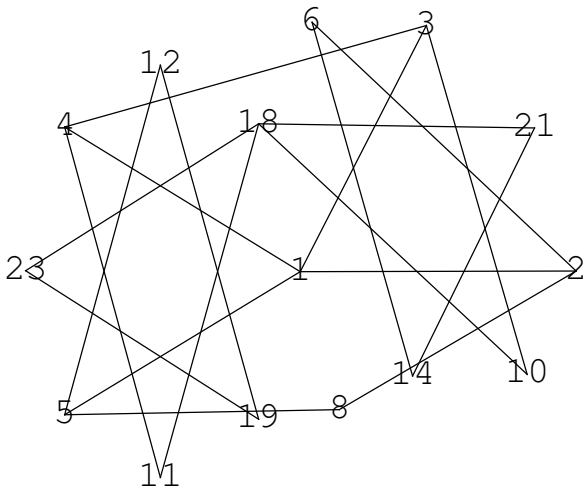
$$\left\{8, \frac{3}{2}, 8, 4\right\}$$



14.

great cubicuboctahedron

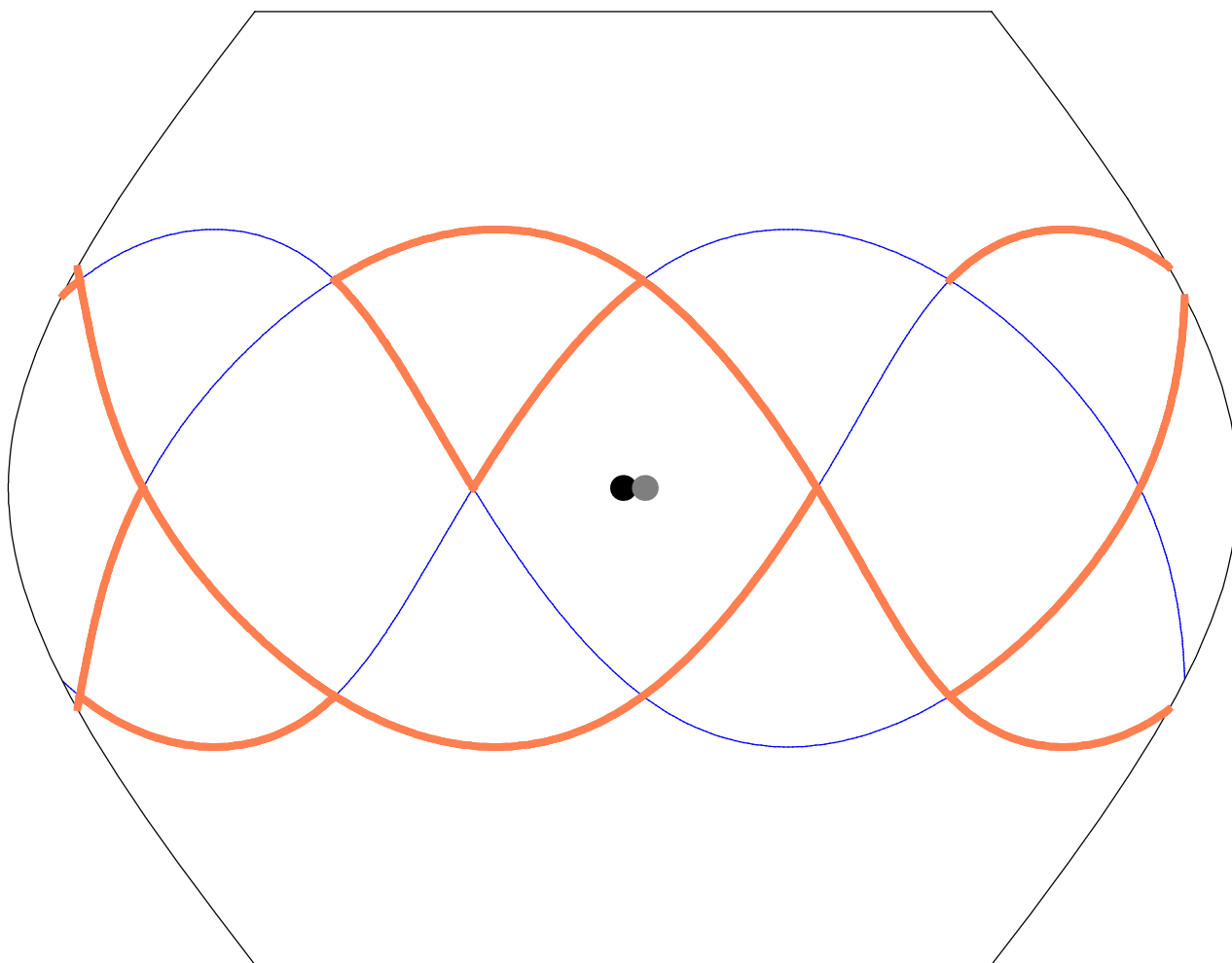
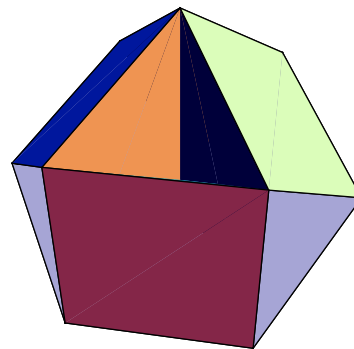
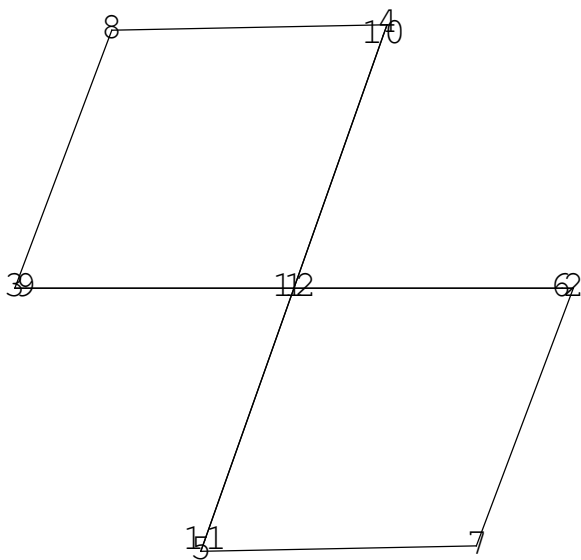
$$\left\{ \frac{8}{3}, 3, \frac{8}{3}, 4 \right\}$$



15.

cubohemioctahedron

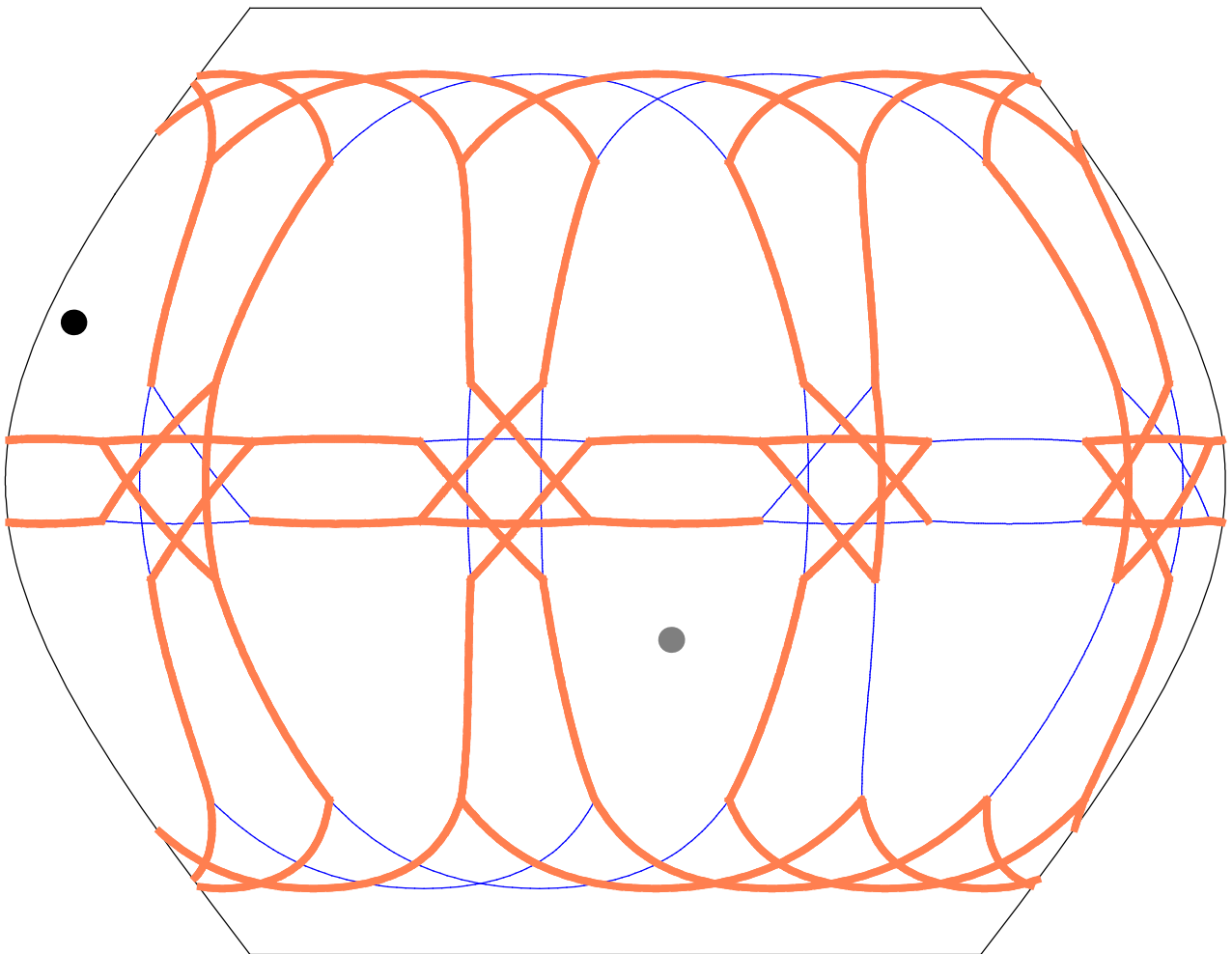
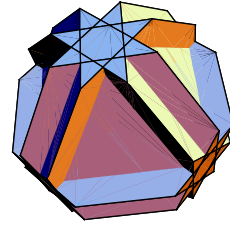
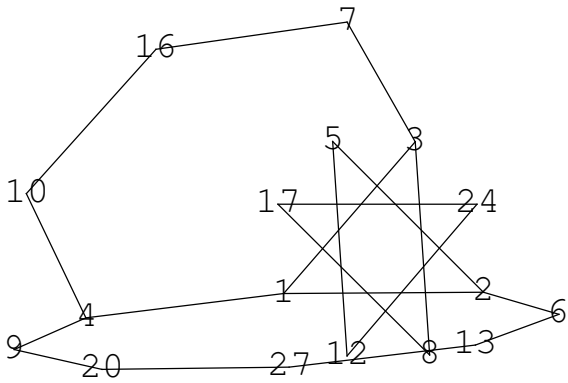
$$\left\{6, \frac{4}{3}, 6, 4\right\}$$



16.

cubitruncated cuboctahedron

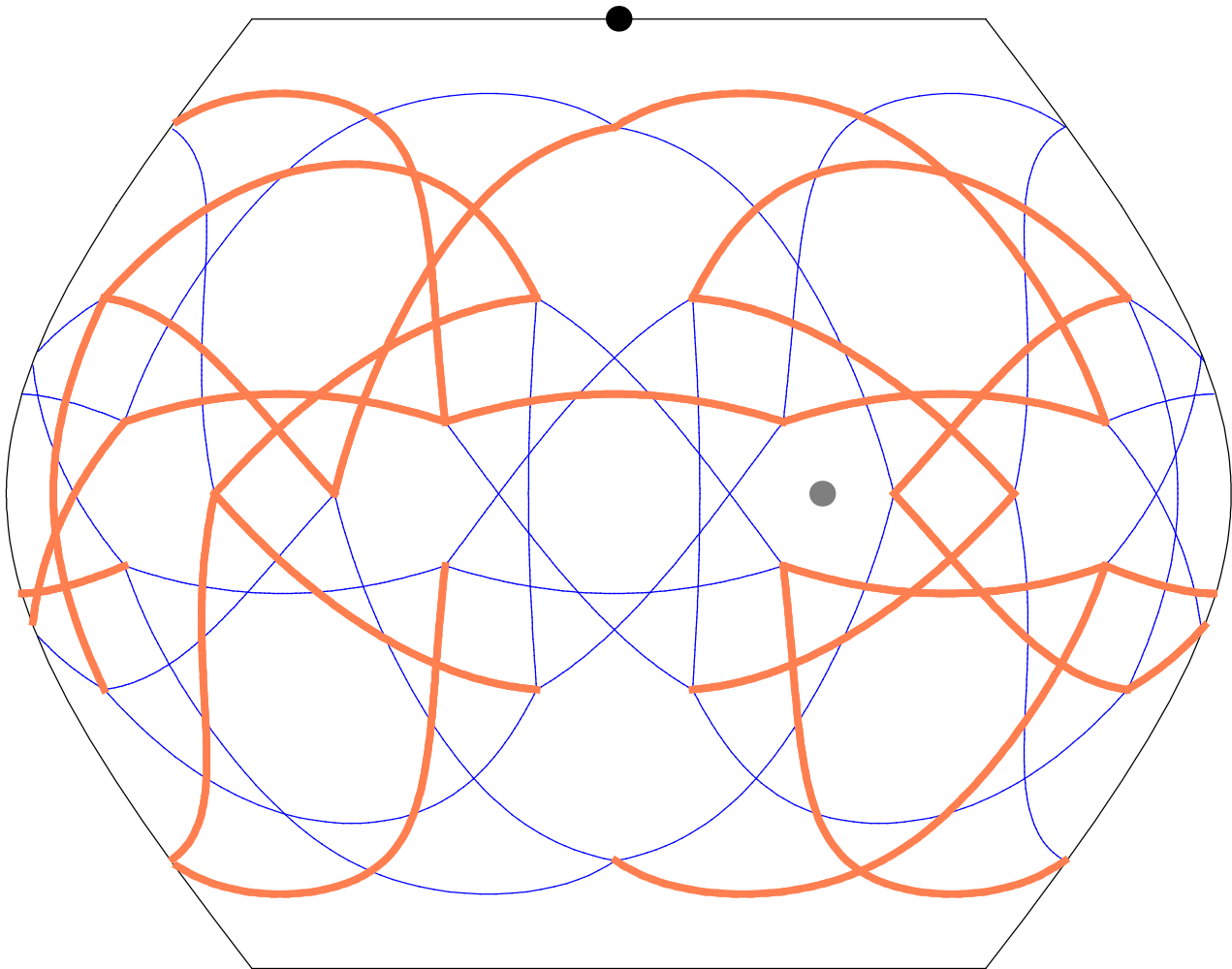
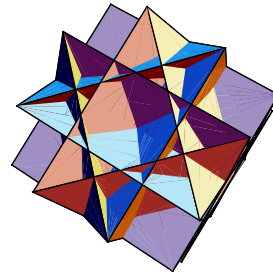
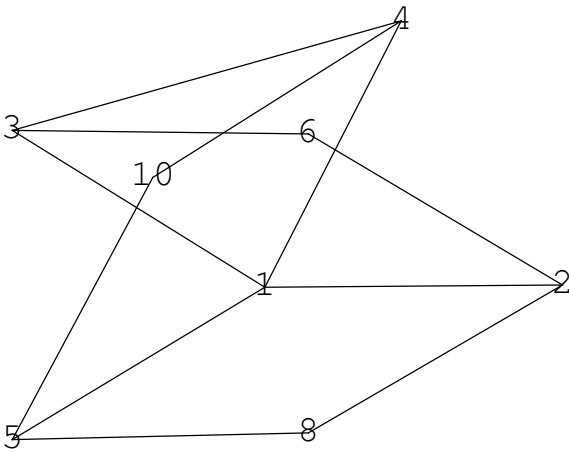
$$\left\{ \frac{8}{3}, 6, 8 \right\}$$



17.

great rhombicuboctahedron

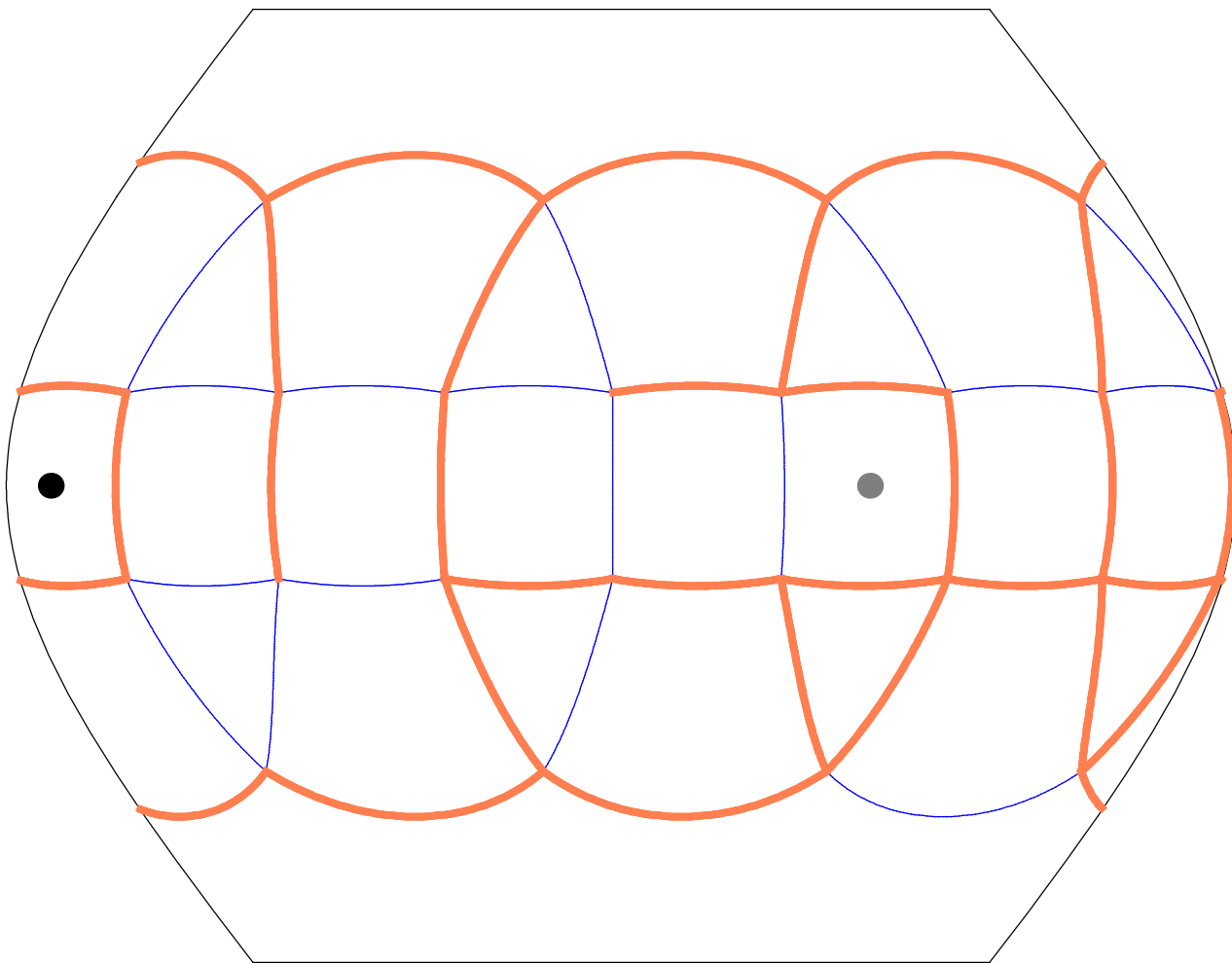
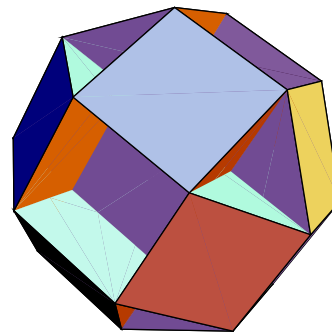
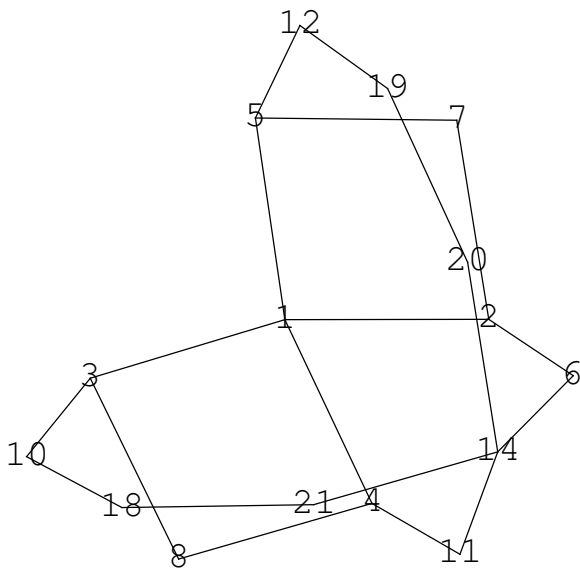
$$\left\{4, \frac{3}{2}, 4, 4\right\}$$



18.

small rhombihexahedron

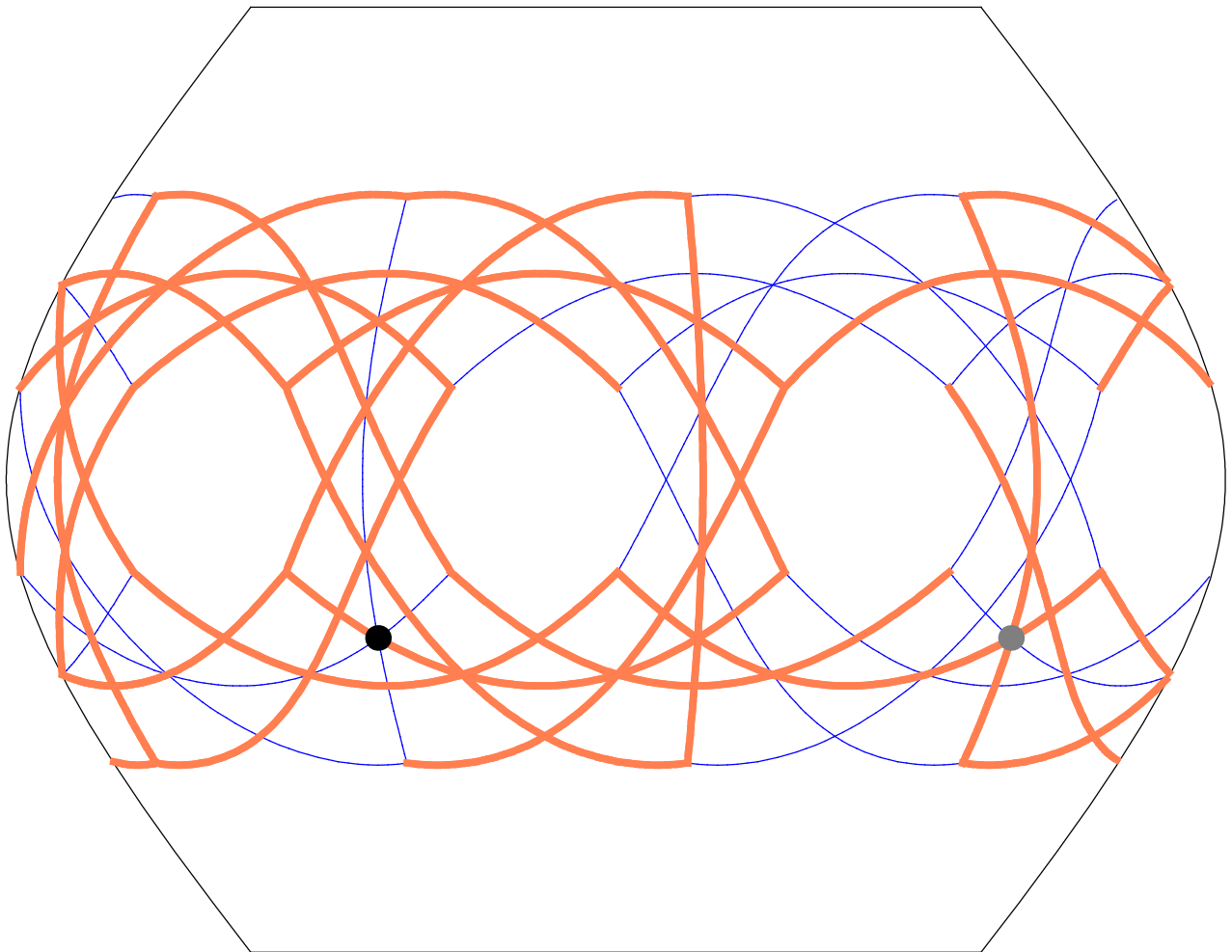
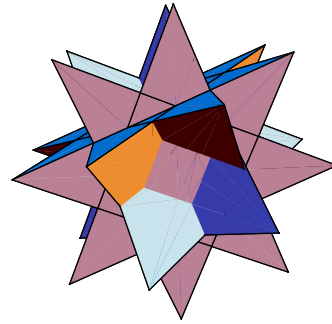
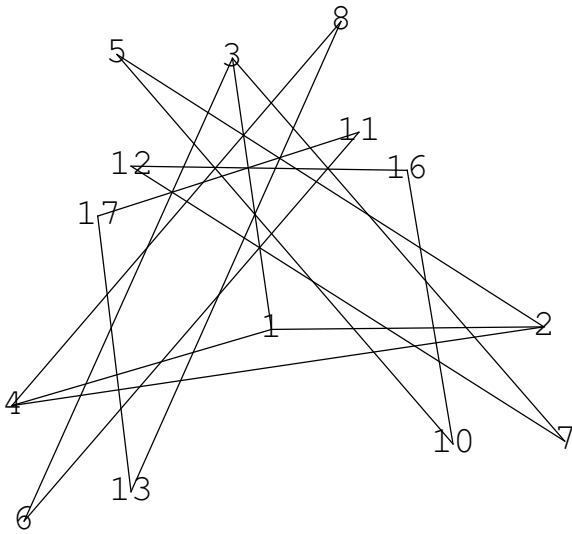
$$\{8, 4, \frac{8}{7}, \frac{4}{3}\}$$



19.

stellated truncated hexahedron

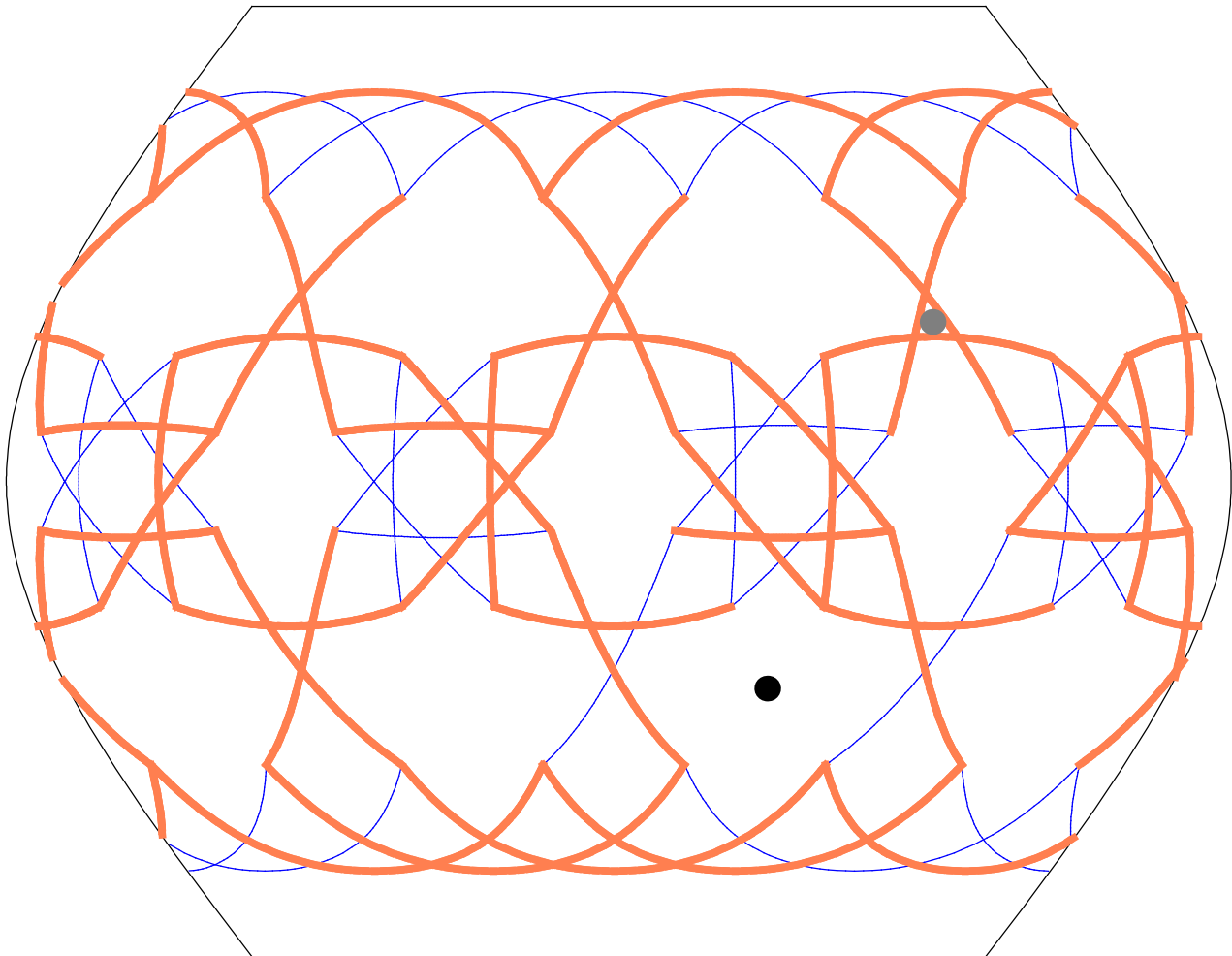
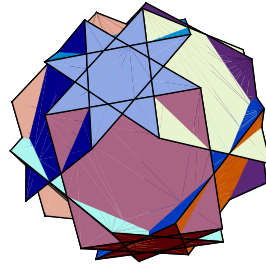
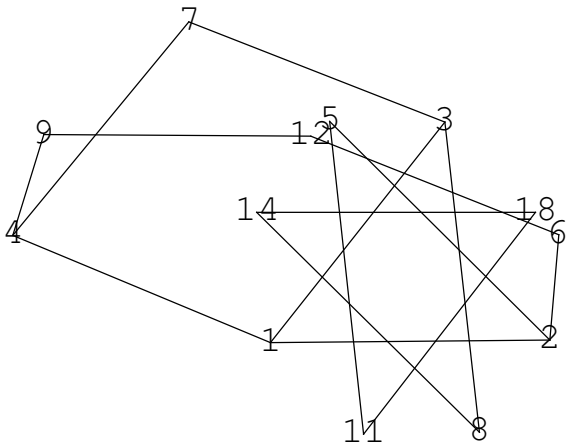
$$\left\{ \frac{8}{3}, \frac{8}{3}, 3 \right\}$$



20.

great truncated cuboctahedron

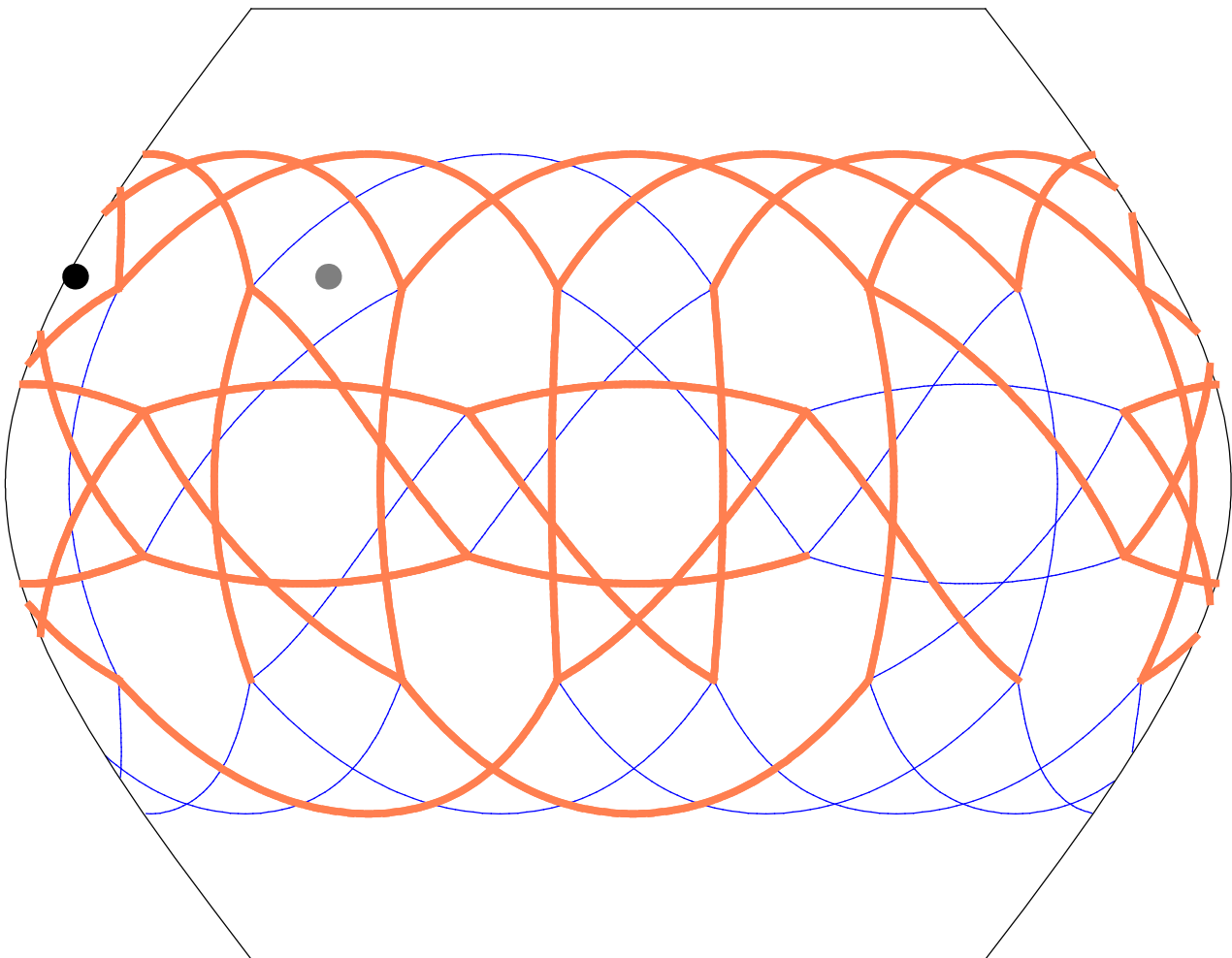
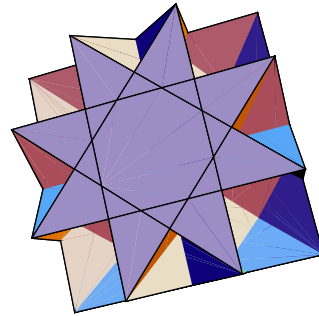
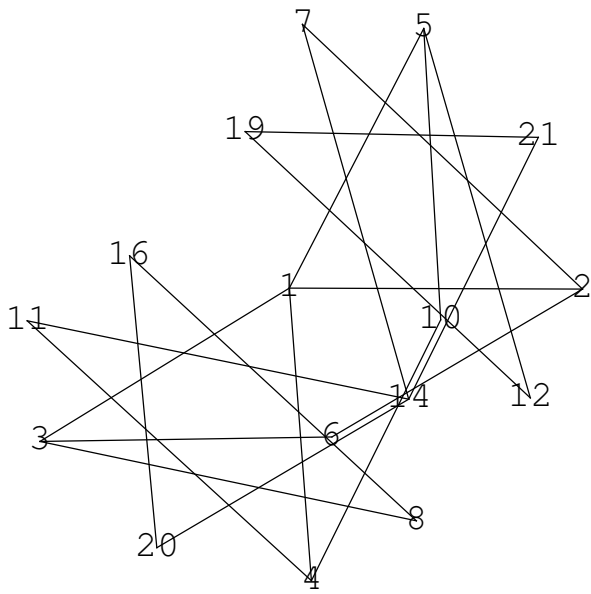
$$\left\{ \frac{8}{3}, 4, 6 \right\}$$



21.

great rhombihexahedron

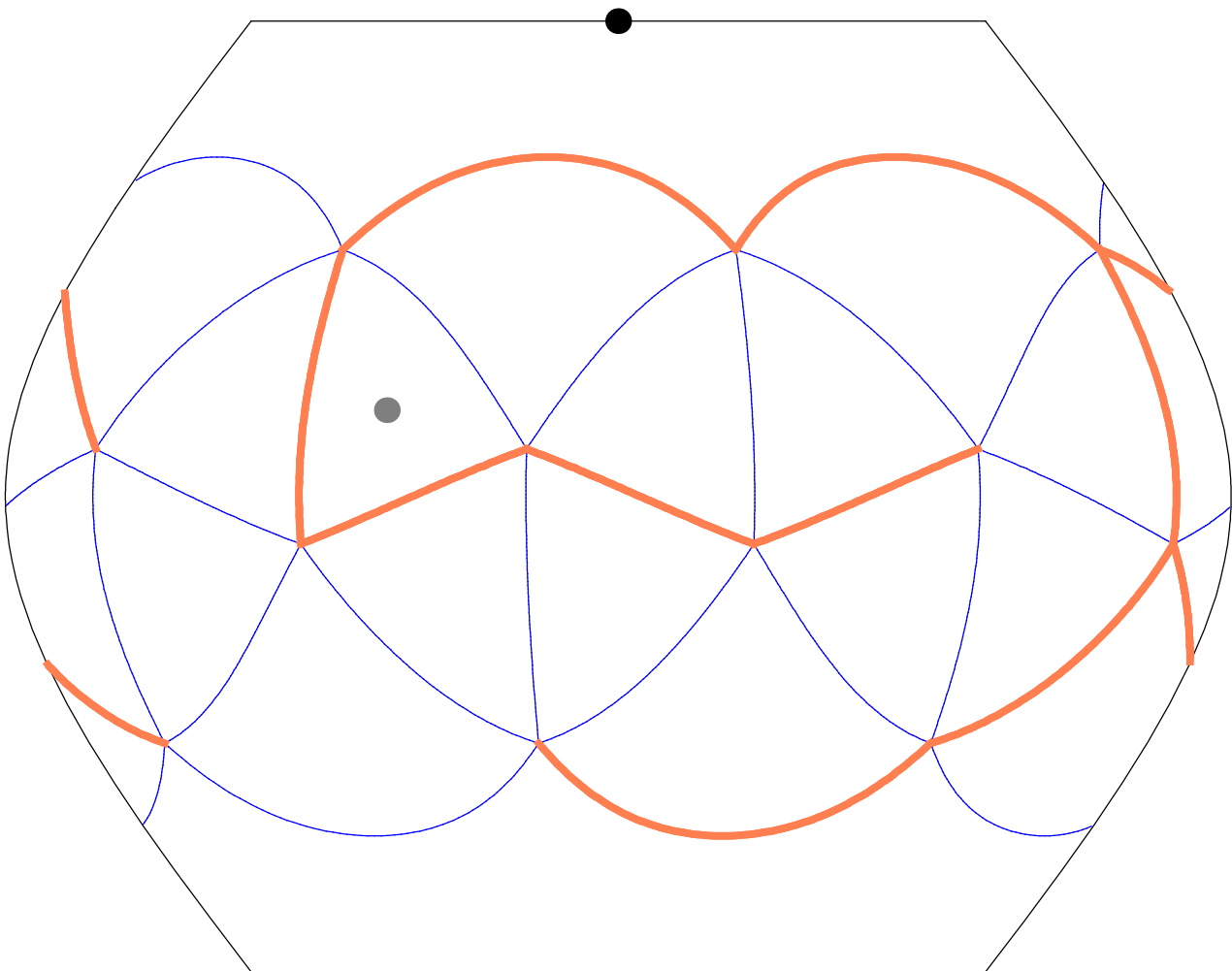
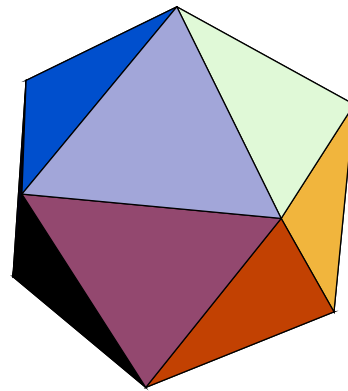
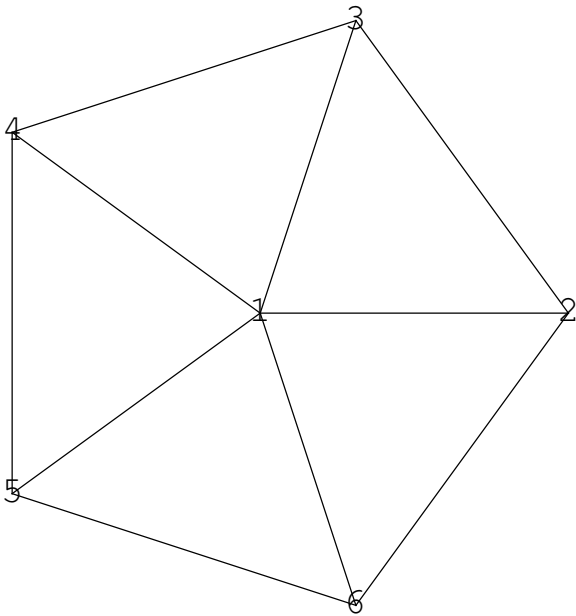
$$\left\{4, \frac{8}{3}, \frac{4}{3}, \frac{8}{5}\right\}$$



22.

icosahedron

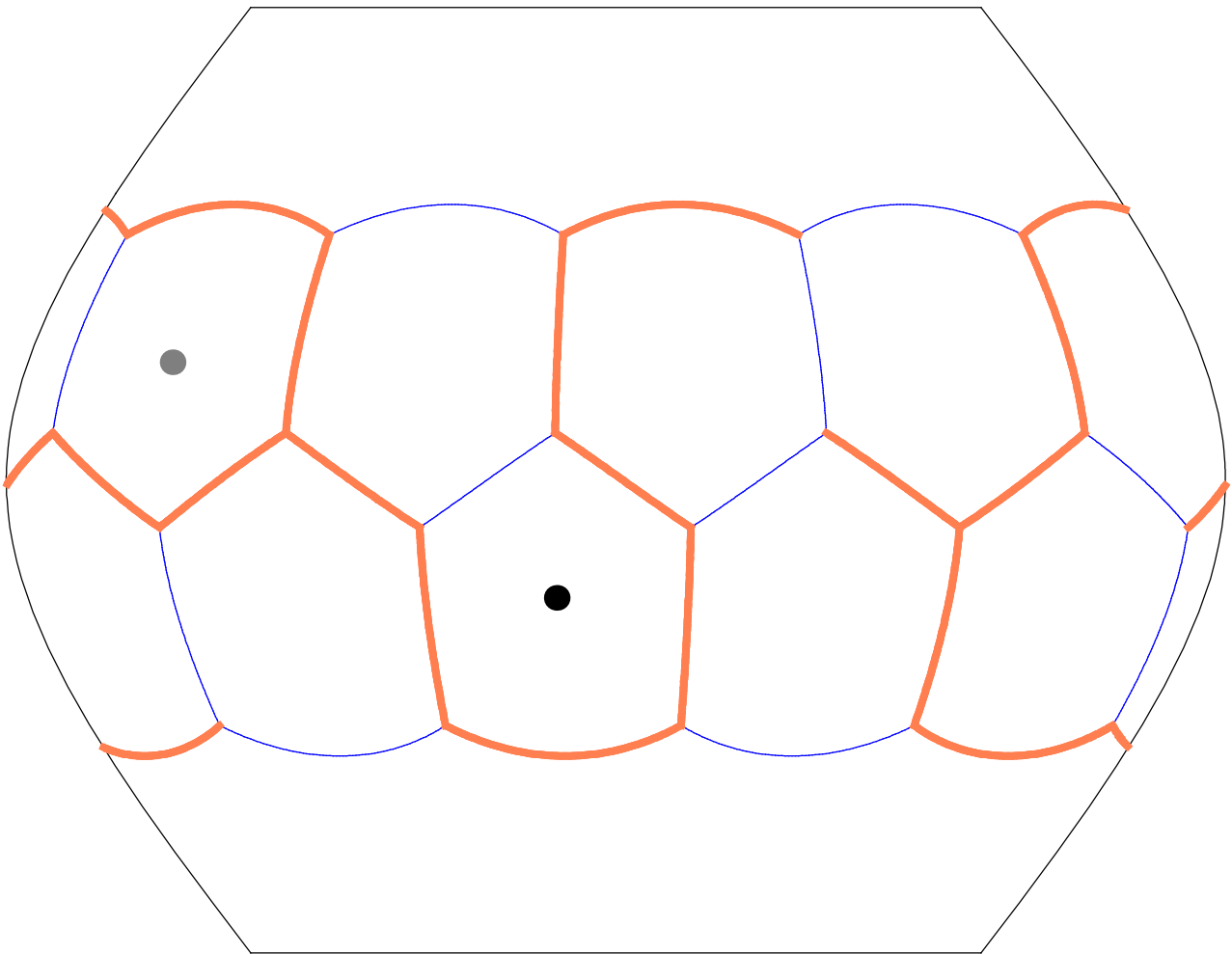
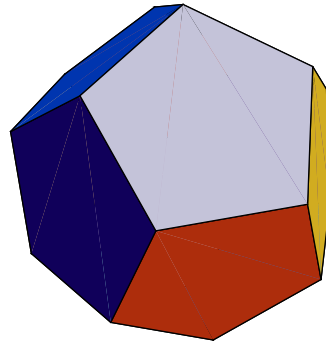
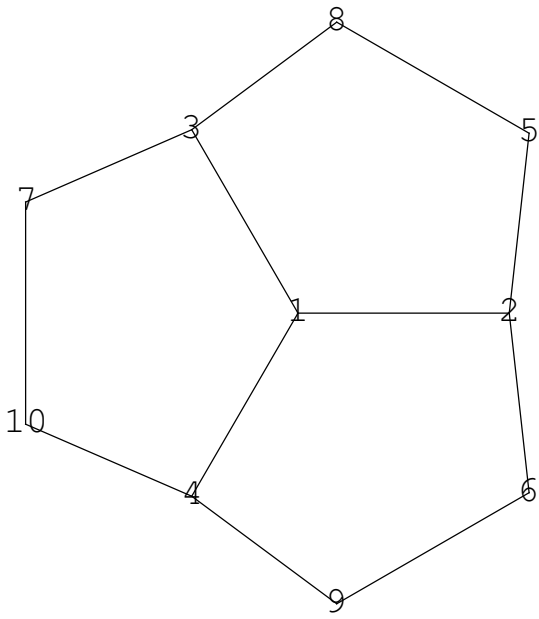
{3, 3, 3, 3, 3}



23.

dodecahedron

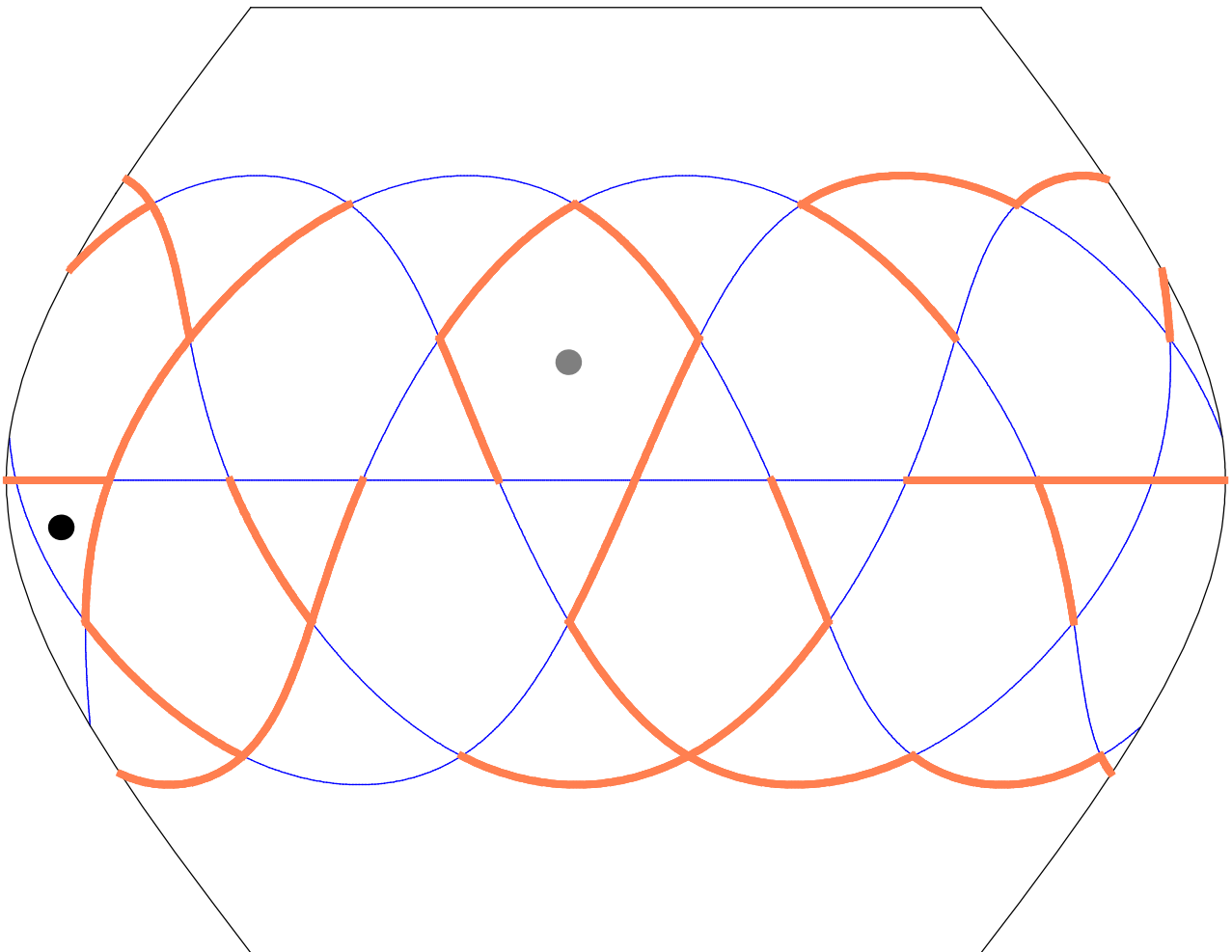
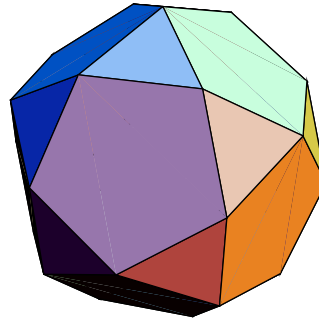
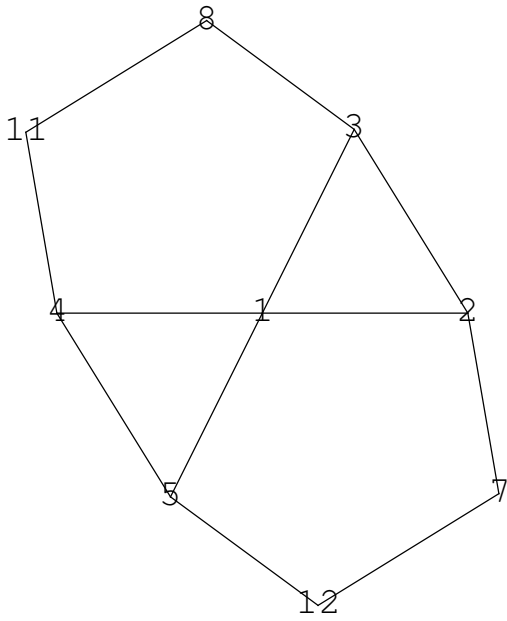
{5, 5, 5}



24.

icosidodecahedron

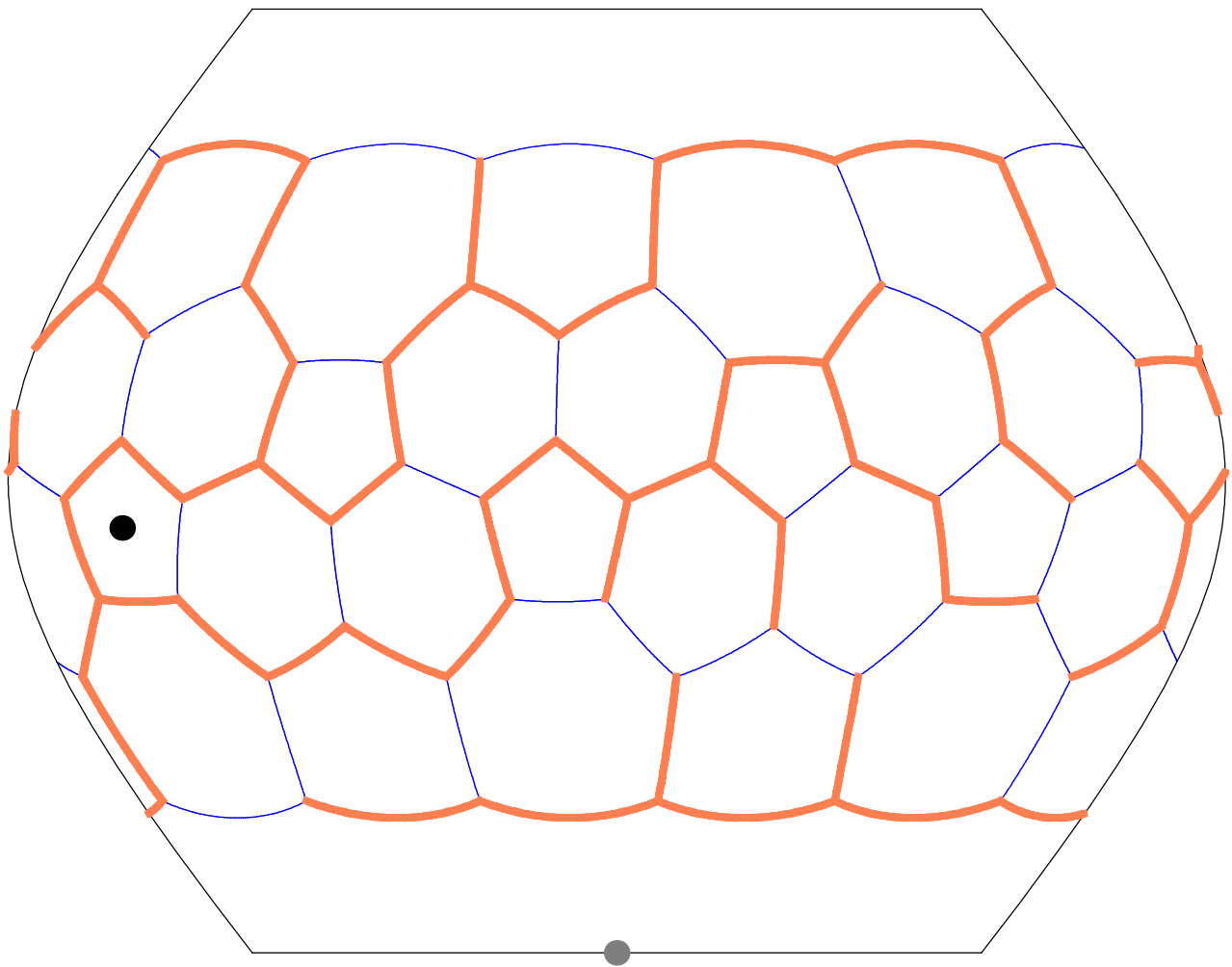
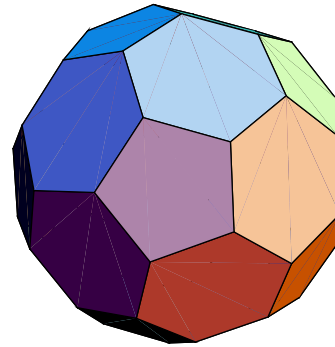
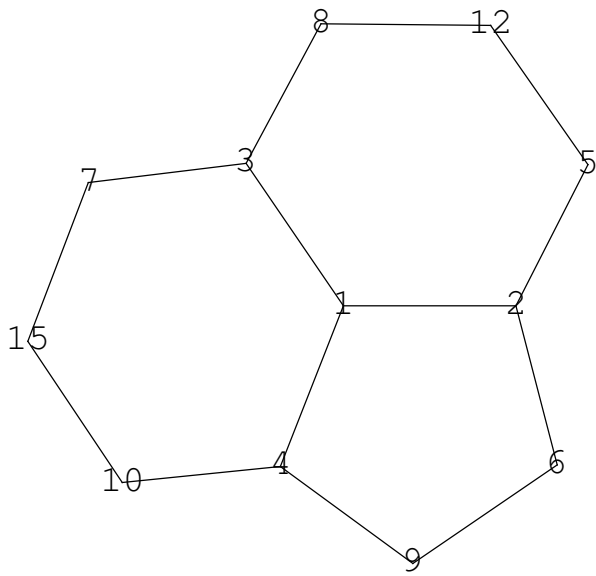
{3, 5, 3, 5}



25.

truncated icosahedron

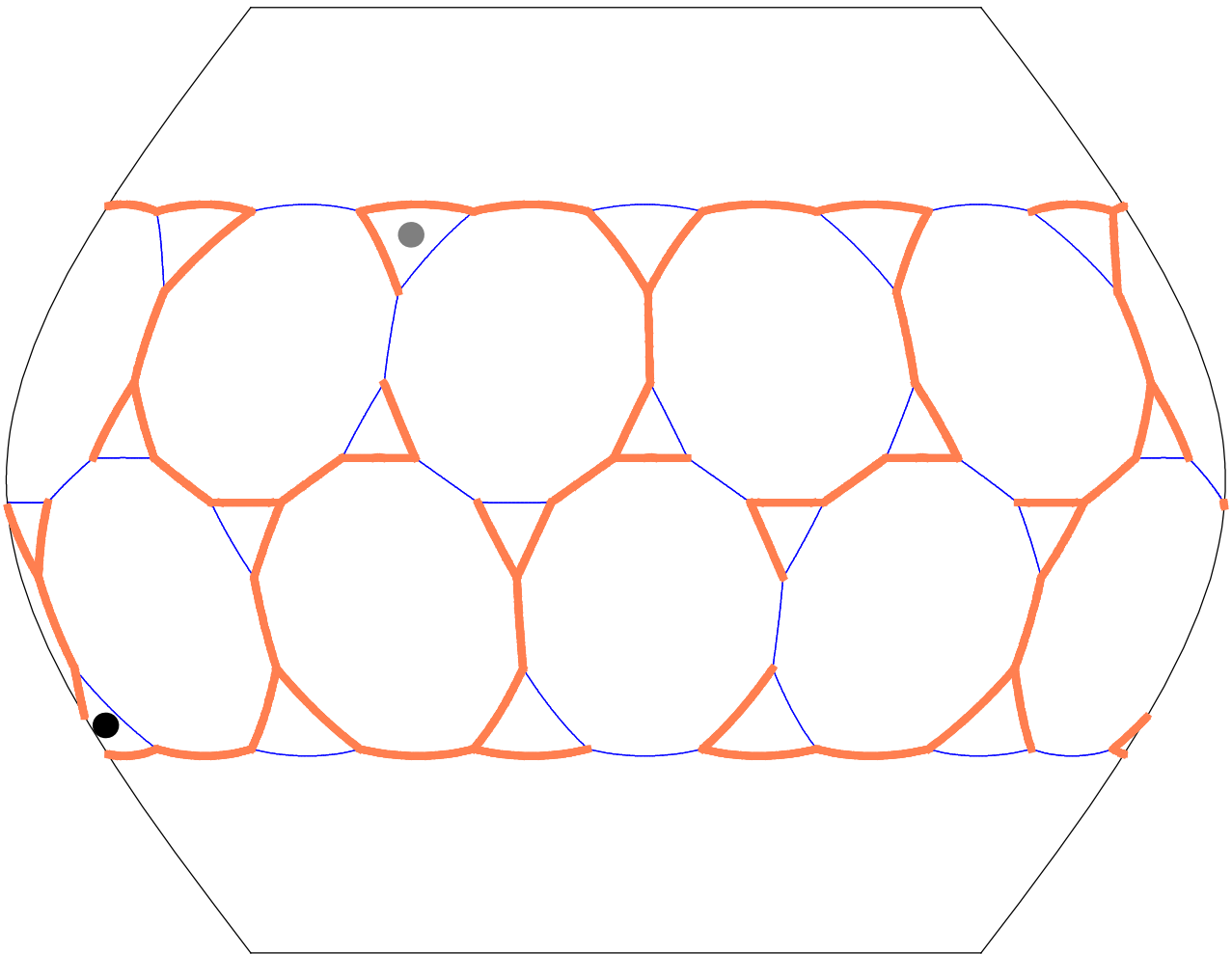
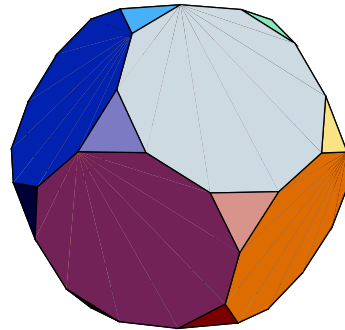
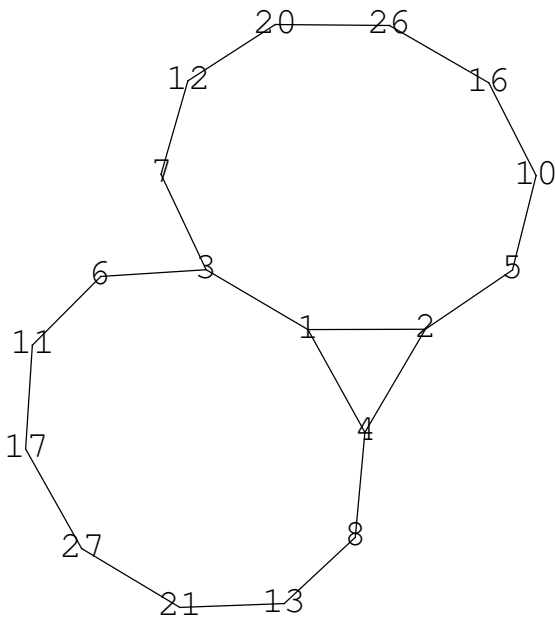
{6, 6, 5}



26.

truncated dodecahedron

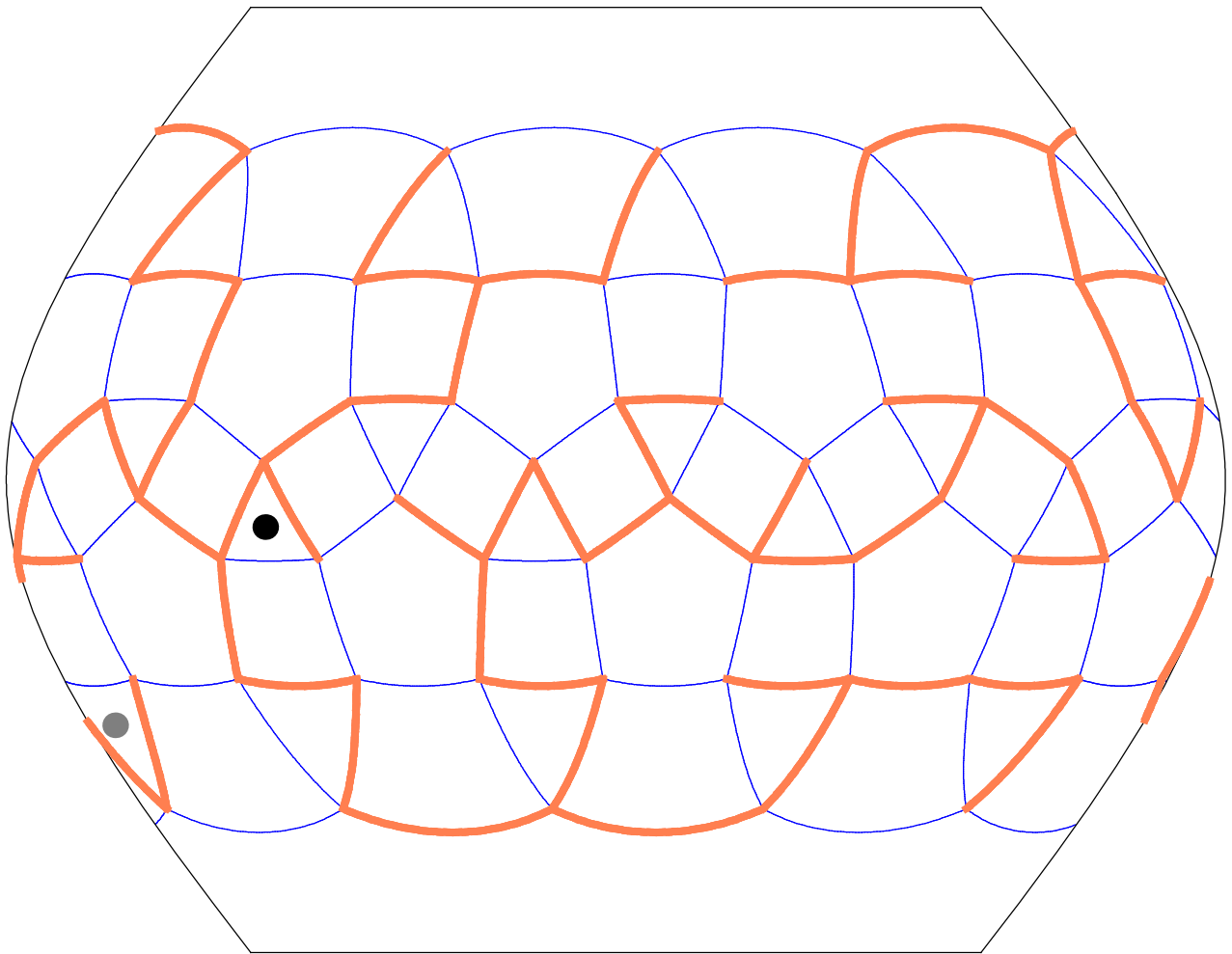
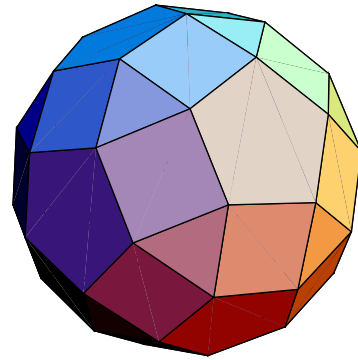
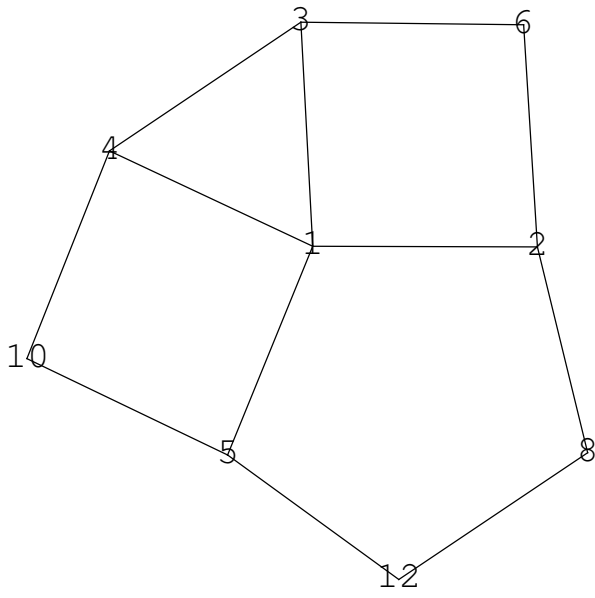
{10, 10, 3}



27.

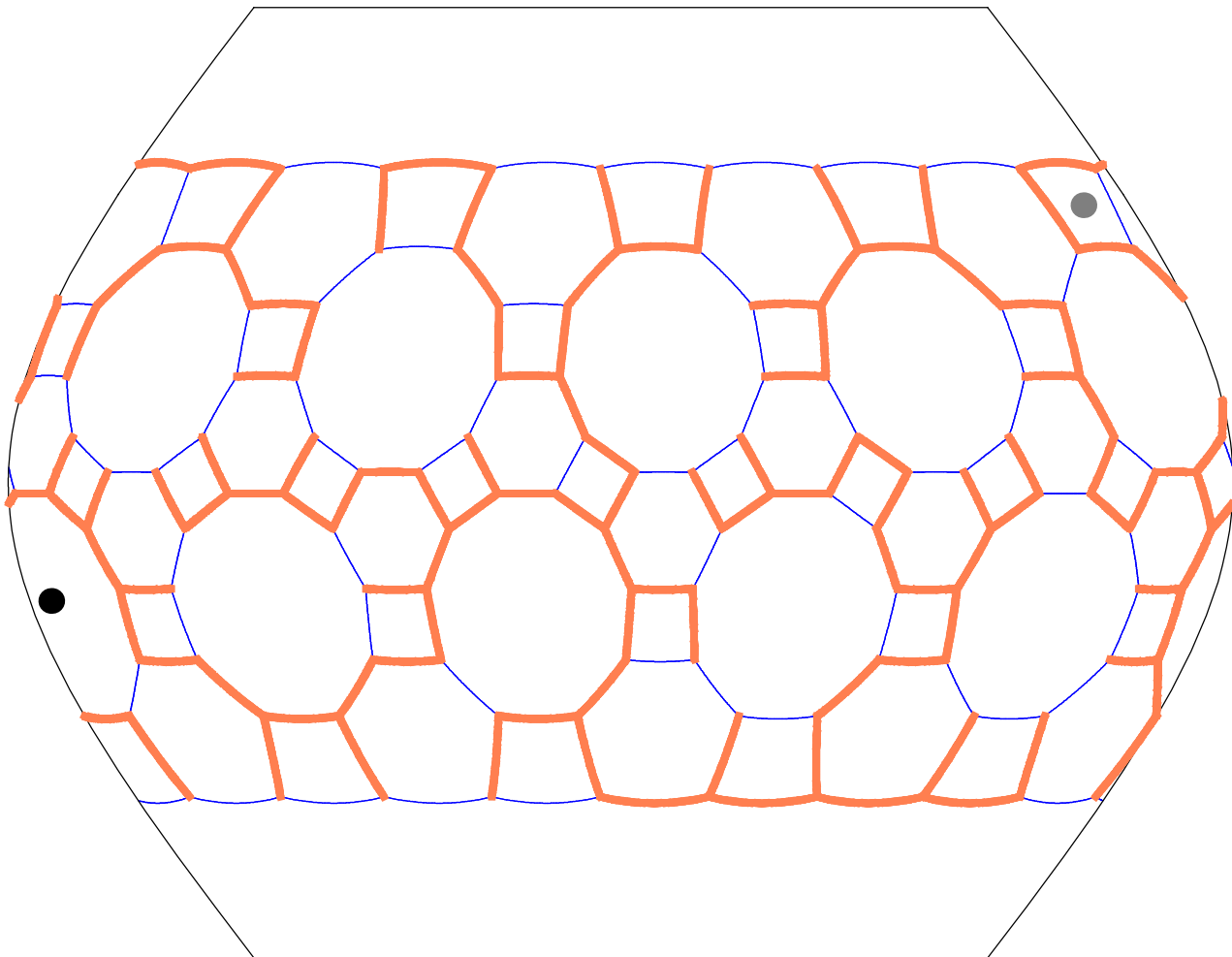
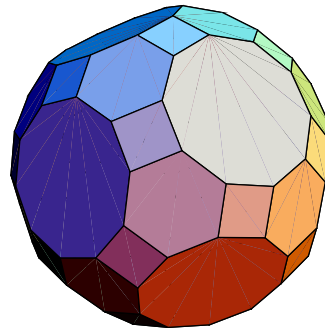
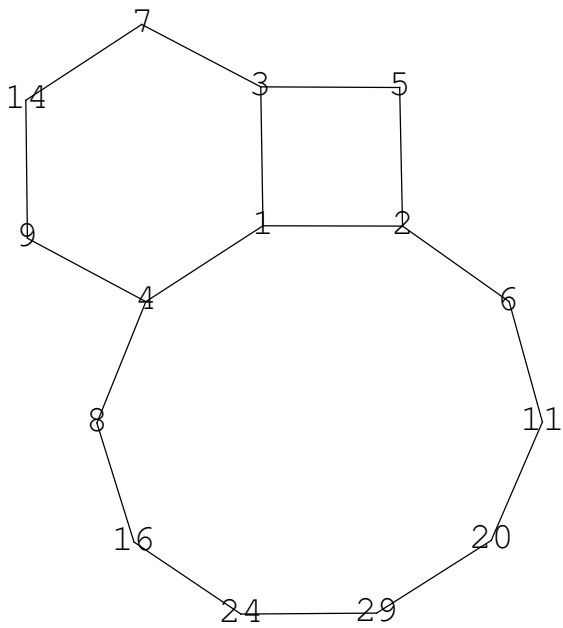
rhombicosidodecahedron

{4, 3, 4, 5}



28.

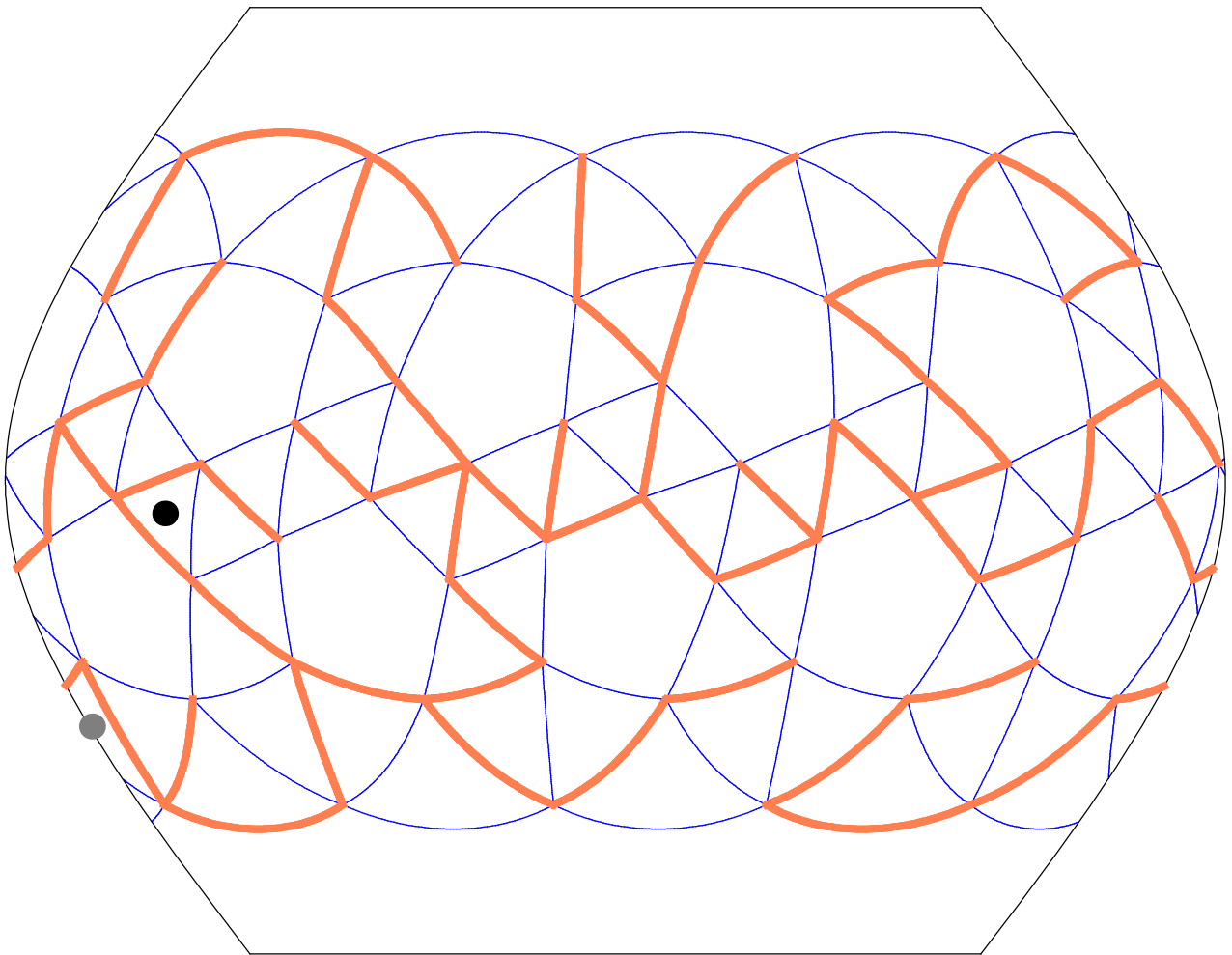
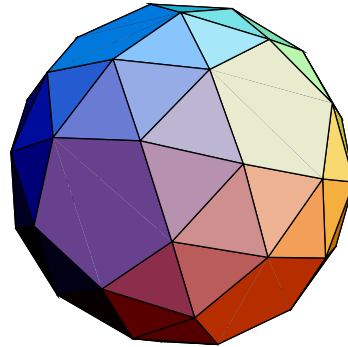
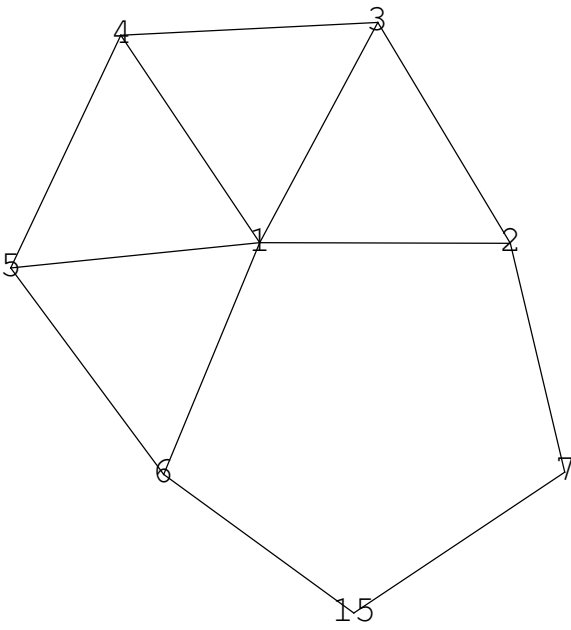
truncated icosidodecahedron

 $\{4, 6, 10\}$ 

29.

snub dodecahedron

{3, 3, 3, 3, 5}

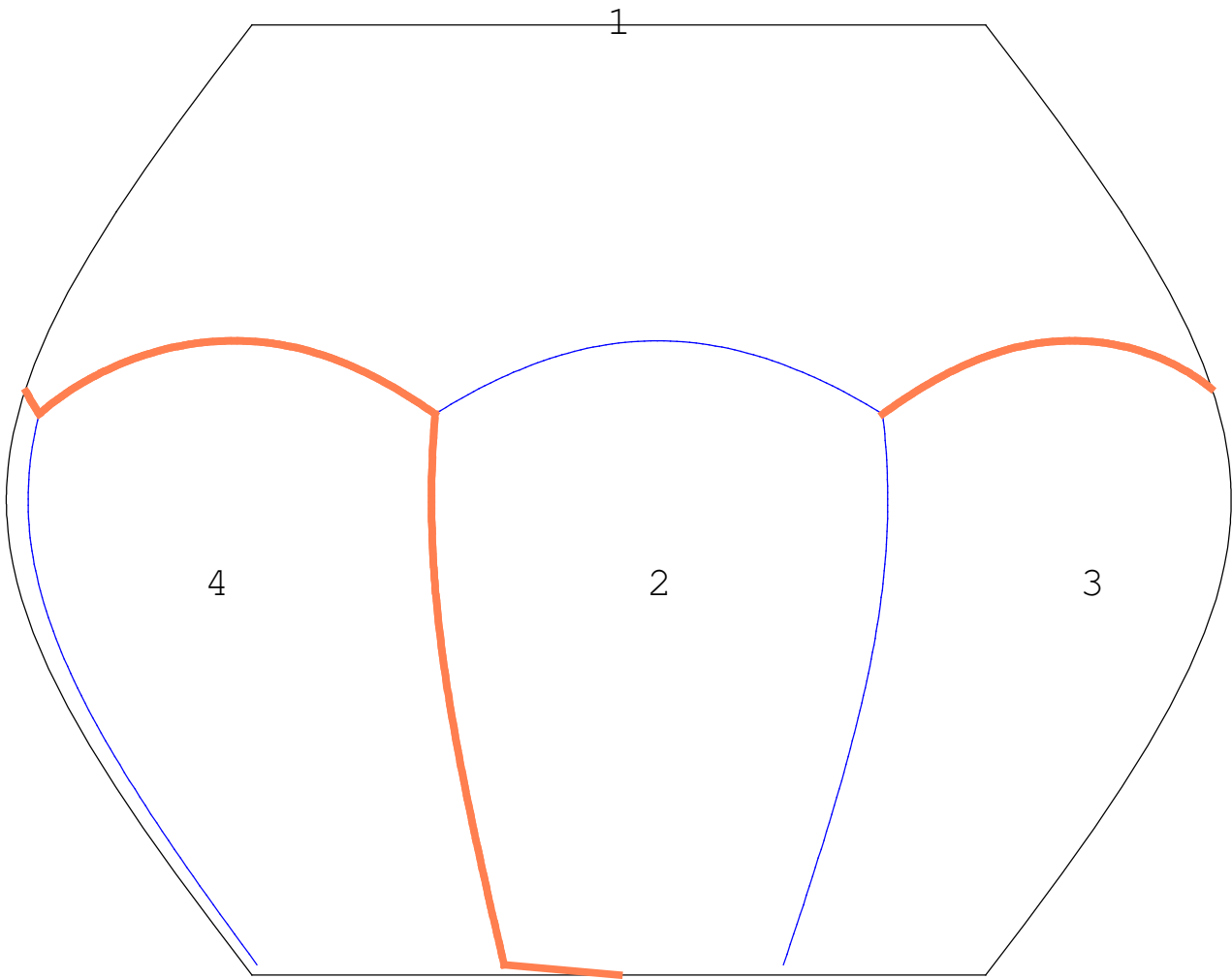
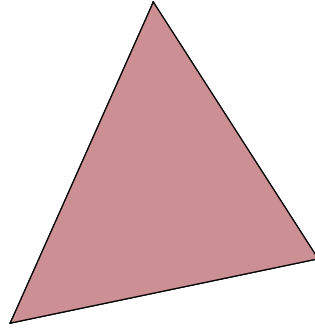
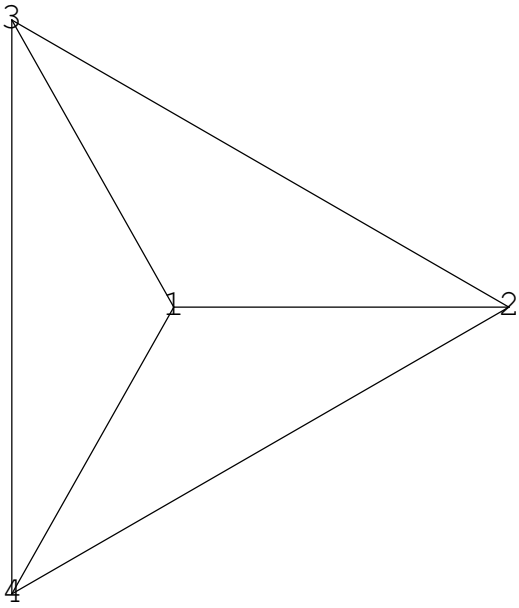


Solutions

1.

tetrahedron

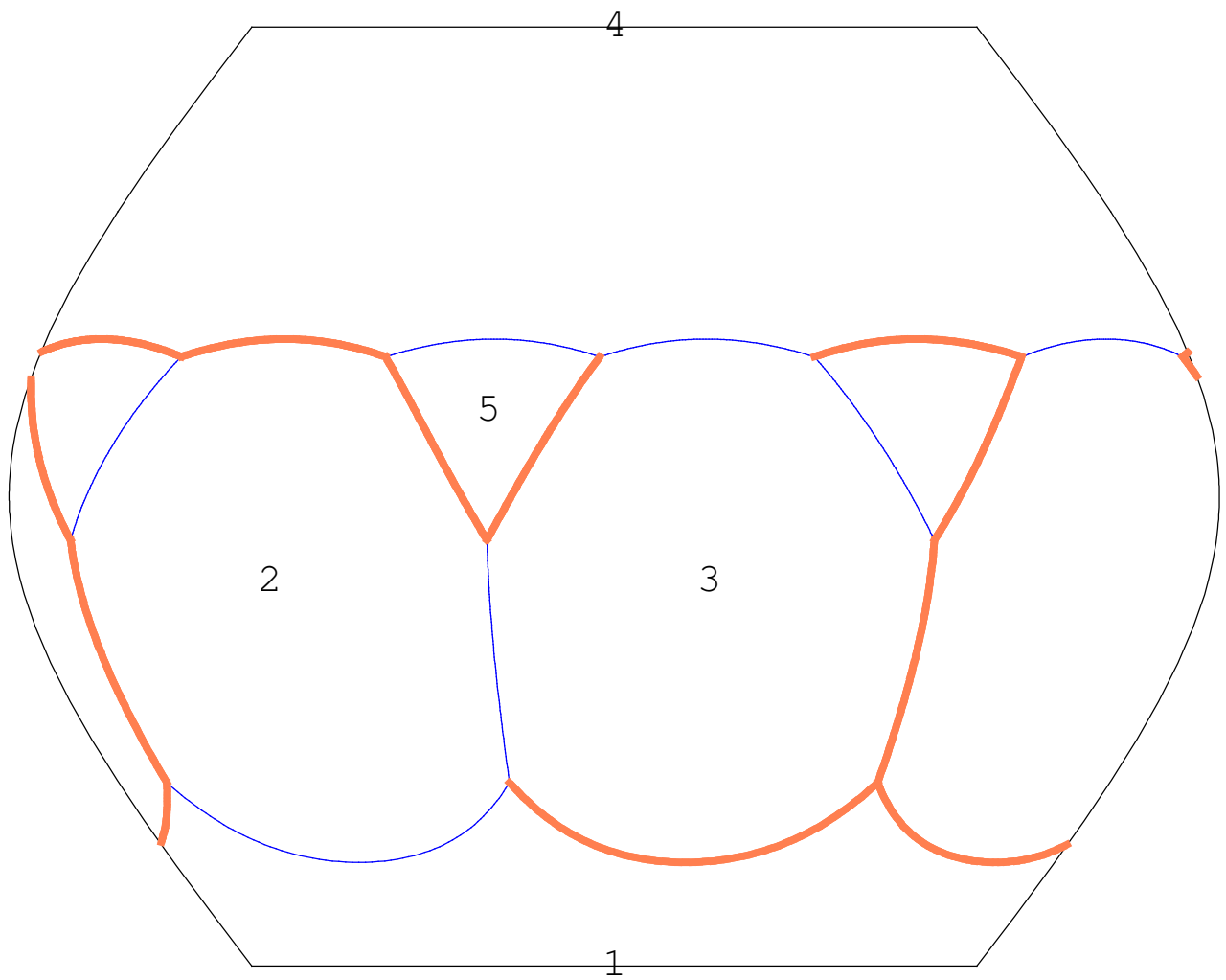
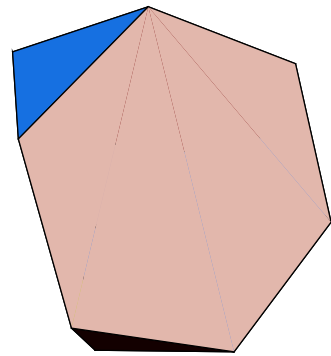
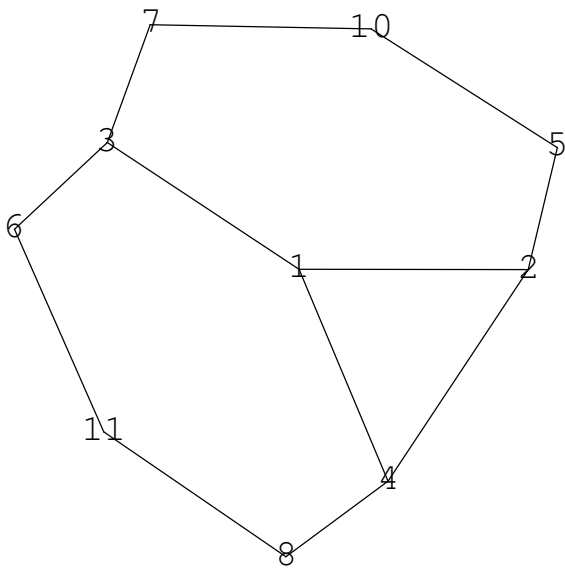
{3, 3, 3}



2.

truncated tetrahedron

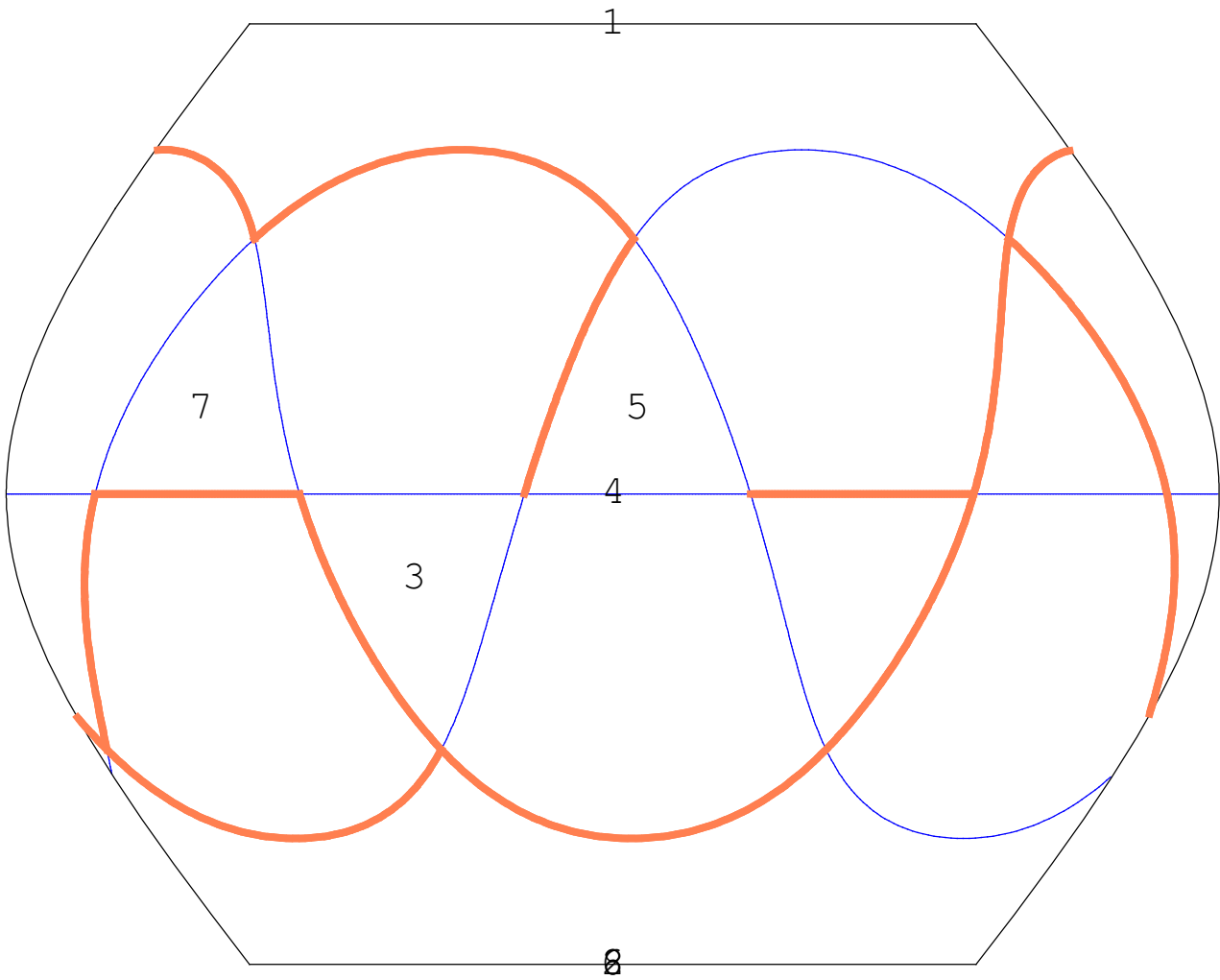
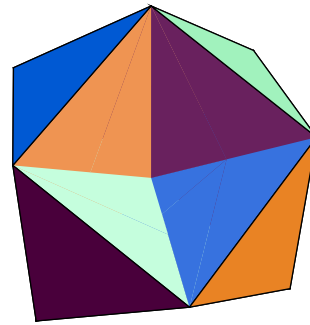
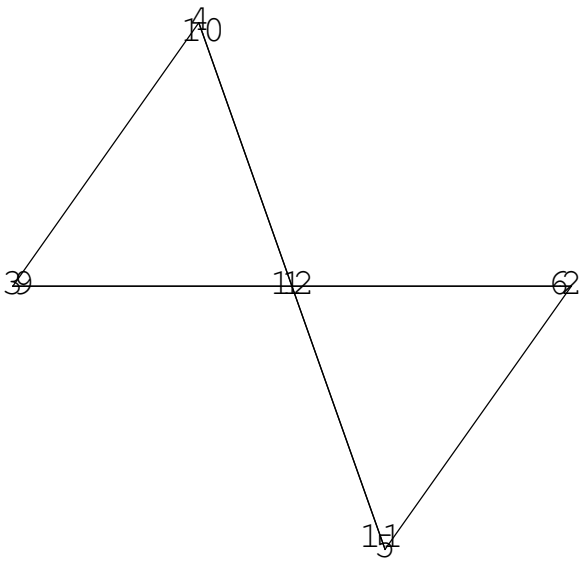
{6, 6, 3}



3.

octahemioctahedron

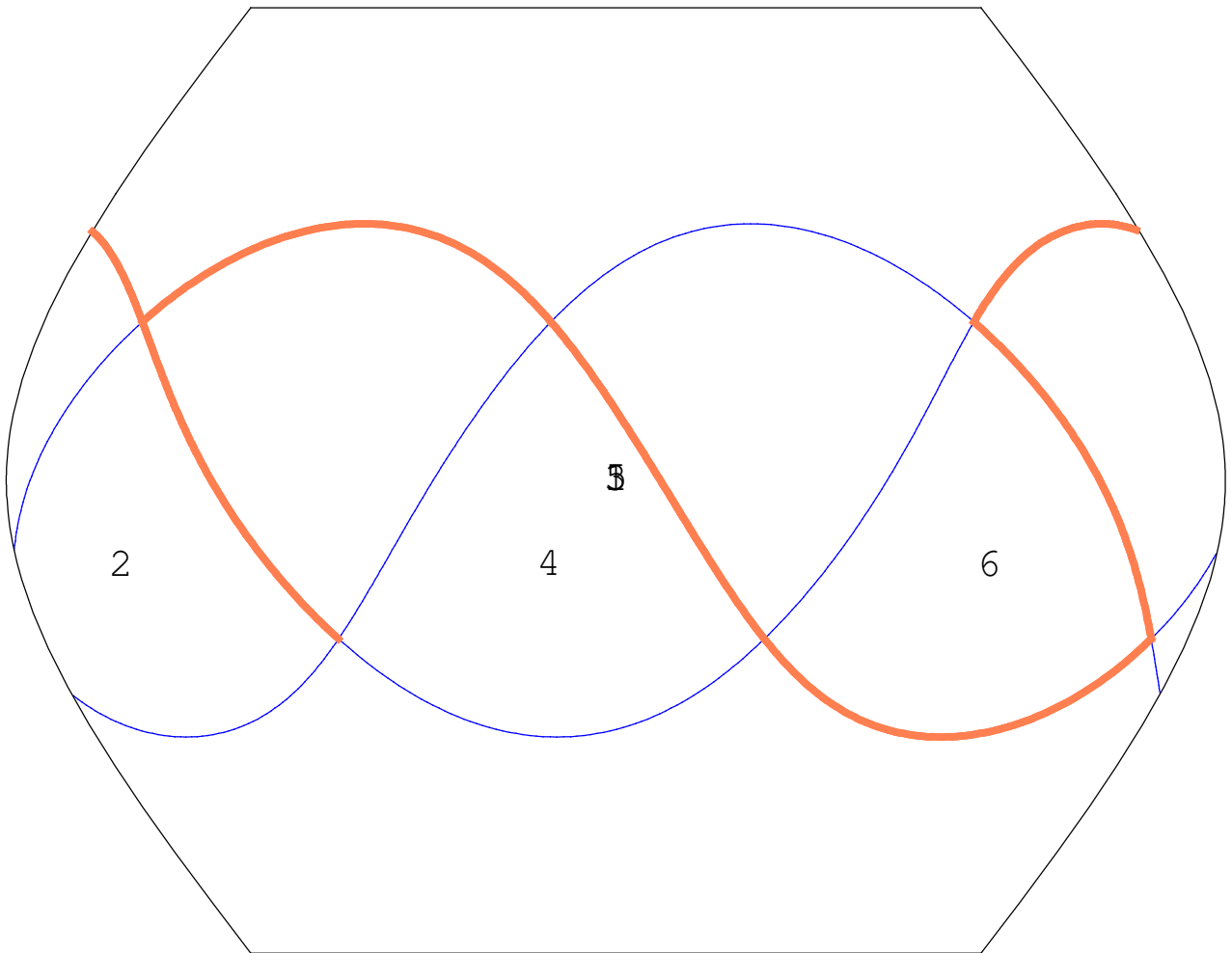
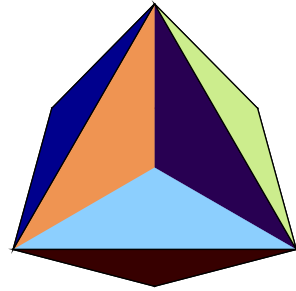
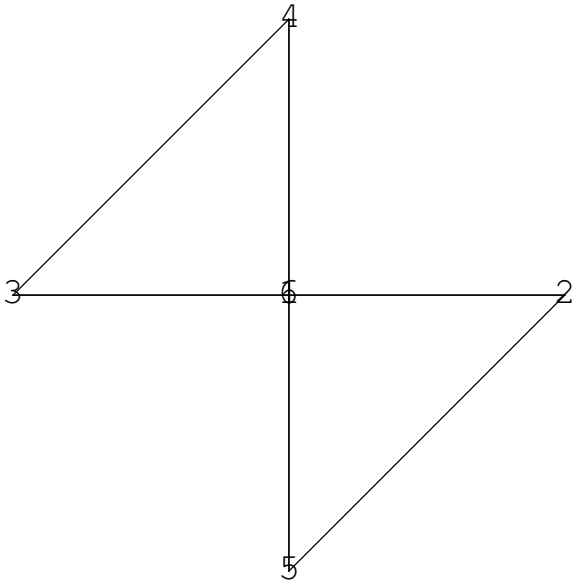
$$\{6, \frac{3}{2}, 6, 3\}$$



4.

tetrahemihexahedron

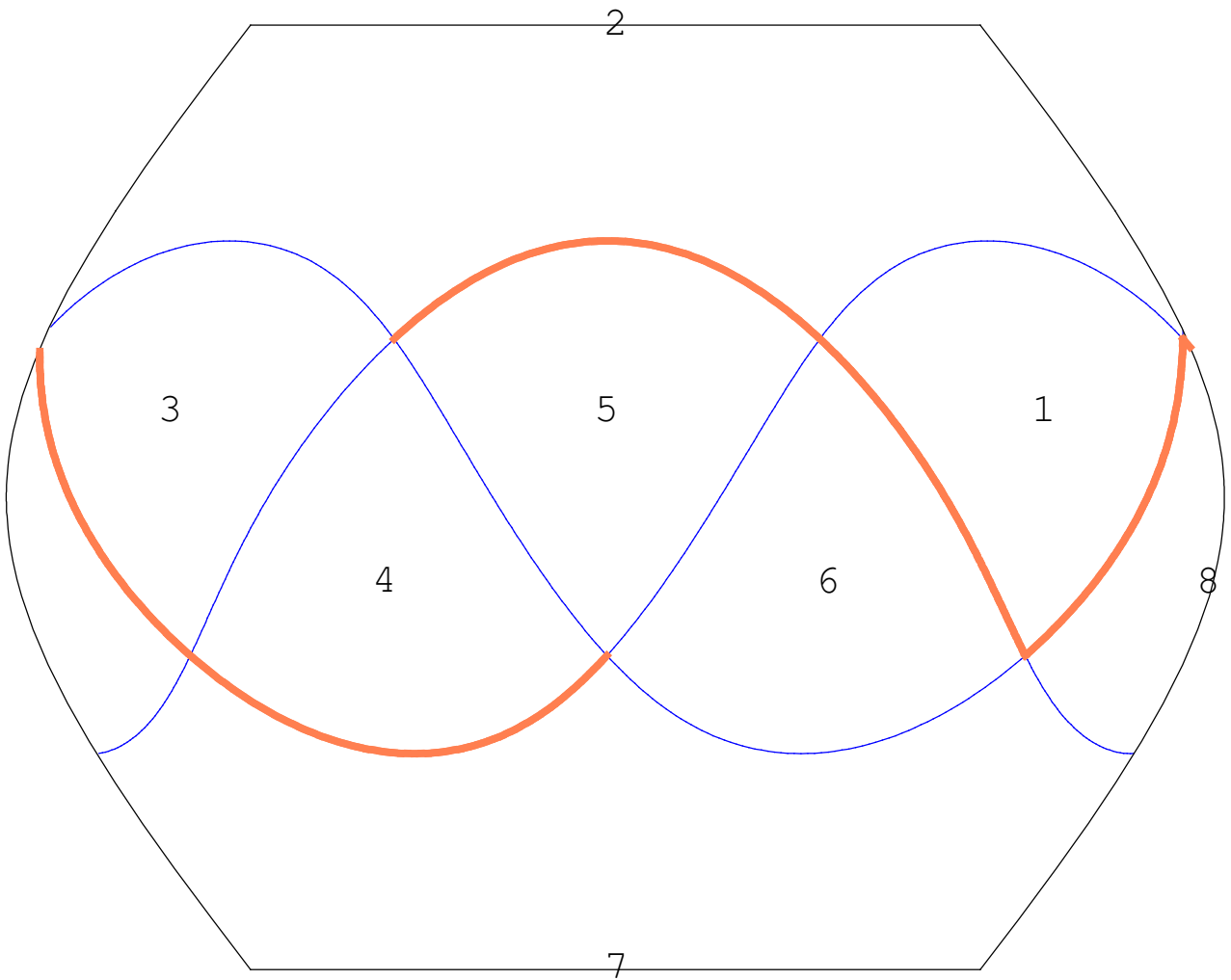
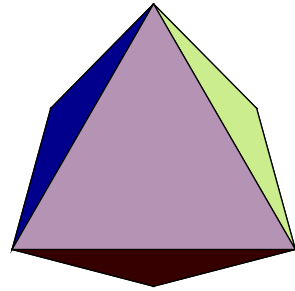
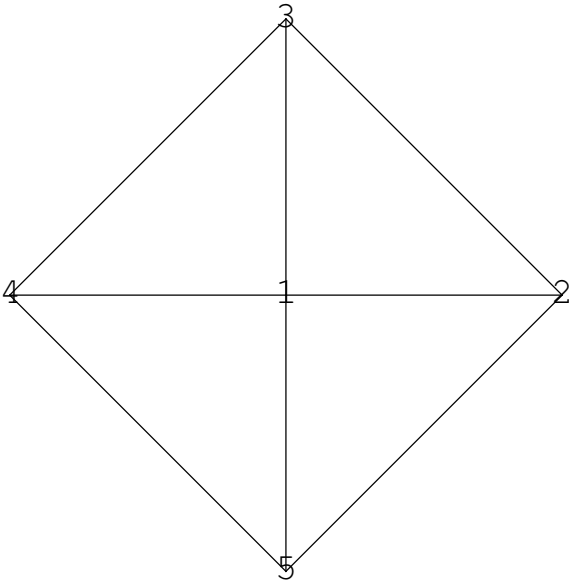
$$\{4, \frac{3}{2}, 4, 3\}$$



5.

octahedron

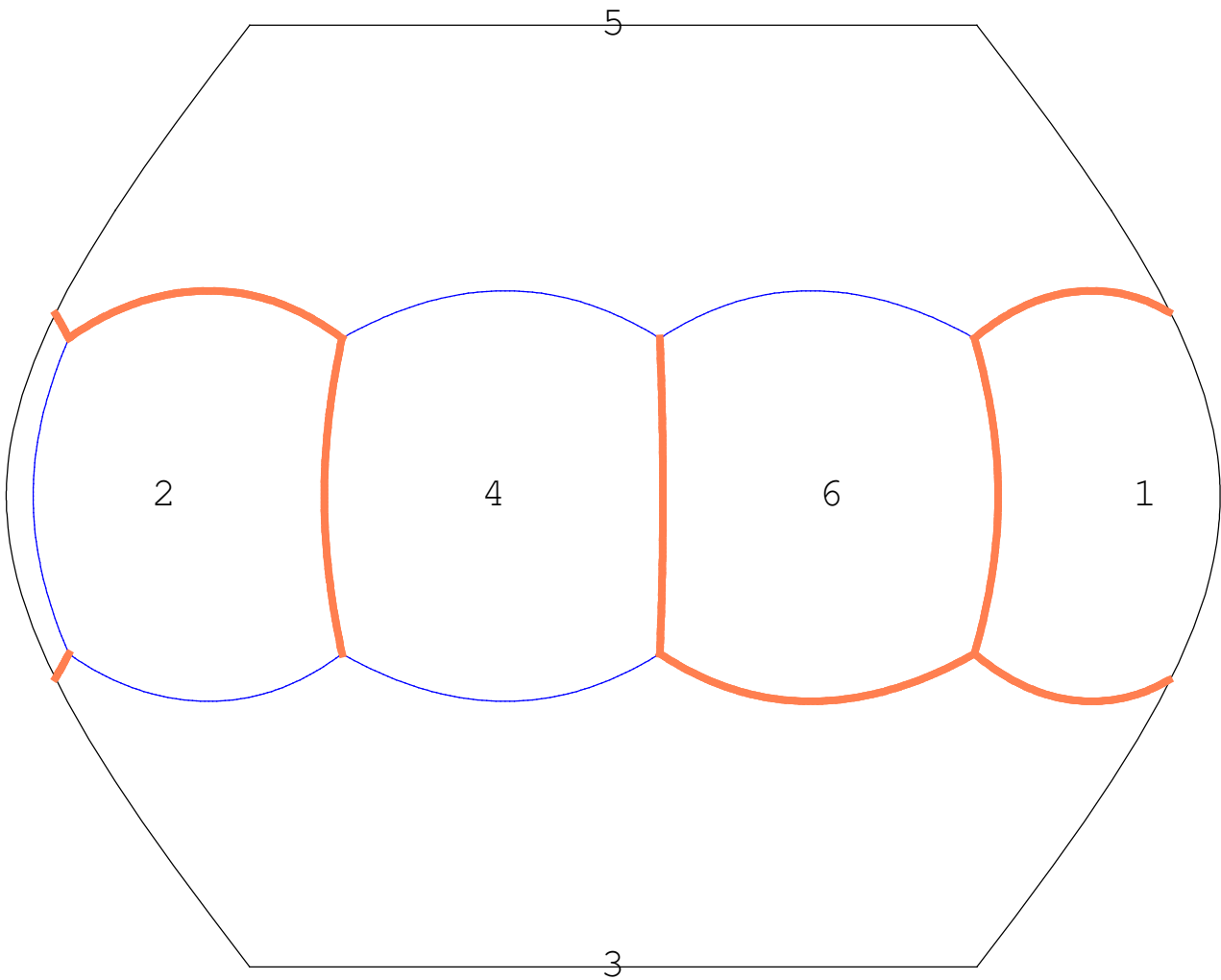
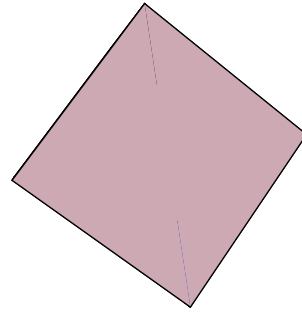
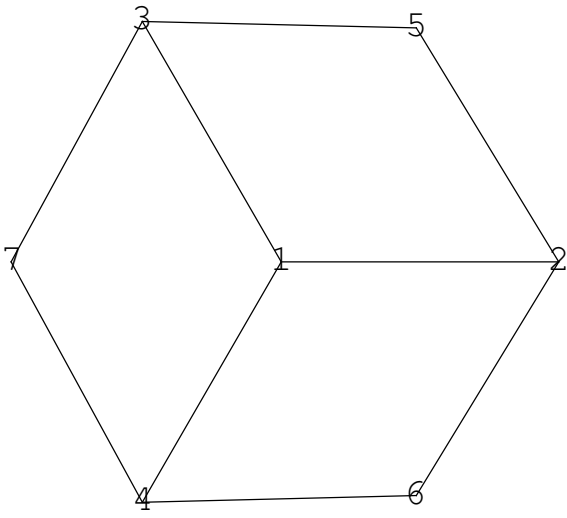
{3, 3, 3, 3}



6.

cube

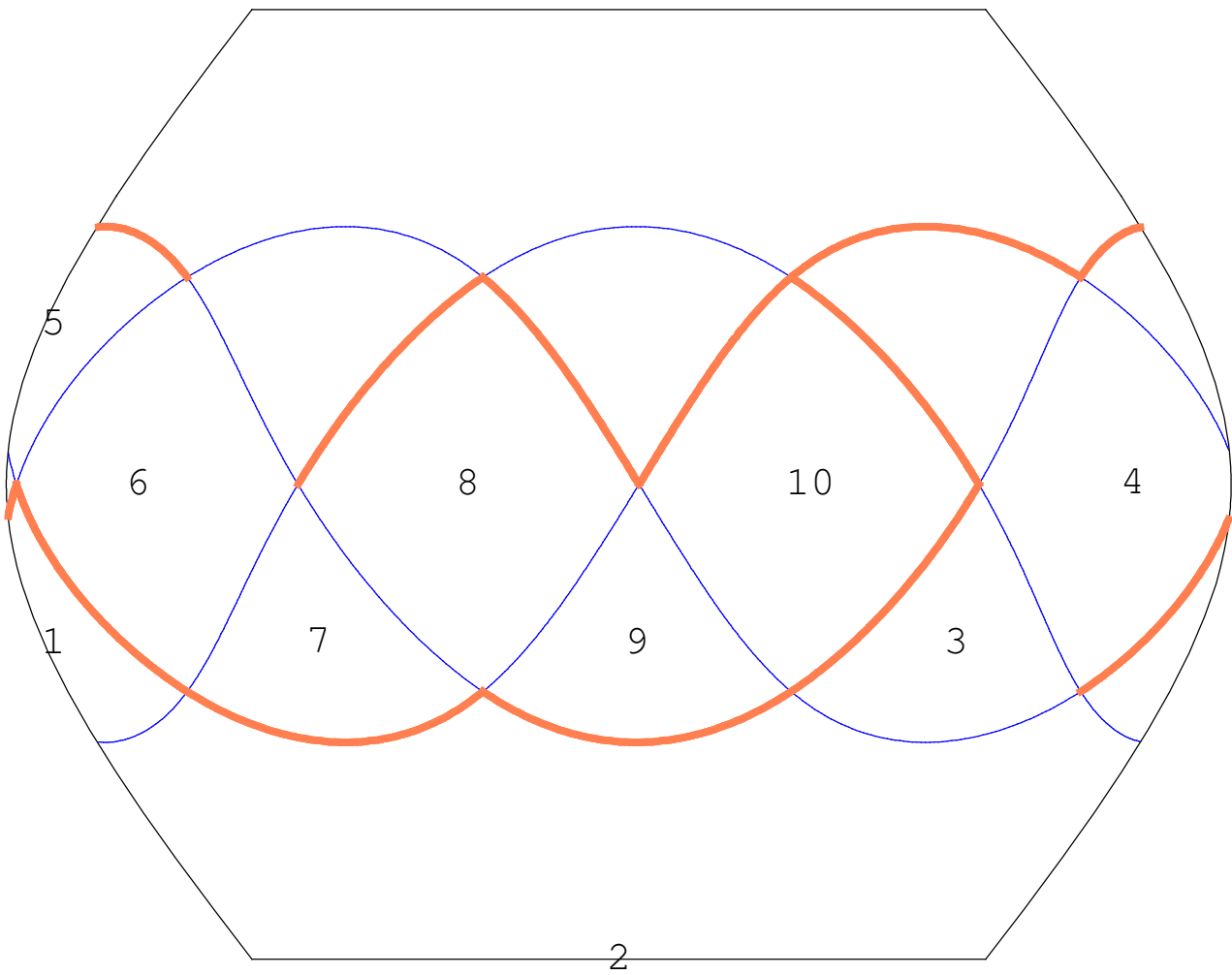
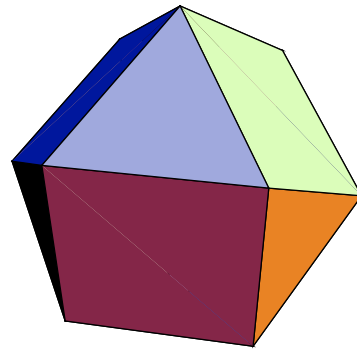
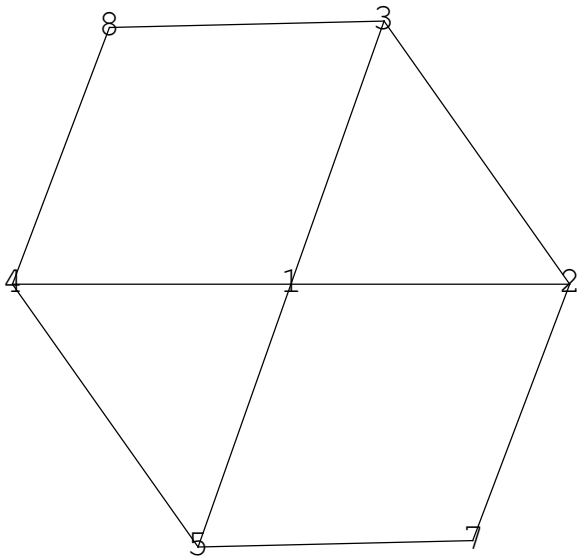
{4, 4, 4}



7.

cuboctahedron

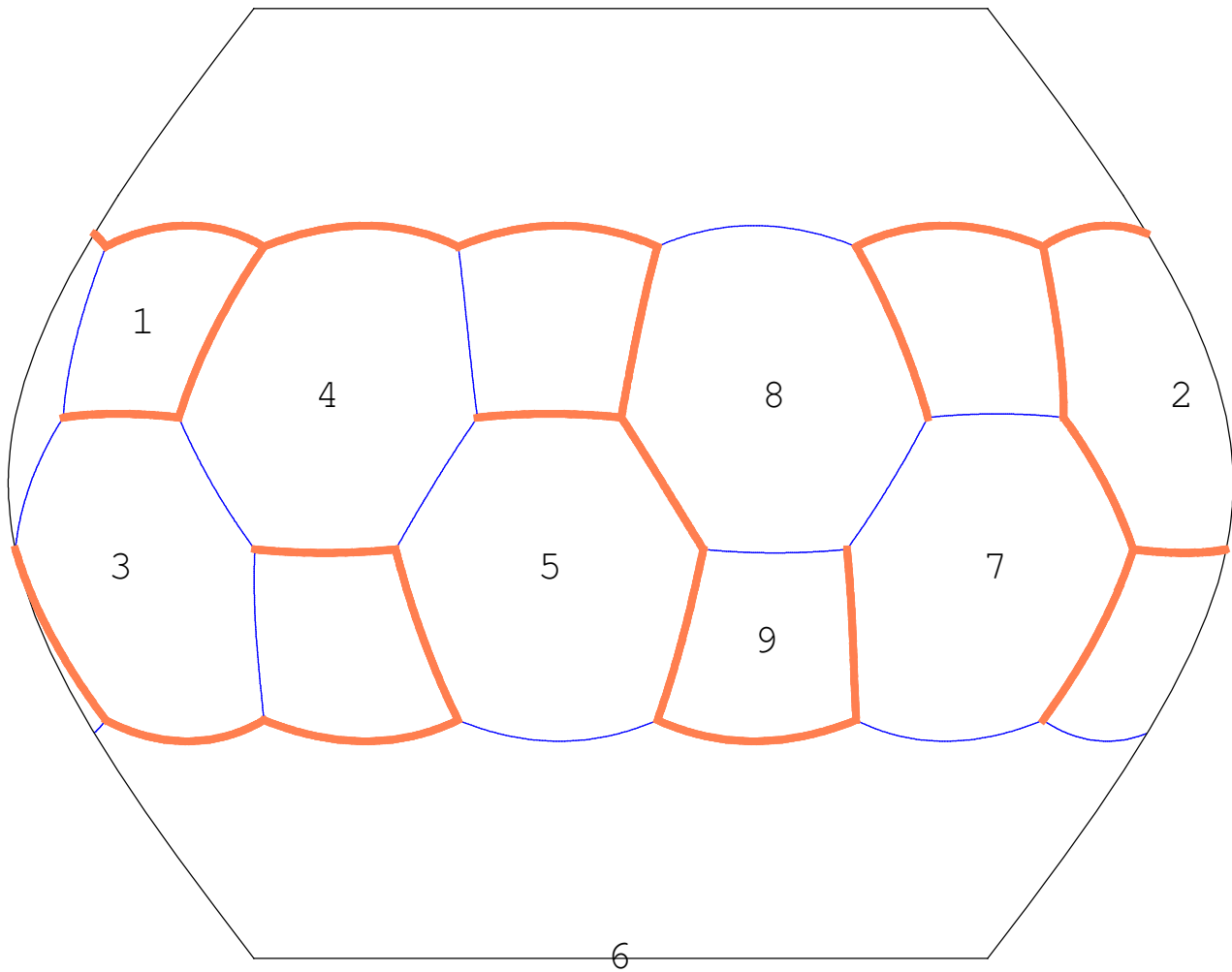
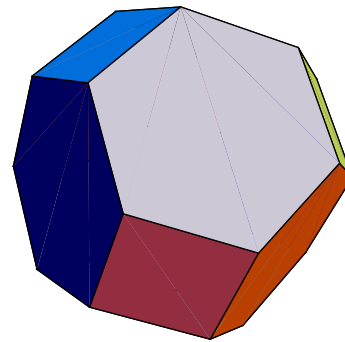
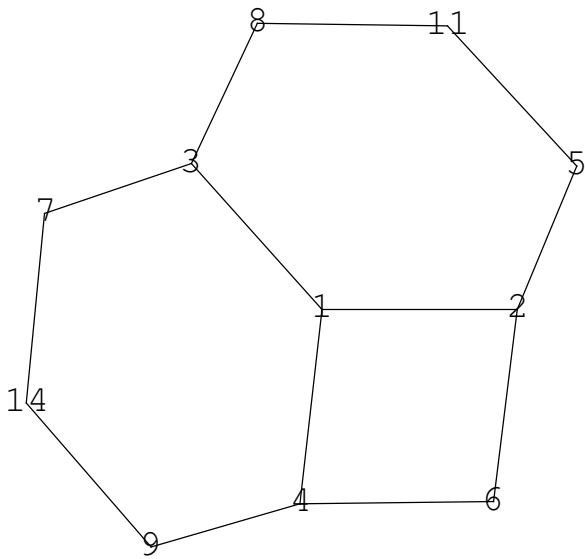
{3, 4, 3, 4}



8.

truncated octahedron

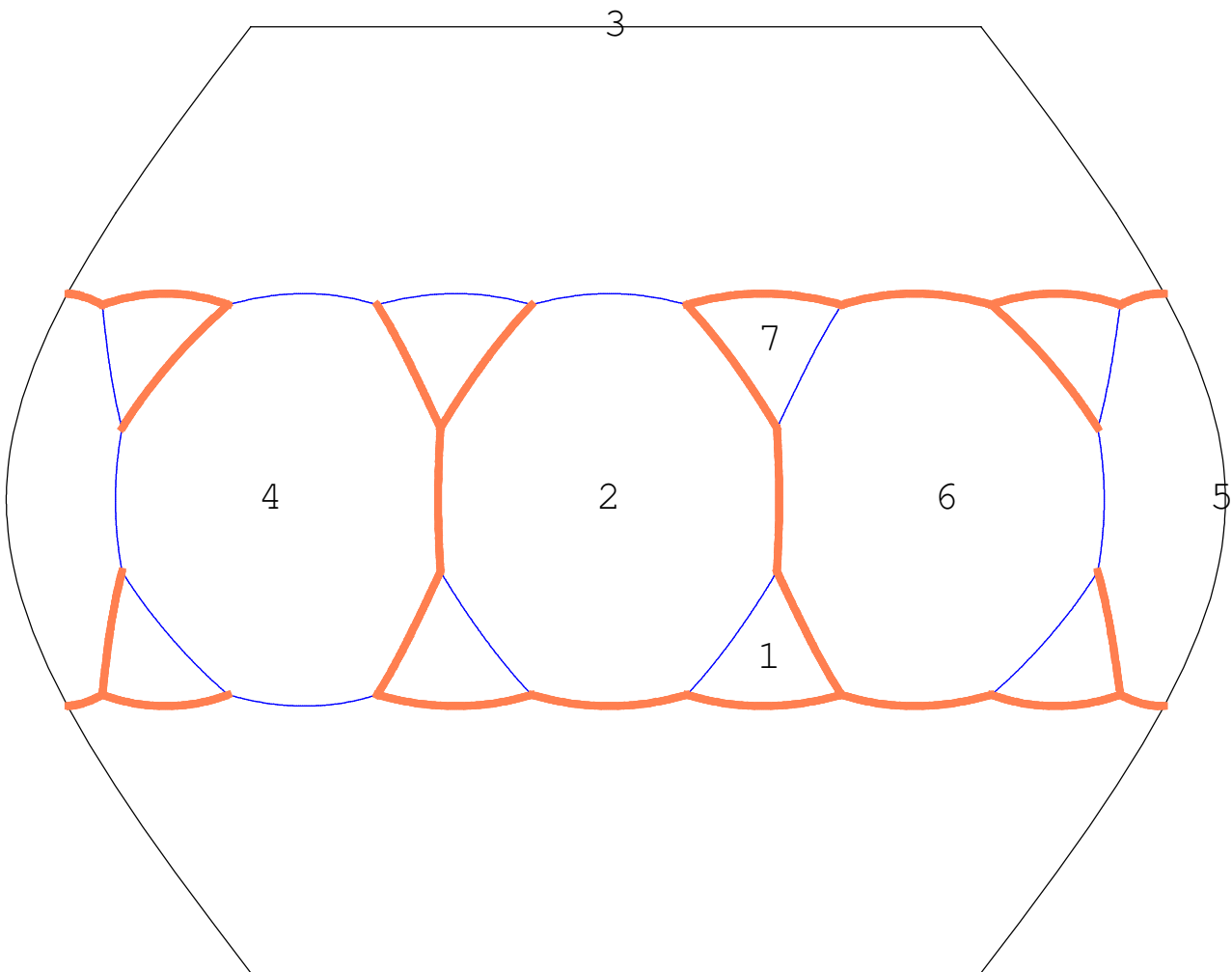
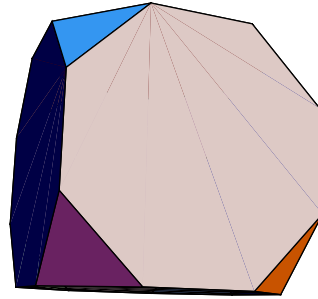
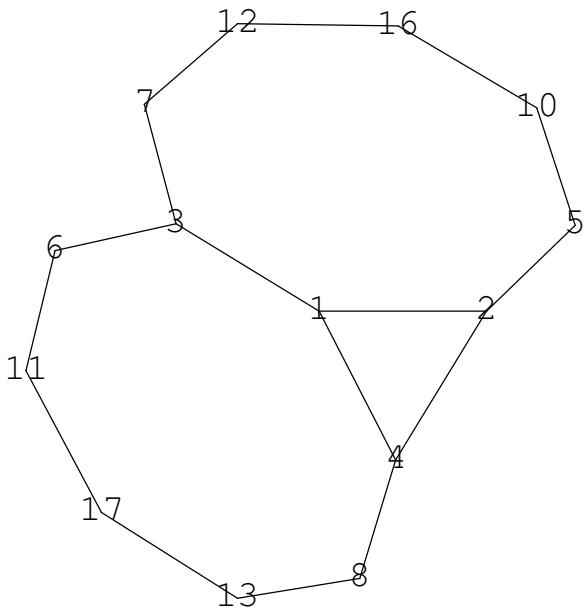
{6, 6, 4}



9.

truncated cube

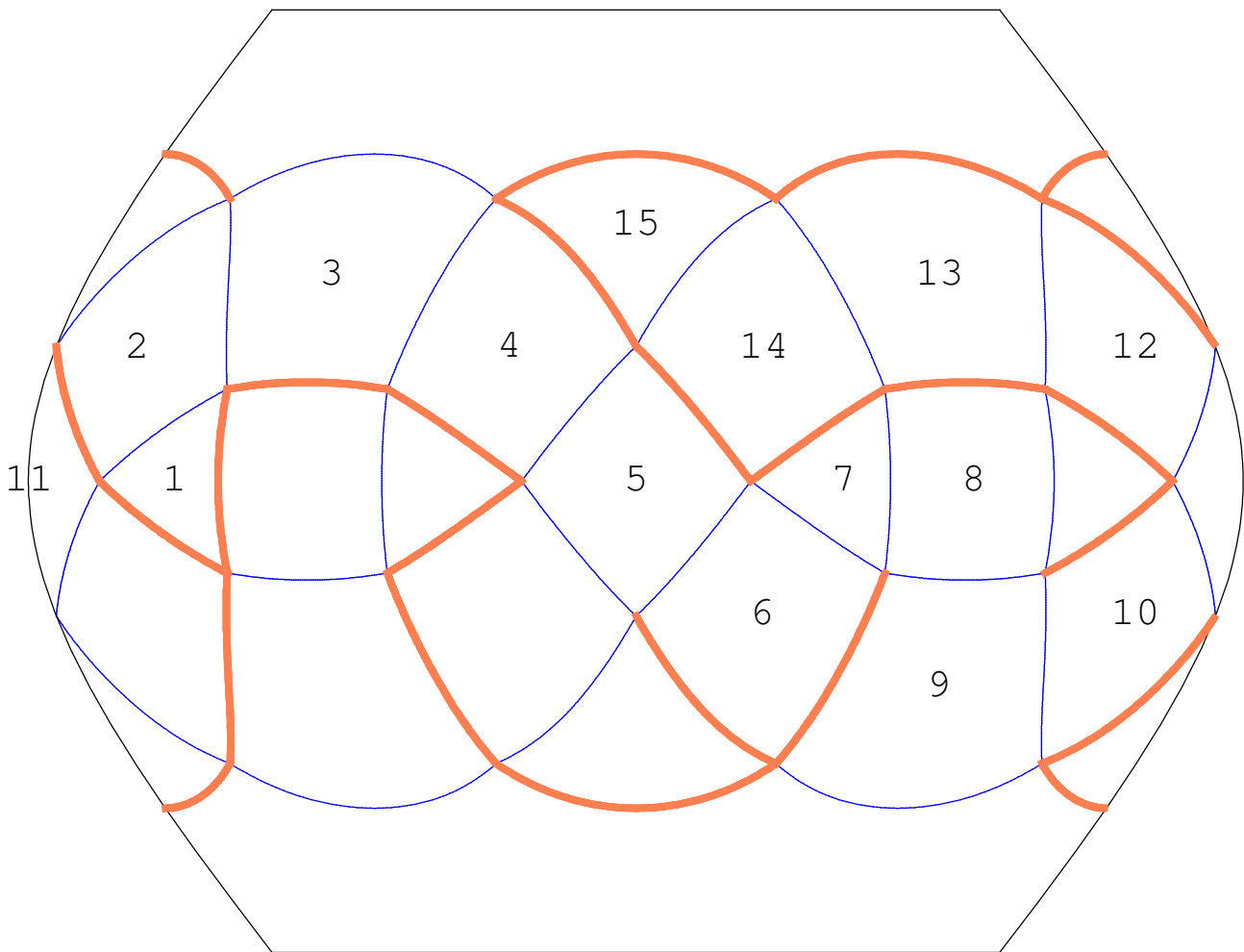
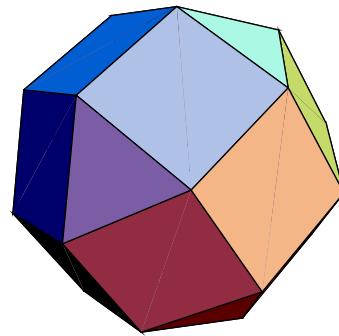
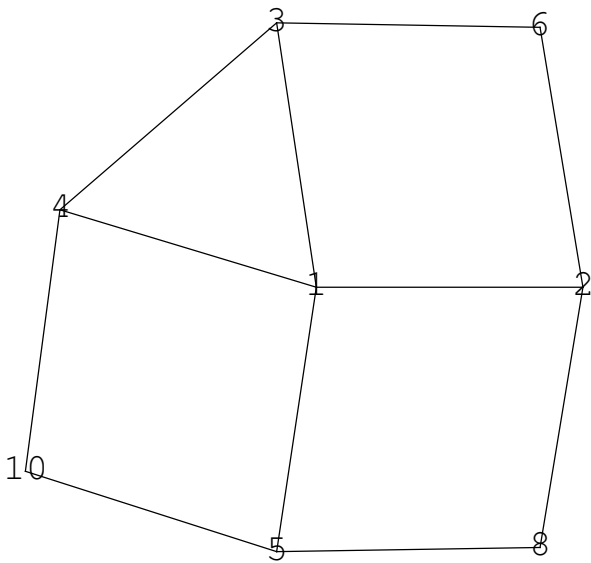
{8, 8, 3}



10.

rhombicuboctahedron

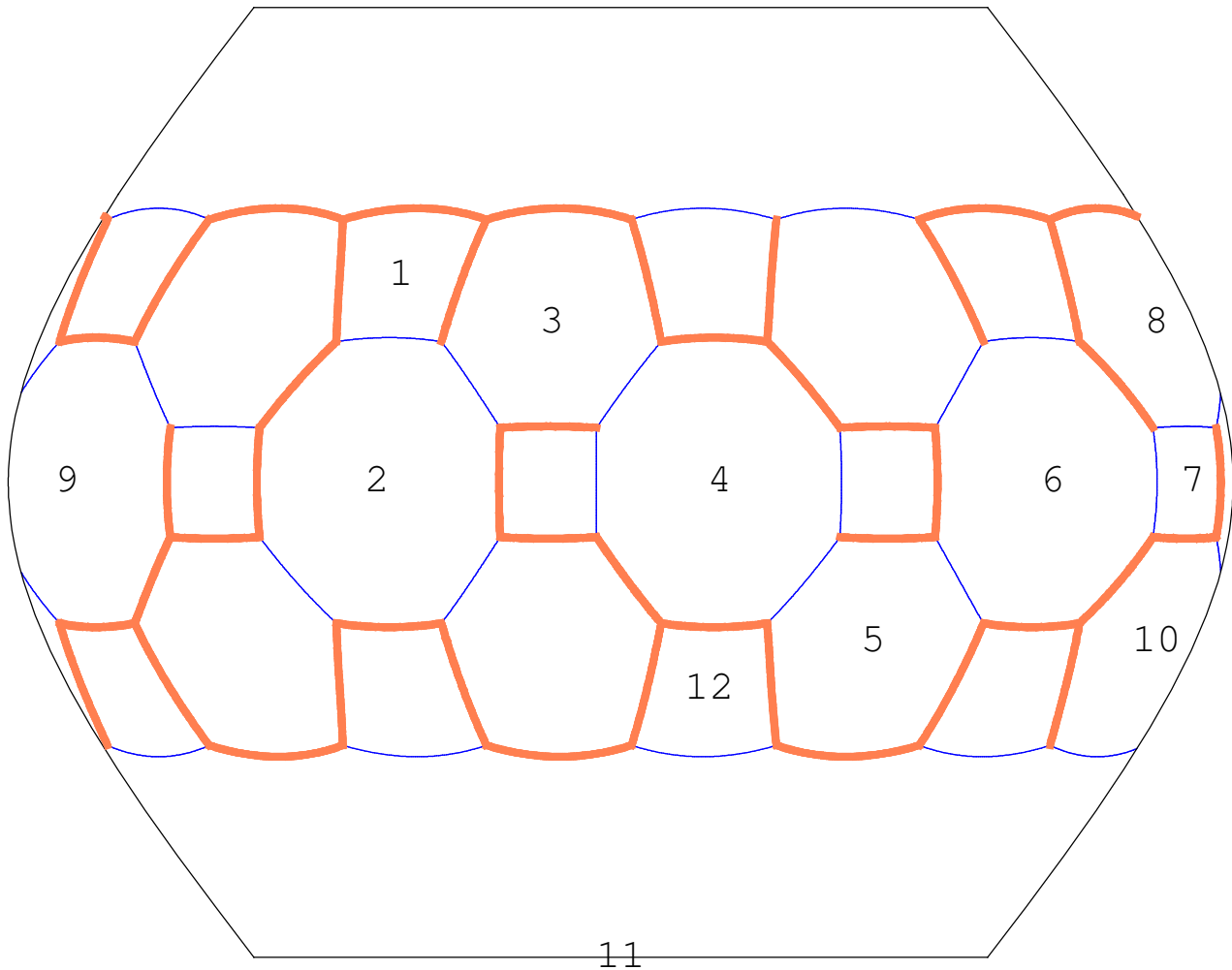
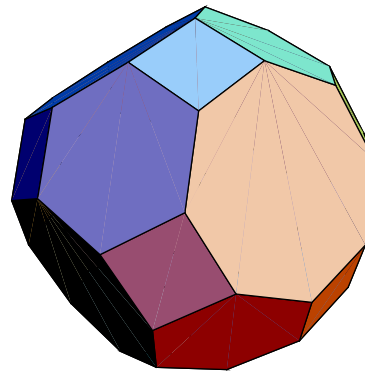
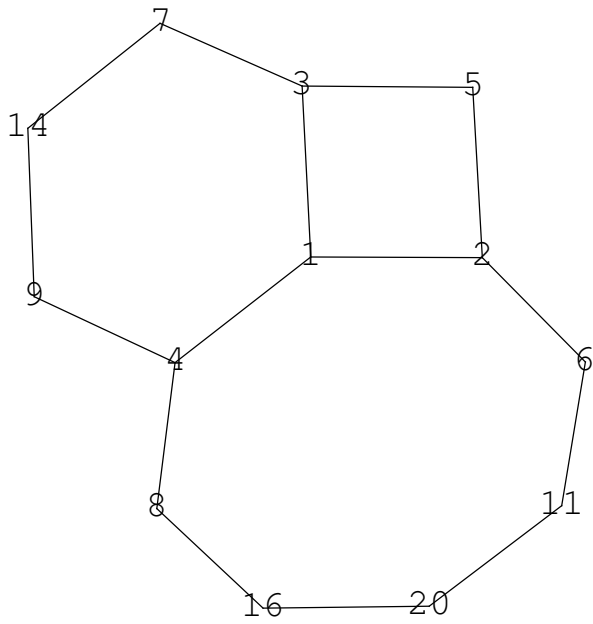
{4, 3, 4, 4}



11.

truncated cuboctahedron

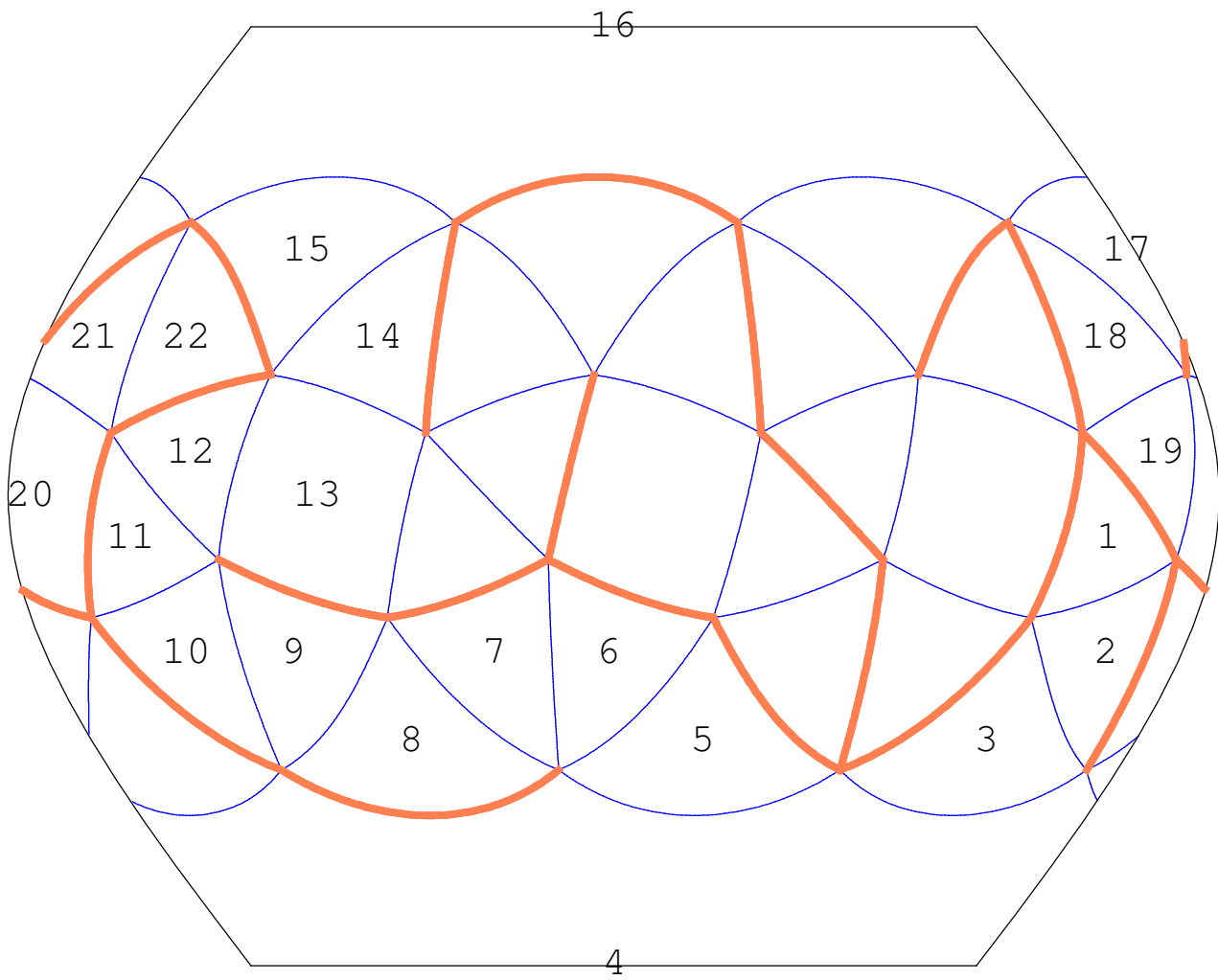
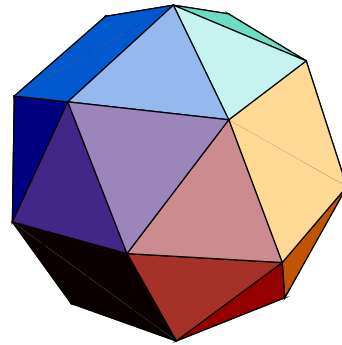
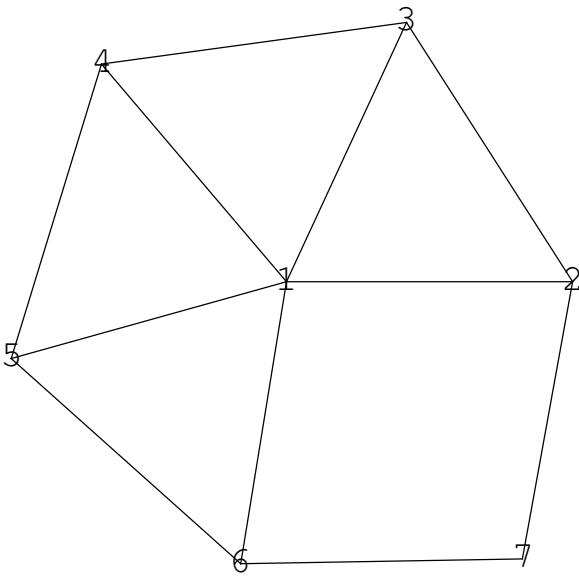
{4, 6, 8}



12.

snub cube

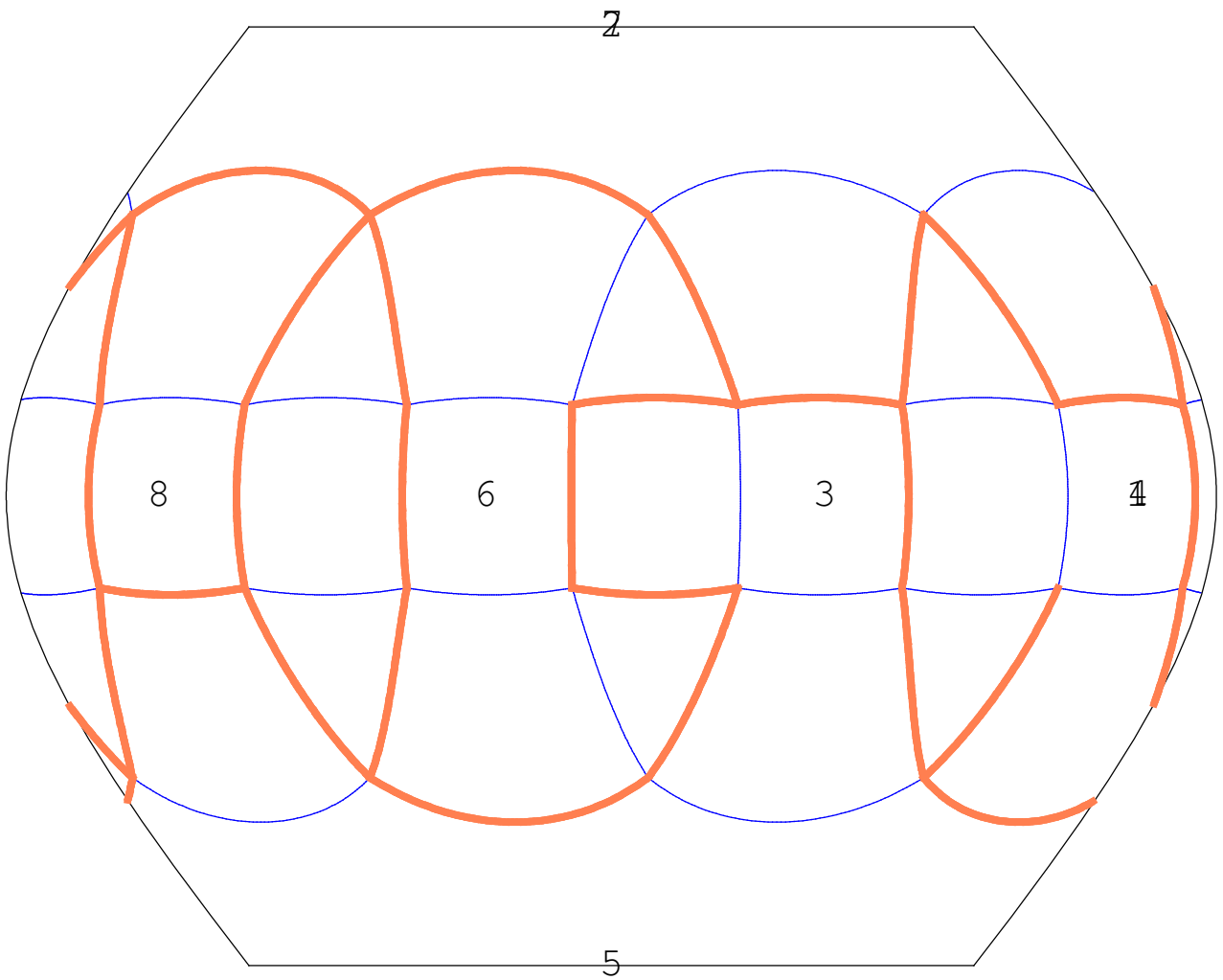
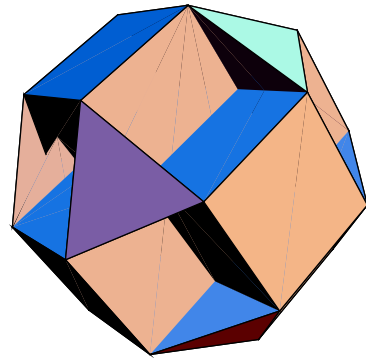
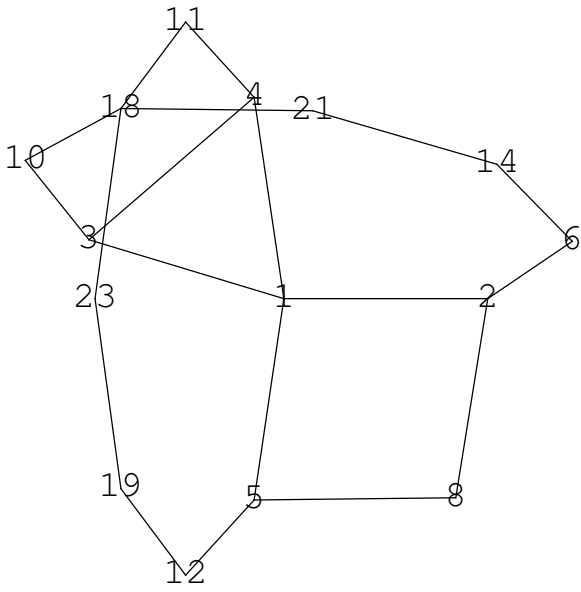
{3, 3, 3, 3, 4}



13.

small cubicuboctahedron

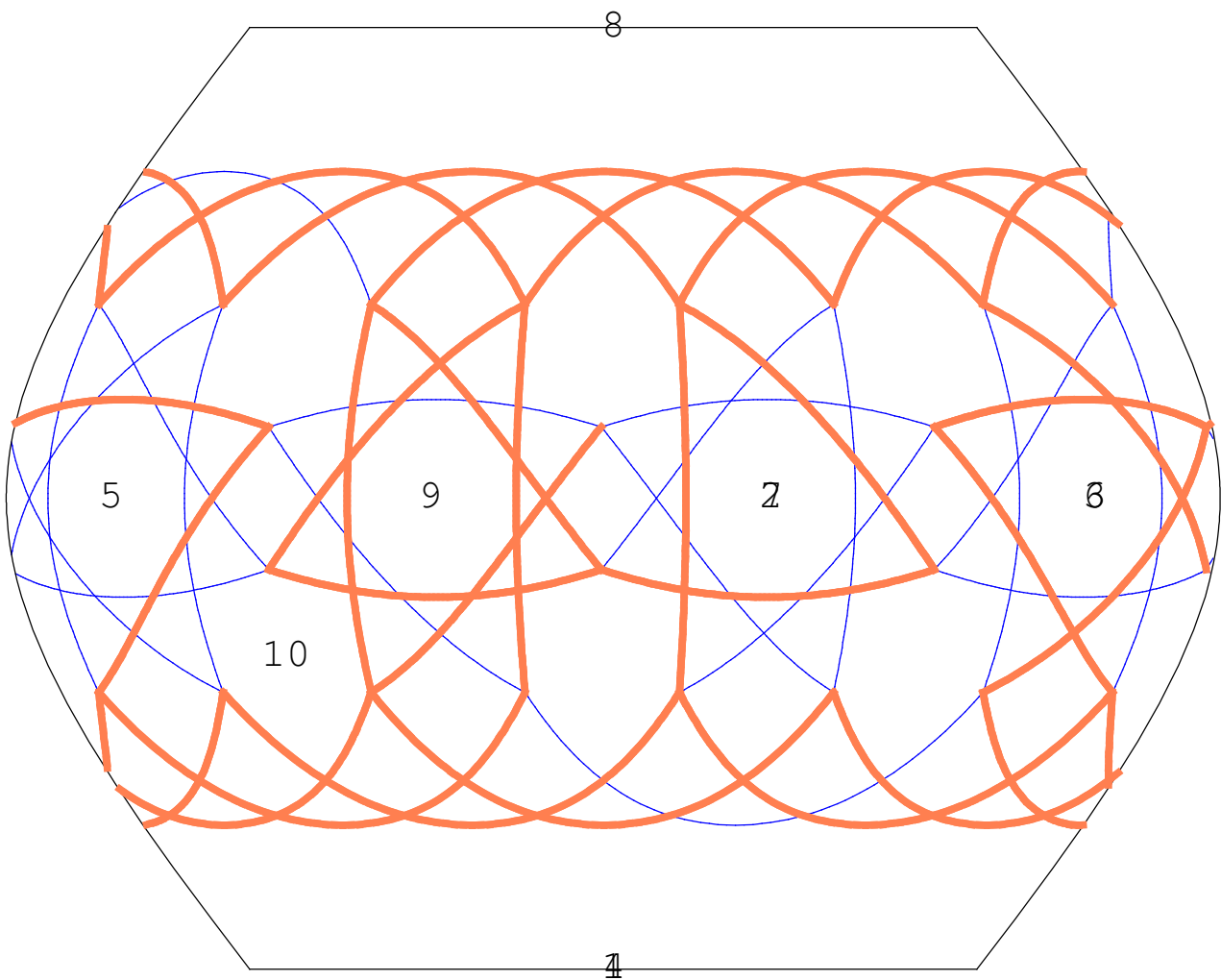
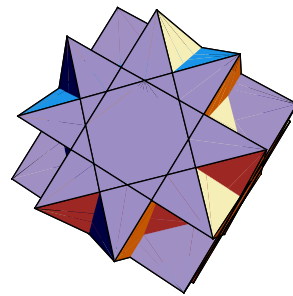
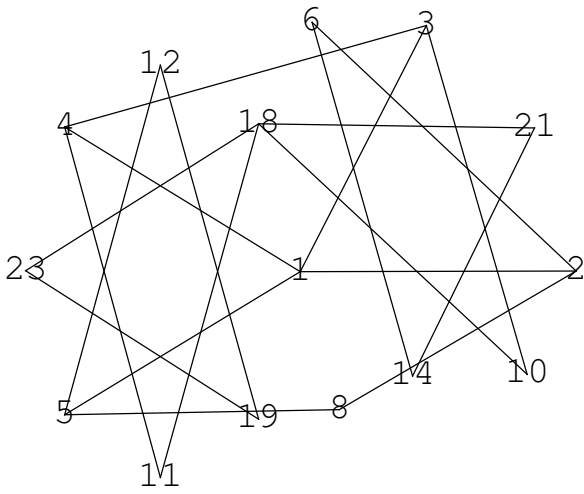
$$\{8, \frac{3}{2}, 8, 4\}$$



14.

great cubicuboctahedron

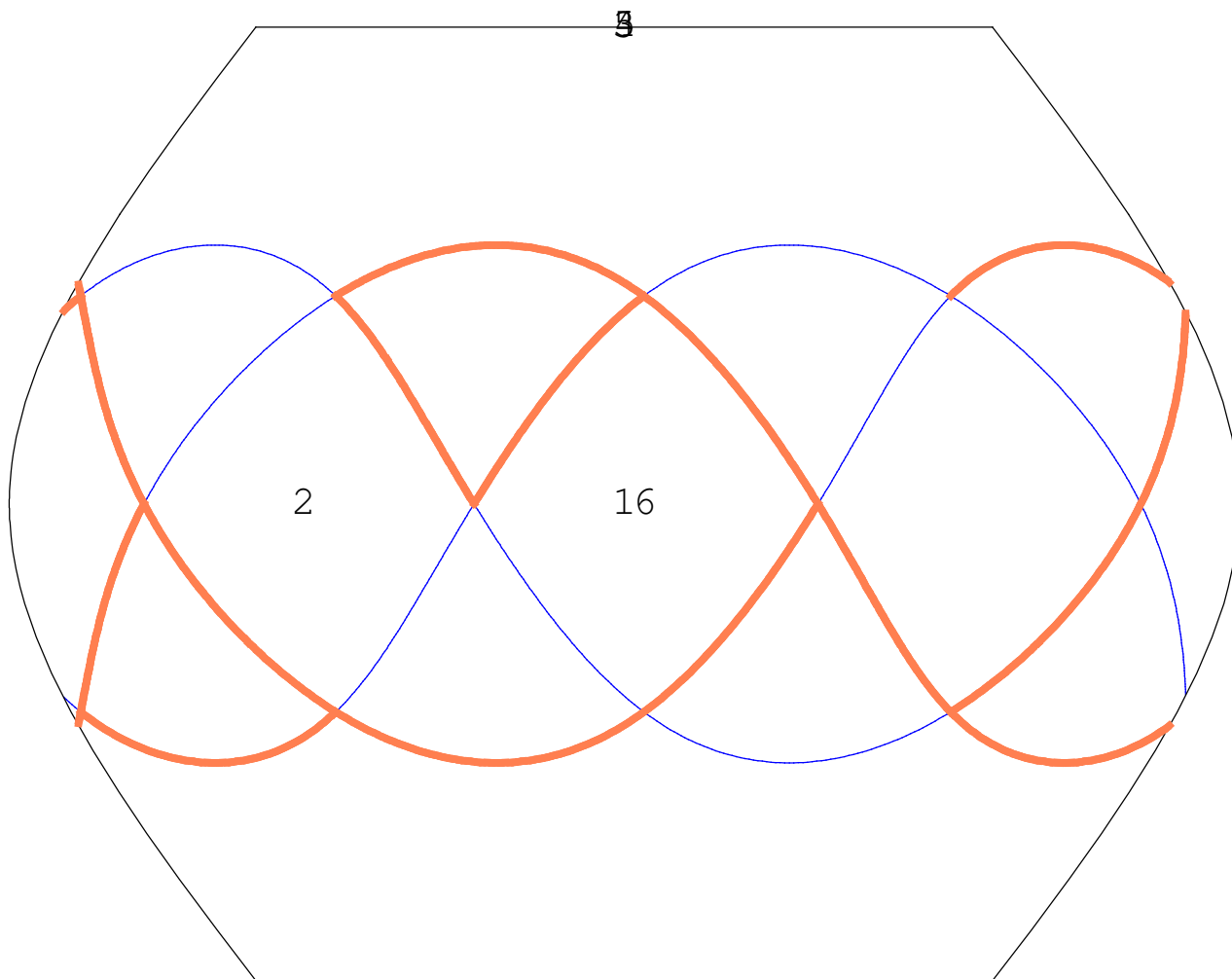
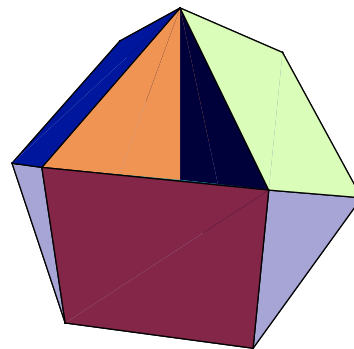
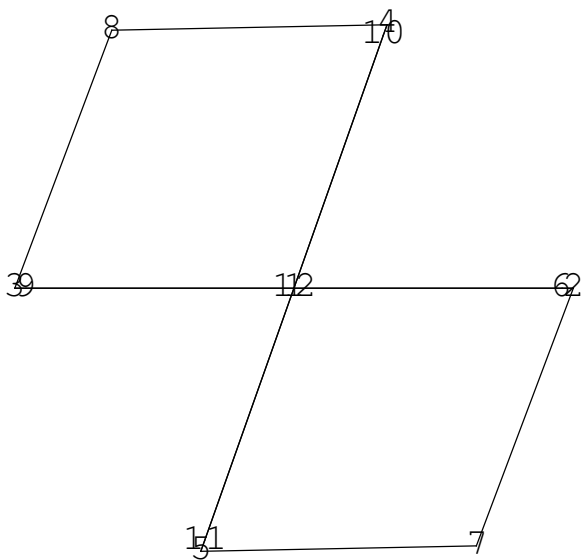
$$\left\{ \frac{8}{3}, 3, \frac{8}{3}, 4 \right\}$$



15.

cubohemioctahedron

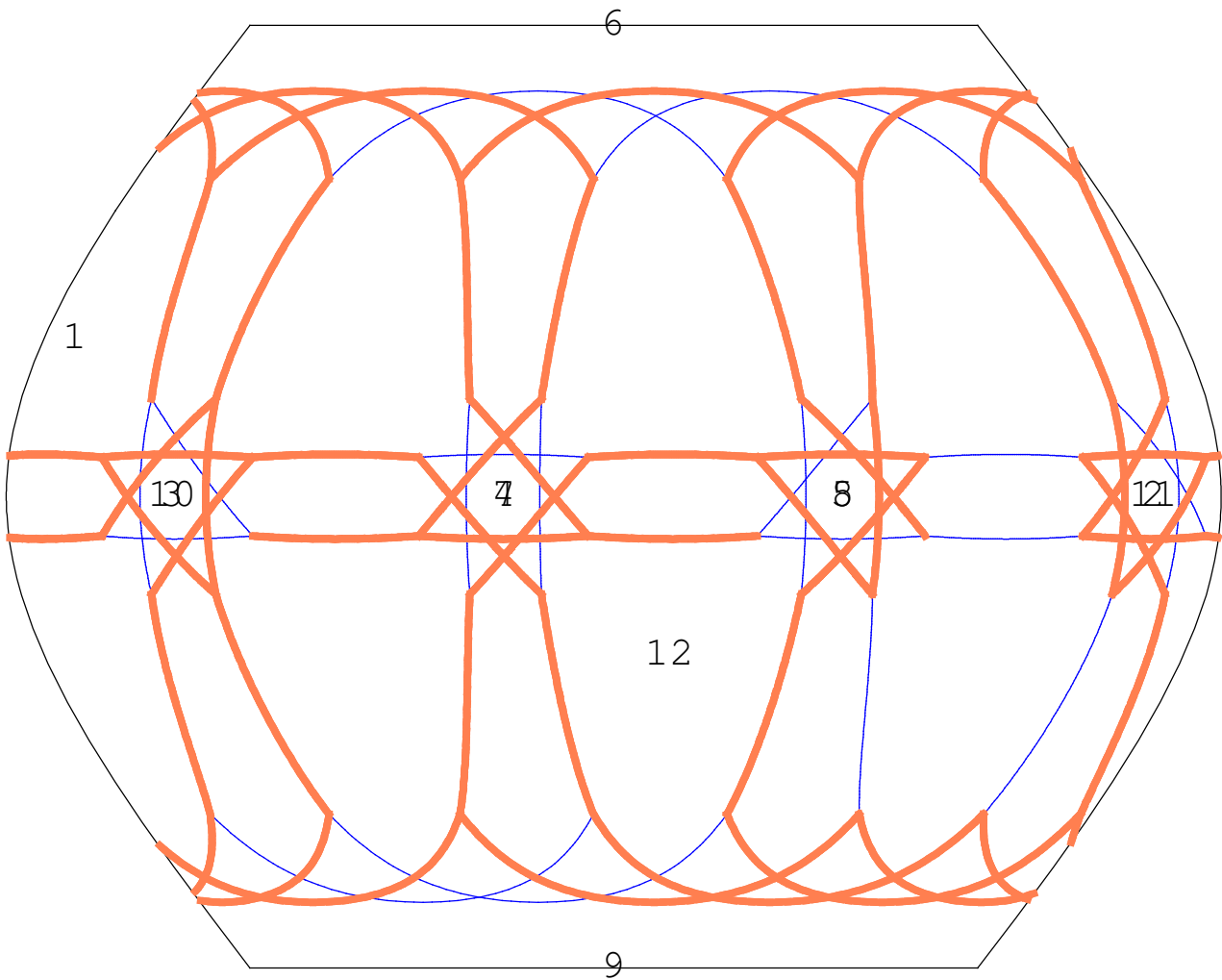
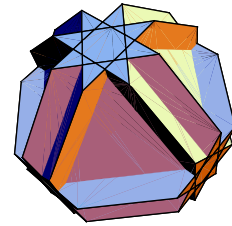
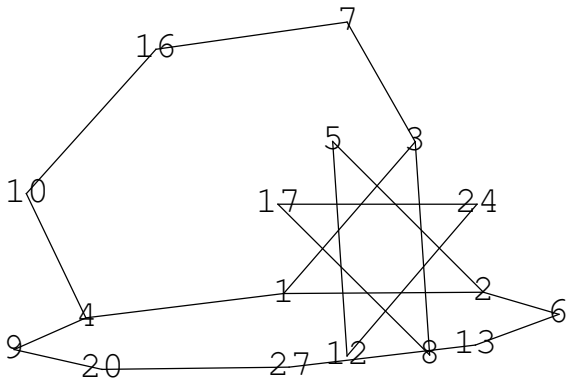
$$\left\{6, \frac{4}{3}, 6, 4\right\}$$



16.

cubitruncated cuboctahedron

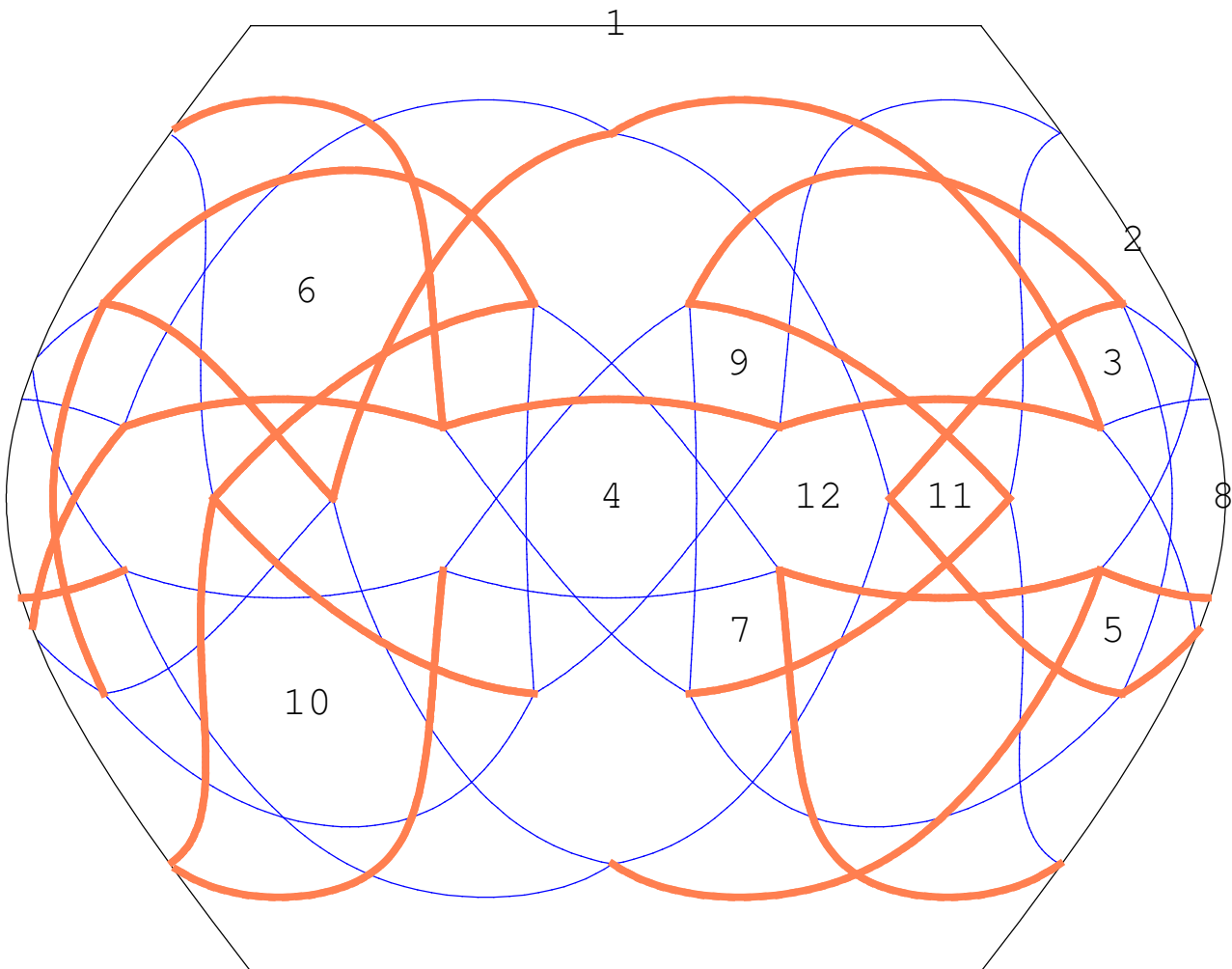
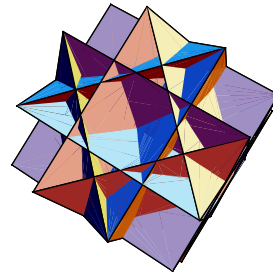
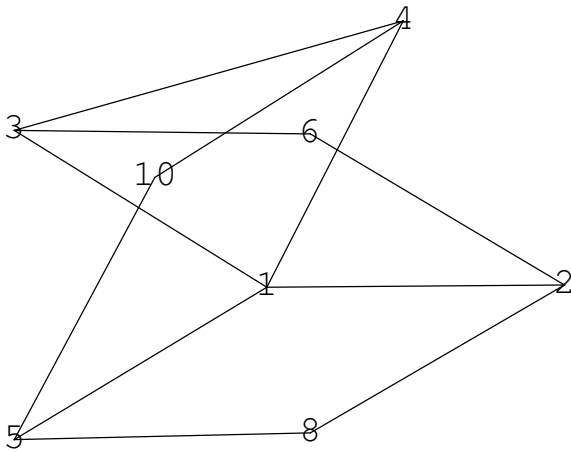
$$\left\{ \frac{8}{3}, 6, 8 \right\}$$



17.

great rhombicuboctahedron

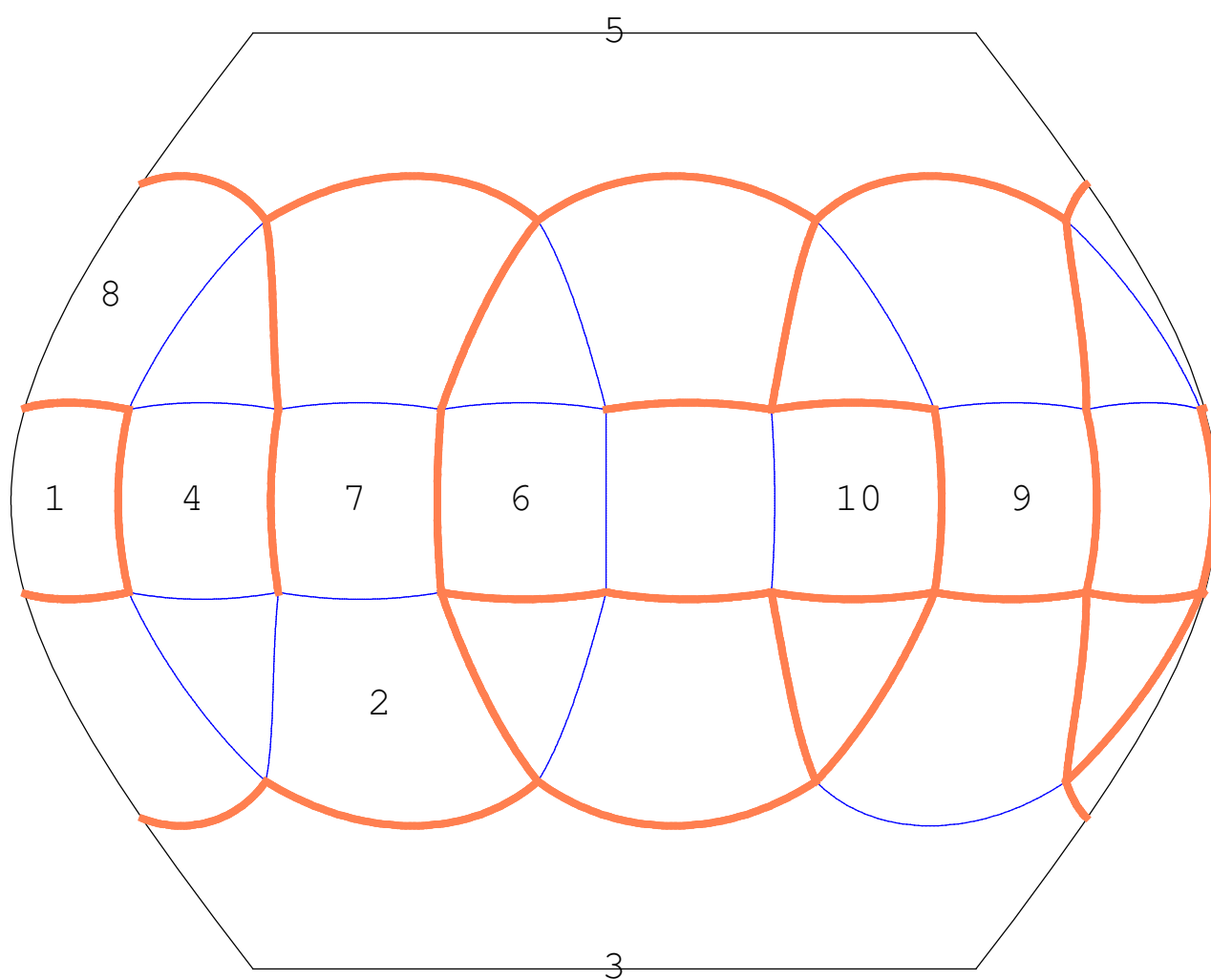
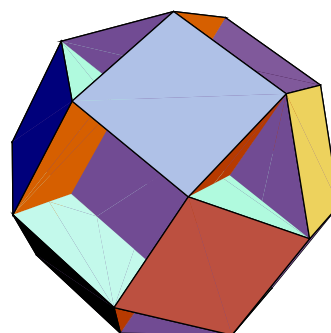
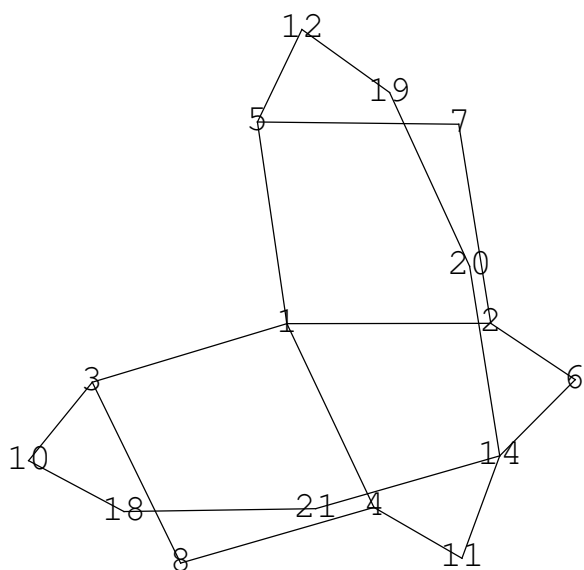
$$\{4, \frac{3}{2}, 4, 4\}$$



18.

small rhombihexahedron

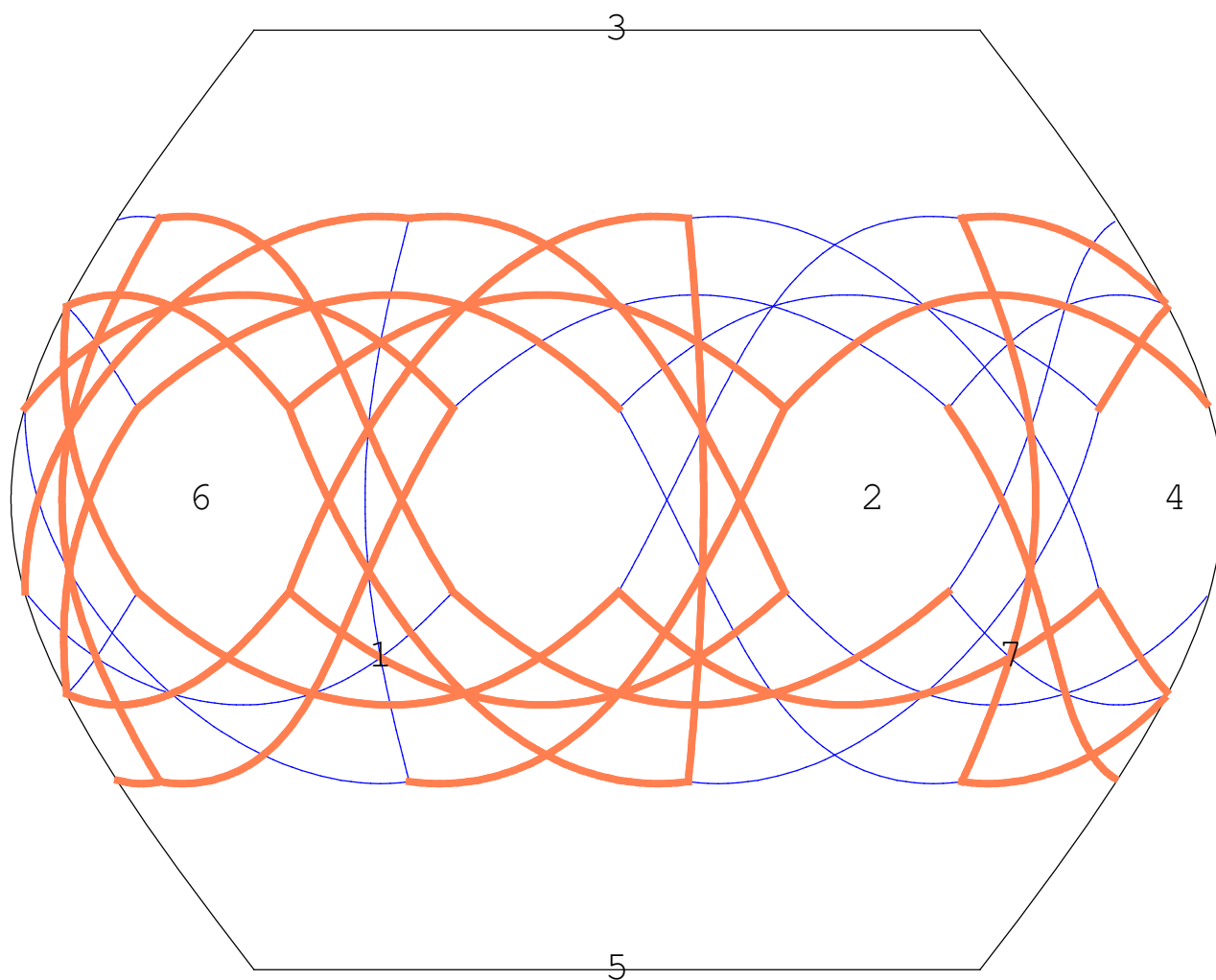
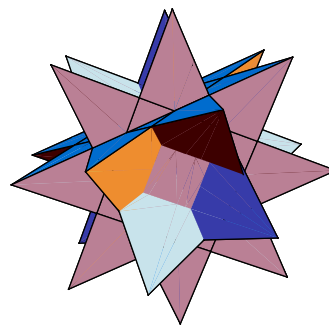
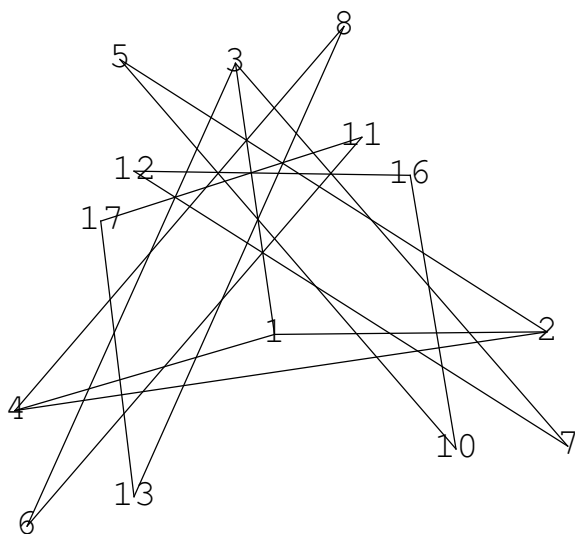
$$\{8, 4, \frac{8}{7}, \frac{4}{3}\}$$



19.

stellated truncated hexahedron

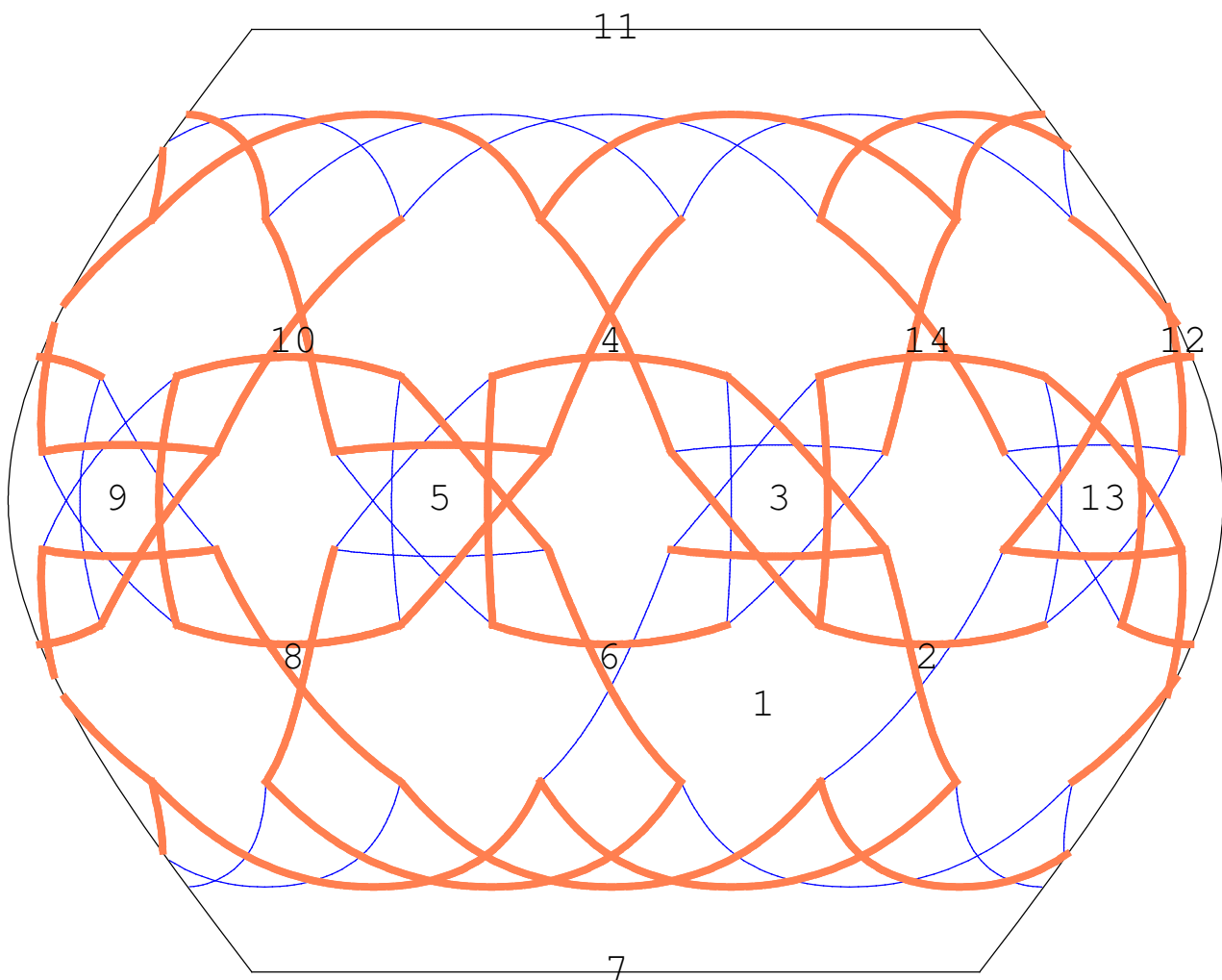
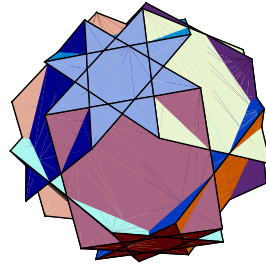
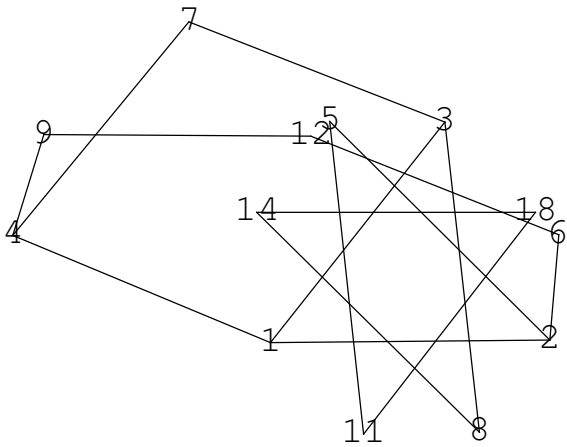
$$\left\{ \frac{8}{3}, \frac{8}{3}, 3 \right\}$$



20.

great truncated cuboctahedron

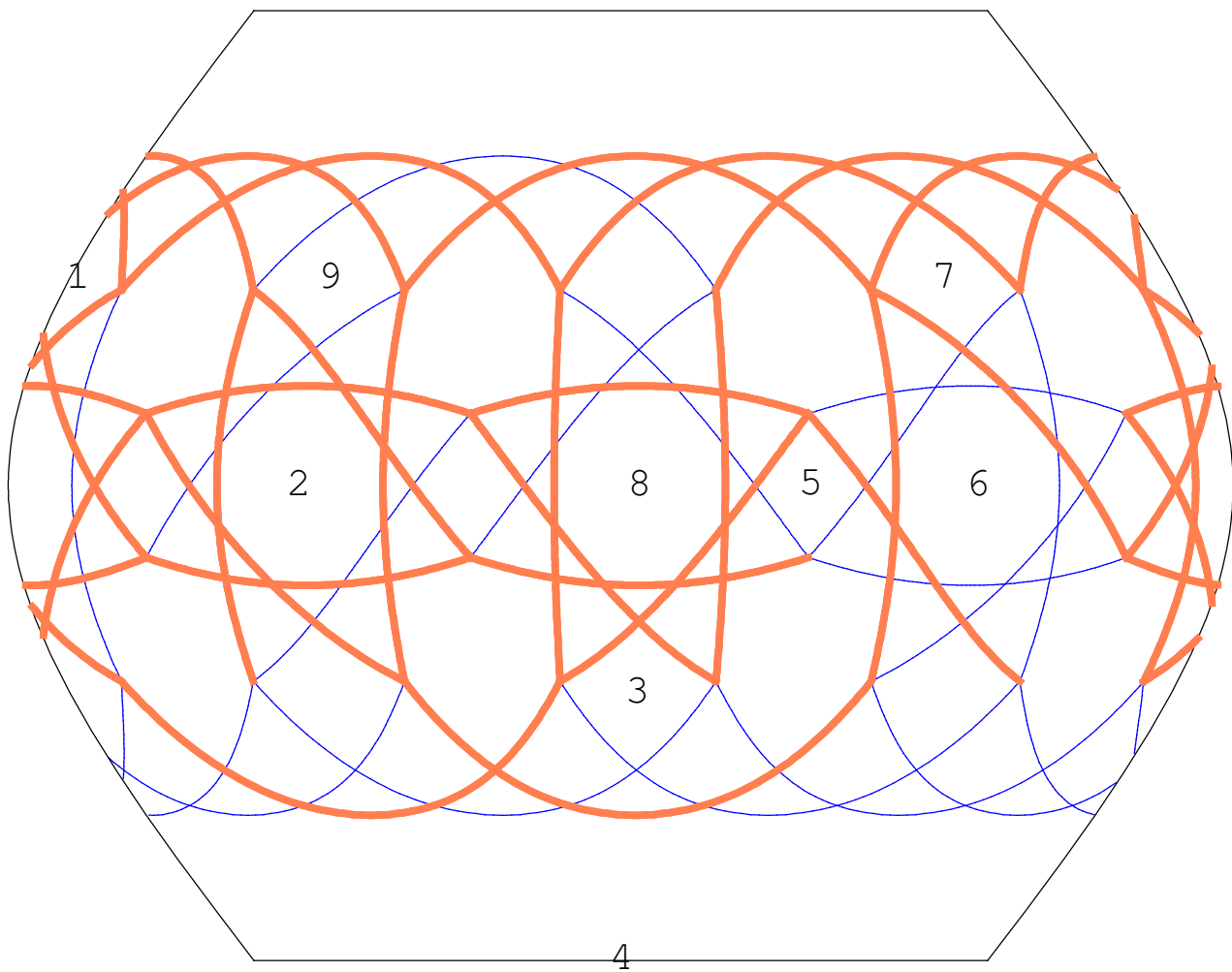
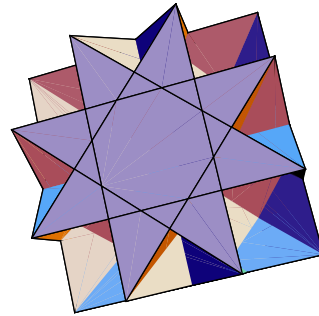
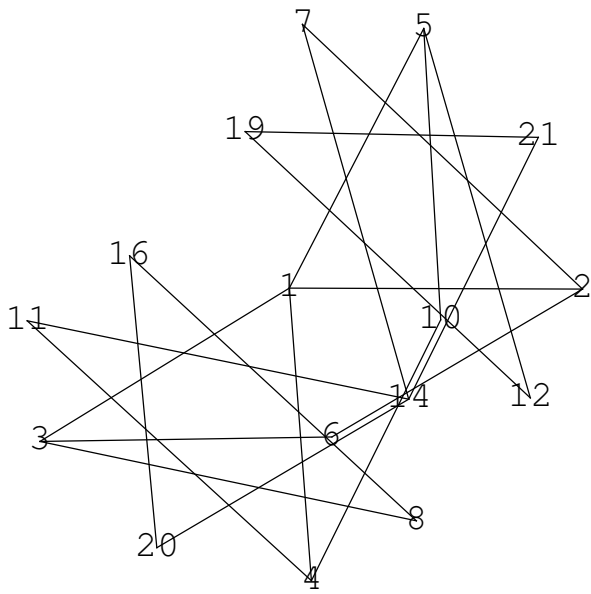
$$\left\{ \frac{8}{3}, 4, 6 \right\}$$



21.

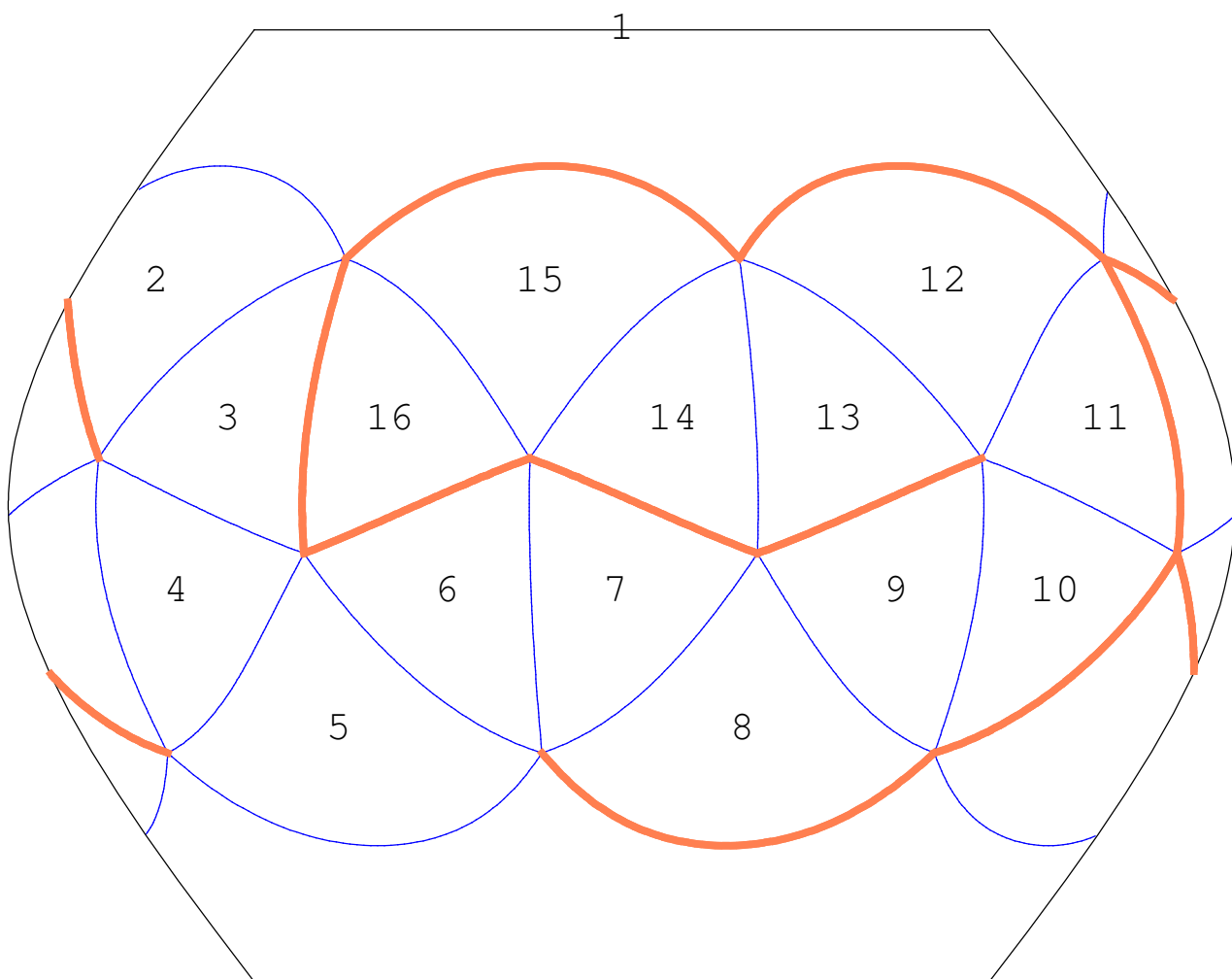
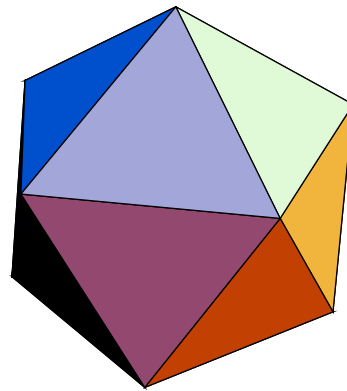
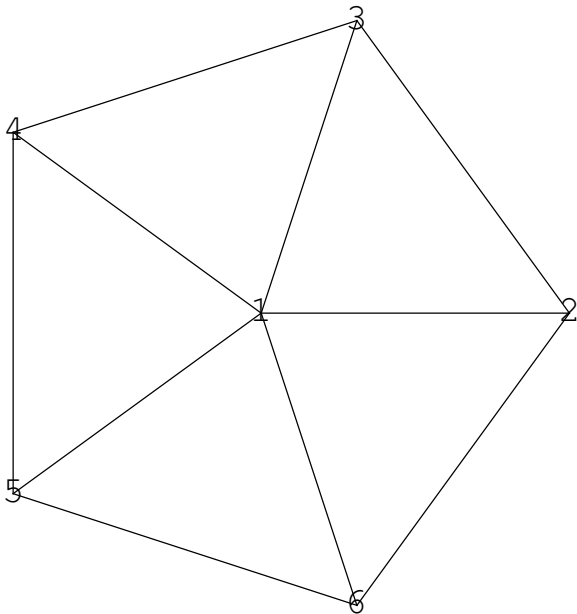
great rhombihexahedron

$$\left\{4, \frac{8}{3}, \frac{4}{3}, \frac{8}{5}\right\}$$



22.

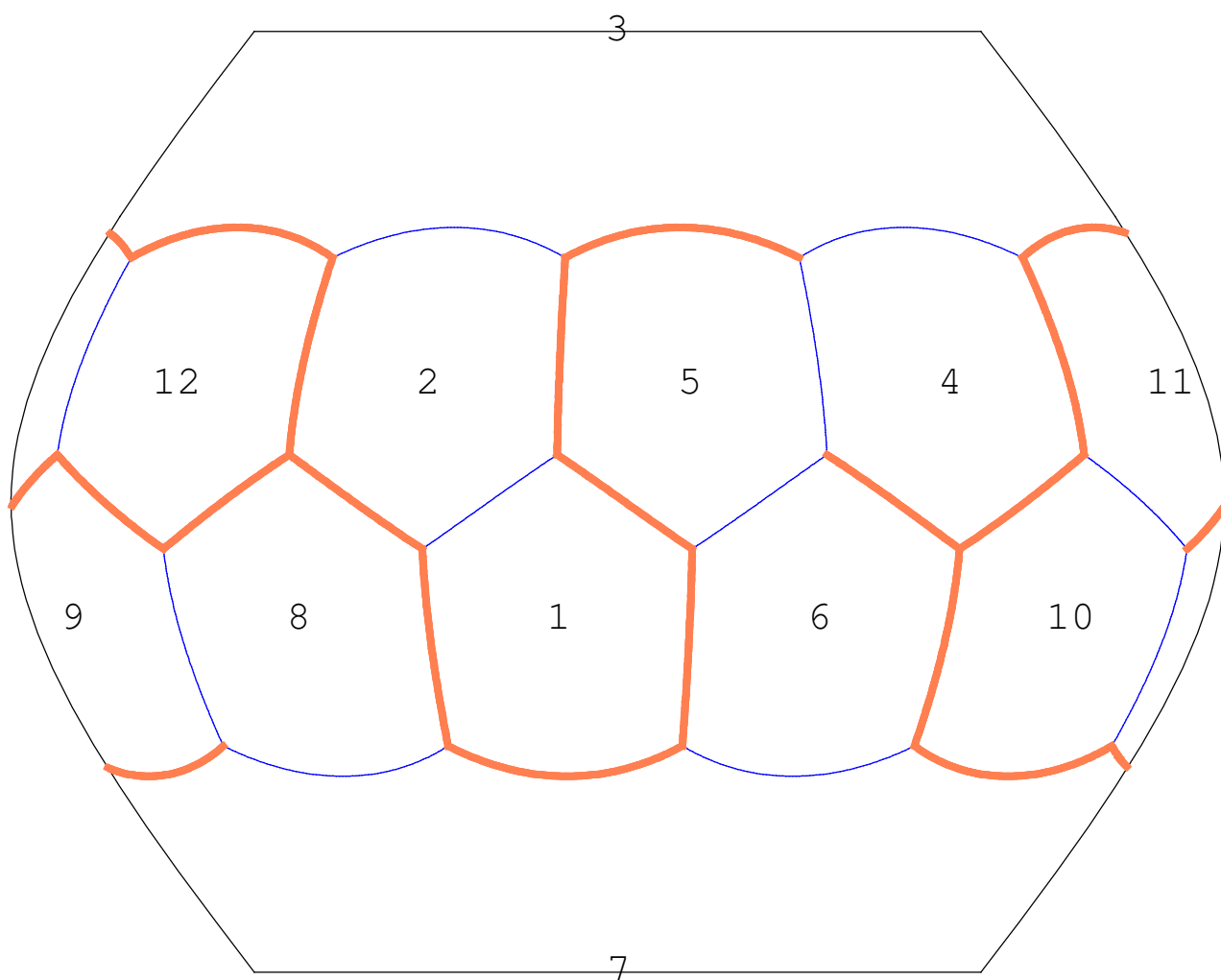
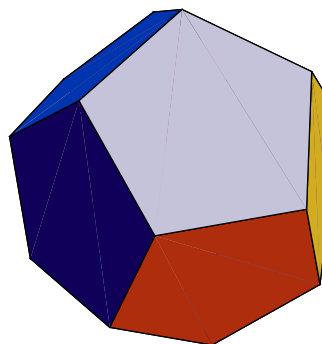
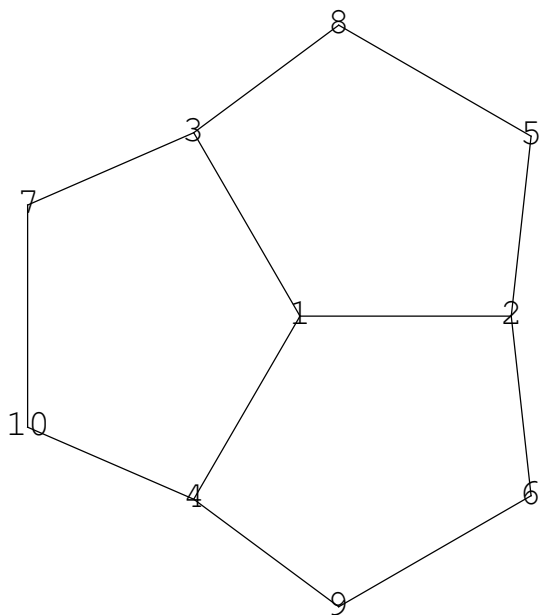
icosahedron

 $\{3, 3, 3, 3, 3\}$ 

23.

dodecahedron

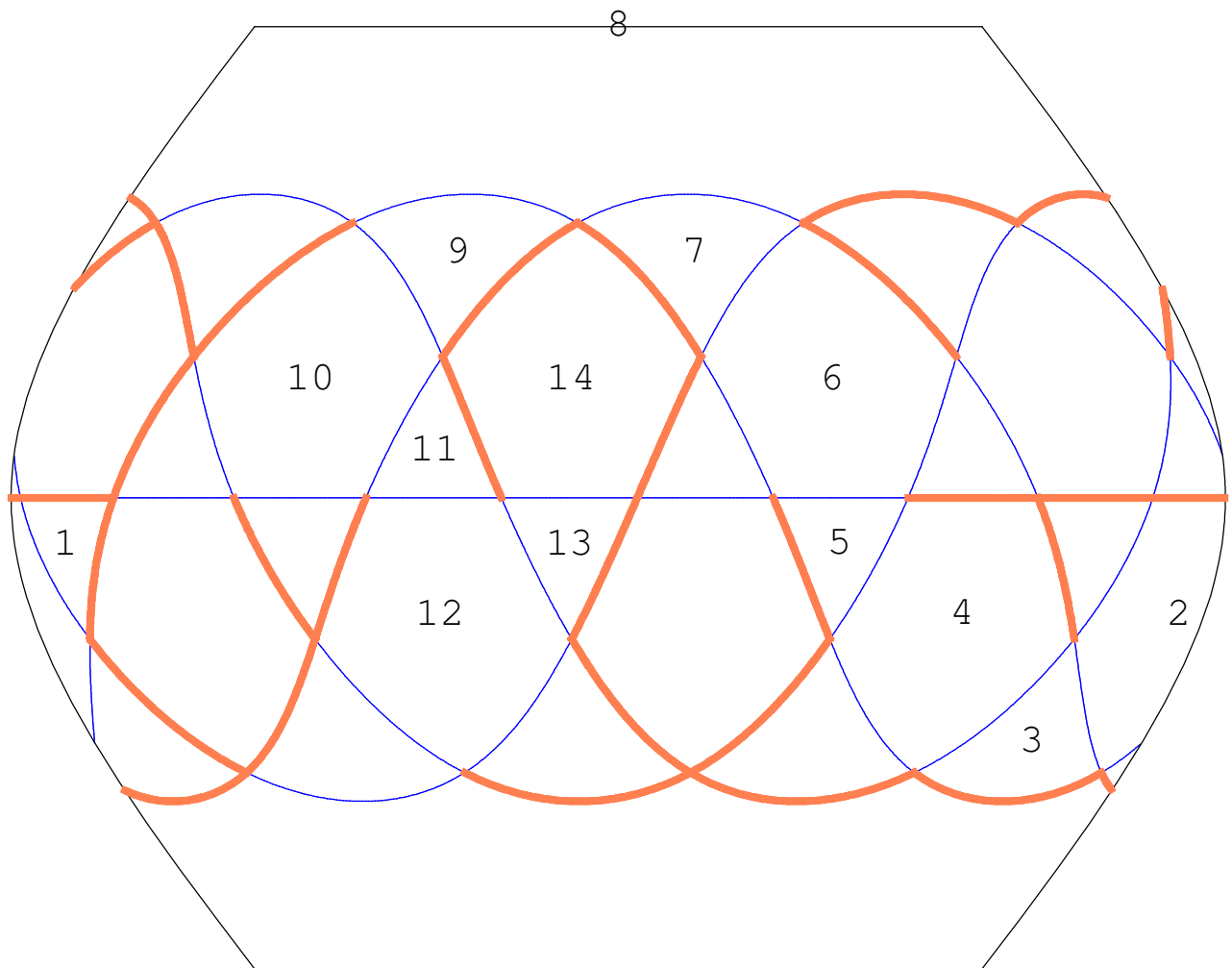
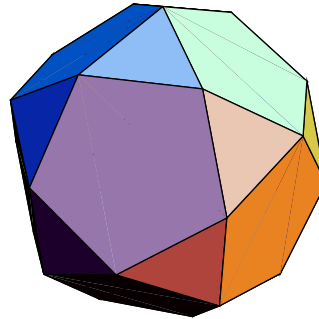
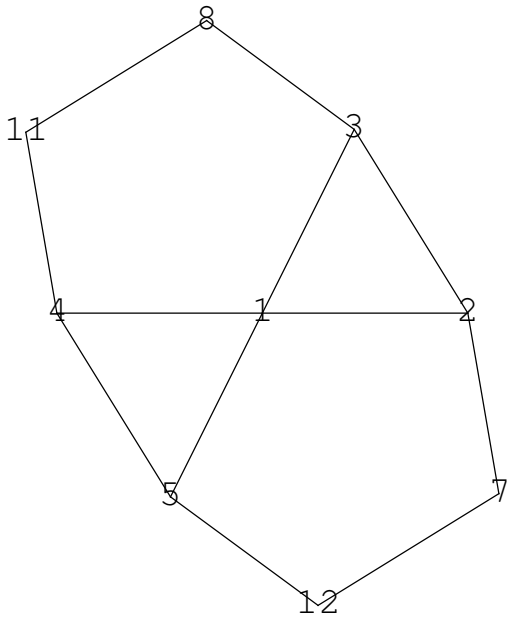
{5, 5, 5}



24.

icosidodecahedron

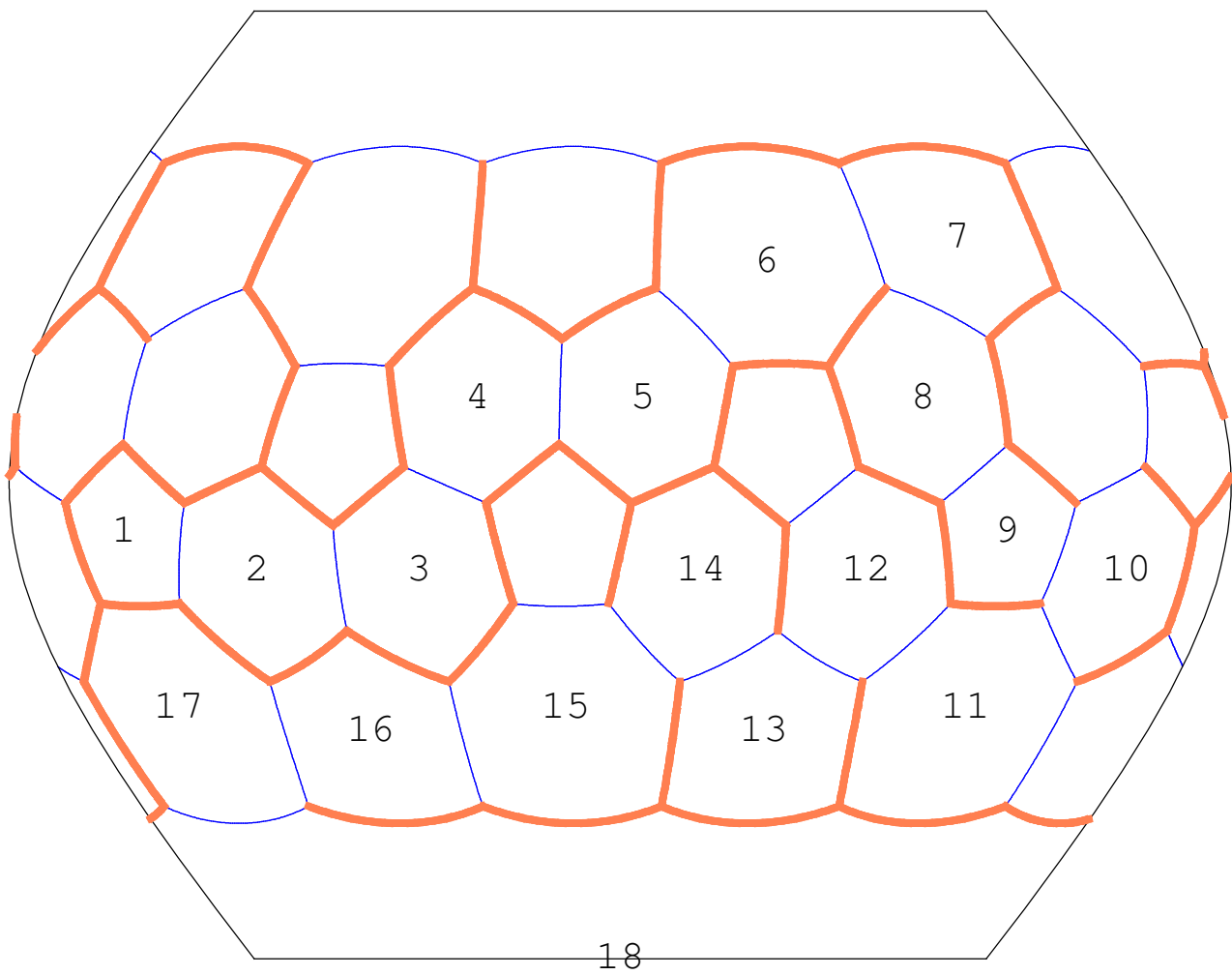
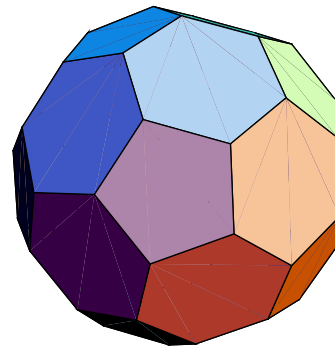
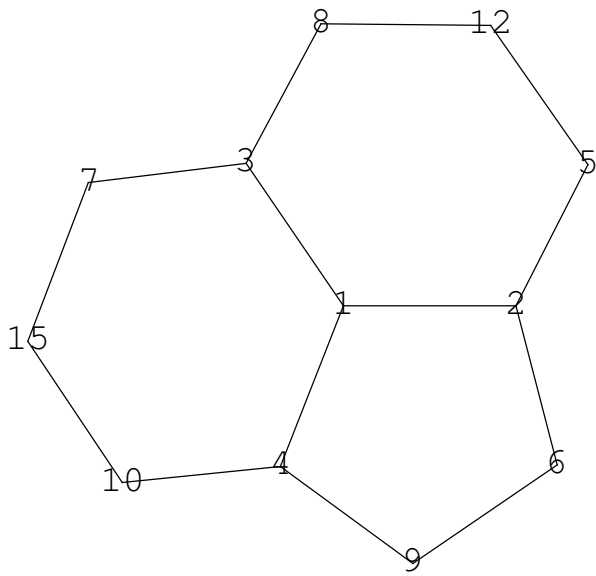
{3, 5, 3, 5}



25.

truncated icosahedron

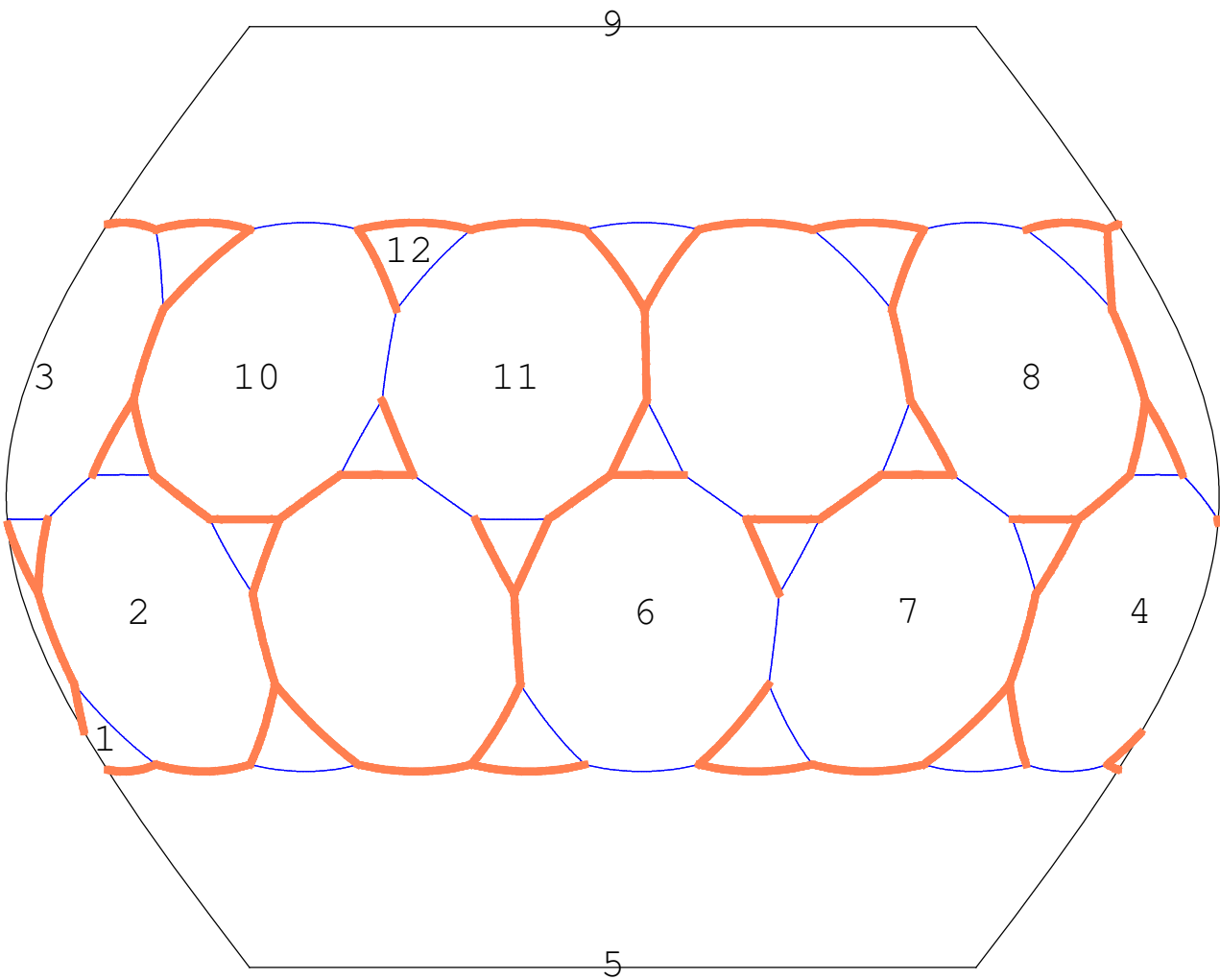
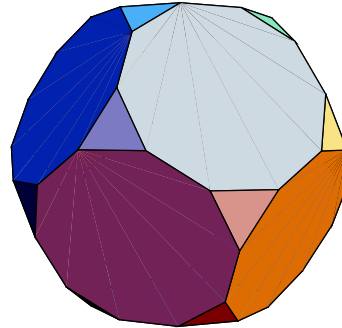
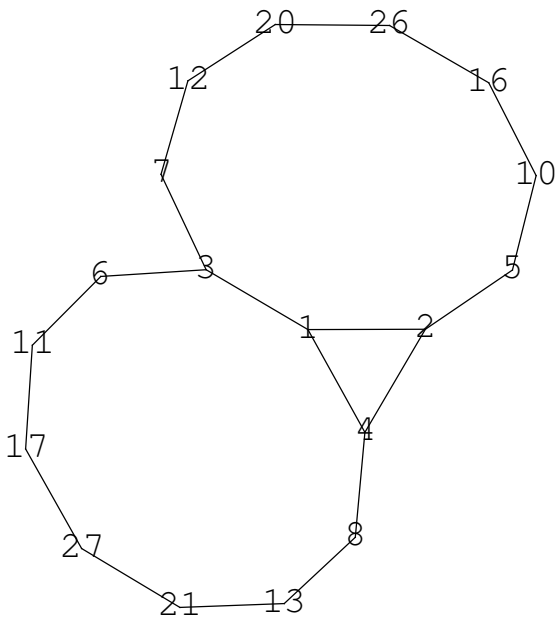
{6, 6, 5}



26.

truncated dodecahedron

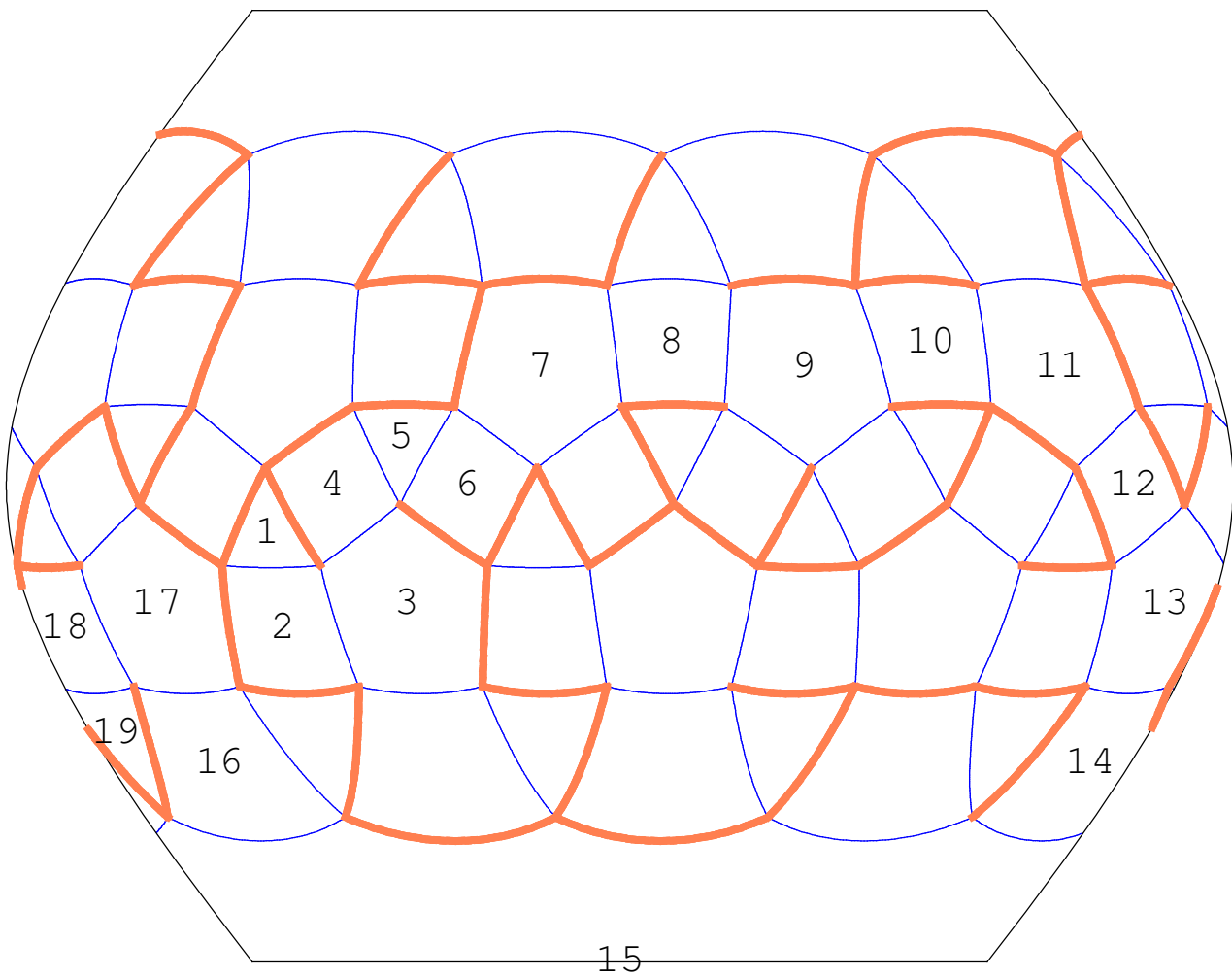
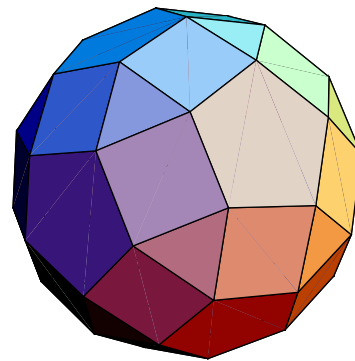
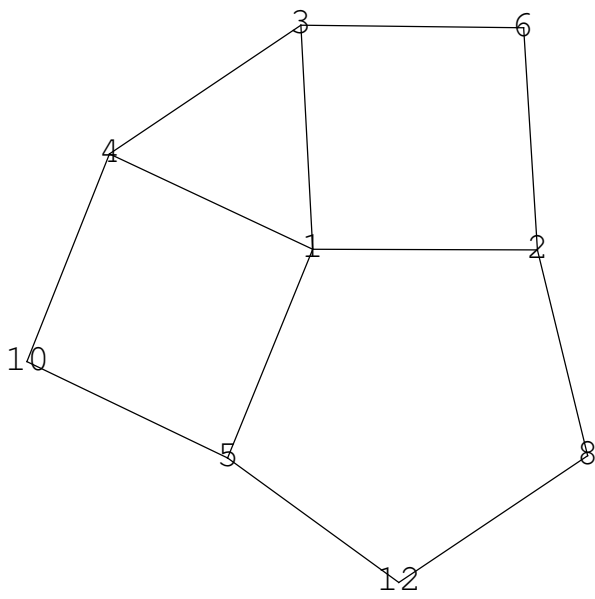
{10, 10, 3}



27.

rhombicosidodecahedron

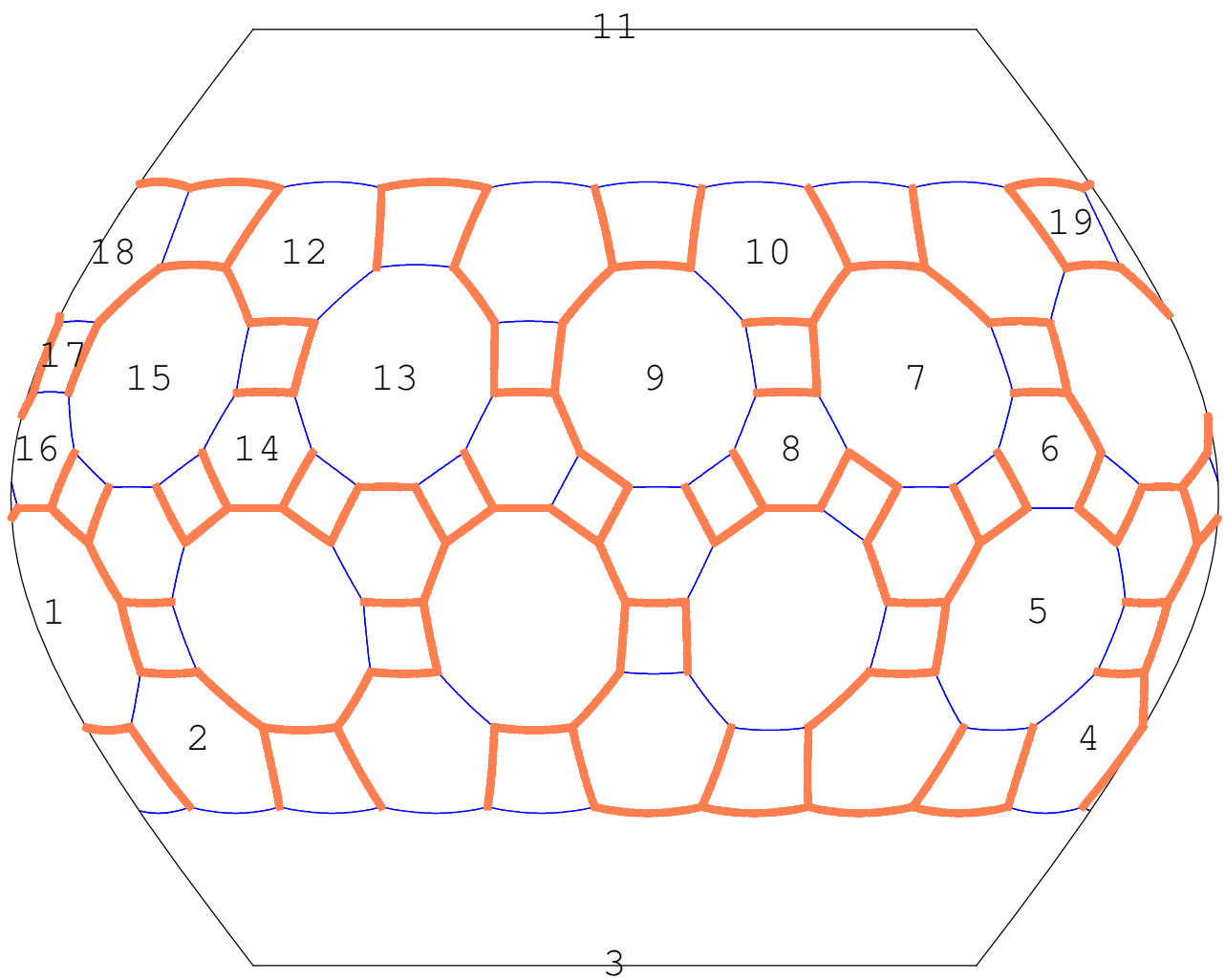
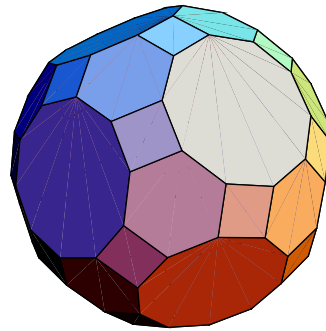
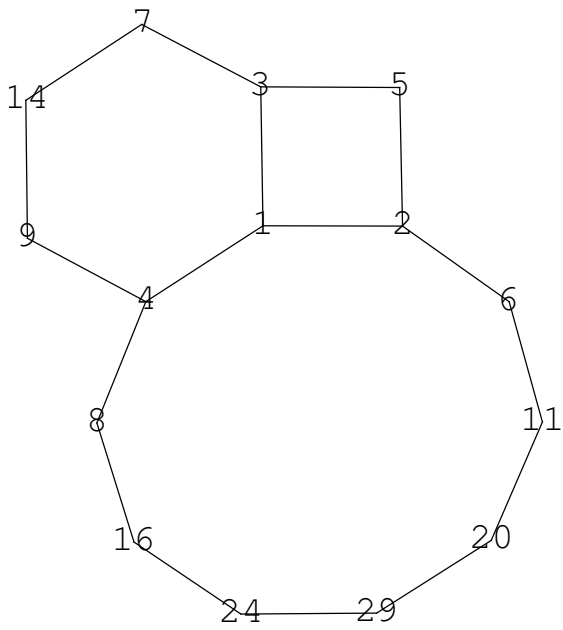
{4, 3, 4, 5}



28.

truncated icosidodecahedron

{4, 6, 10}



29.

snub dodecahedron

{3, 3, 3, 3, 5}

